Seismic Performance Evaluation Of Reinforced Concrete Frames

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Abstract: Ten storied -3bays reinforced concrete bare frame designed for gravity loads as per IS 456: 2000 (rev) and IS 13920: 1993 for ductility is subjected to seismic loads. Seismic loads considered is earthquake loads determined from IS 1893-2002 (part 1) response spectra for 5% damping (for hard soil). Structural elements are modeled as two node element (three degrees of freedom at each end). Plastic hinges are used to represent the failure mode in the beams and columns when member yields. Pushover analysis is performed using SAP 2000 V 14.0 commercial software in reference to various performance levels suggested in first, second and next generation performance based design procedures (ATC 40, FEMA 356, FEMA 440). Base shear versus top displacement curve of structure, known as pushover curve is obtained for force-displacement (brittle) and Deformation-controlled (ductile) actions of plastic hinge. Lateral deformation at performance point proves the building capability to sustain certain level of seismic loads. The failure mechanism indicates structural performance levels in accordance first, second and next generation PBSD procedures. The study aims towards understanding the first, second and next generation PBSD Procedures.

Keywords: PBSD evaluation procedures, Building frames, Plastic hinges, Pushover analysis, Seismic Performance

I. Introduction

Present seismic design codes, describes forced-based design procedures for lateral load resistance structures [1]. In static case loads on structure are low resulting in elastic behavior. During strong seismic event, these structures are subjected to loads beyond its elastic limits [2]. Though the present code can provide reliable indication of expected performance for life safety (strength and ductility) and damage control (serviceability drift limits) but are incapable to describe the expected performance, under large forces [3]. Performance based seismic design has emerged as best alternative towards present seismic code design procedure which is capable to describe the inelastic behavior of structure. PBSD, where inelastic structural analysis in combination to defined seismic hazard level is used to obtained expected performance of structure [1]. Second generation procedure presents improvements in first and second generation procedures [8]. Amongst this Nonlinear Dynamic Procedure (Time history, NLTH) is capable to calculate seismic responses under strong earthquakes, but results in large amount of data and time consuming process hence not considered practical.

Practicing field engineers prefers nonlinear static procedure (Pushover, NLSP) procedure due to easy and compatible compared to results obtained through NLTH [5-9]. First, second and next generation procedure provides various building performance levels based on contribution of structural and non structural performance levels in reference to transient and permanent drift as presented in table 2 [10]. The various structural performance levels and damage for vertical elements described by various PBSD procedures are presented in table 3 [7] and used for modeling of example building frame in present study.

Type of	? Analysis	Usual Name	Dynamic effects	linea	Material Non- rity
Linear	static	Equivalent static		No	No
Linear	dynamic	Response spectrum		Yes	No
Nonline	ear static	Pushover		No	Yes
Nonline	ear dynamic	Time history		Yes	Yes
FENA 2	73/356	Table 2: Building	g Performance Leve	ls [10]	
FEMA 27	73/356	Table 2: Building SEAOC vision 2	g Performance Leve	ls [10] ATC 58	
EMA 27	73/356 Performance	Table 2: Building SEAOC vision 2 Rating	g Performance Leve 2000 Performance Expostation	ls [10] ATC 58 Anticipated	Color code
TEMA 27 Rating 5-1	73/356 Performance Levels Immediate occupancy	Table 2: Building SEAOC vision 2 Rating 10	g Performance Leve 2000 Performance Expectation Fully operational	ls [10] ATC 58 Anticipated damage Negligible	Color code Green
EMA 27 Rating	73/356 Performance Levels Immediate occupancy Damage control	Table 2: Building SEAOC vision 2 Rating 10 9	g Performance Leve 2000 Performance Expectation Fully operational	ls [10] ATC 58 Anticipated damage Negligible	Color code Green
<u>*EMA 27</u> tating 1 2	73/356 Performance Levels Immediate occupancy Damage control	Table 2: Building SEAOC vision 2 Rating 10 9 8 7	g Performance Leve 2000 Performance Expectation Fully operational Operational	ls [10] ATC 58 Anticipated damage Negligible Light	Color code Green

Table 1: Various analysis procedures to estimate seismic demands suggested by second generation procedure [4]

		5			
S-4	Limited safety	4	Near collapse	Severe	Red
S-5	Collapse	3			
	prevention	2	Partial collapse	Complete	
		2	Partial collapse-		
			assembly areas		
		1	Total collapse		

Table 3: Performance levels corresponding to damage states and drift limits [7]

Structural Performance		Damage state	Transient	Permanent
level			Drift	drift
Imm ediate occupancy	Minor hair lin	e cracking	1%	Negligible
Life safety	Extensive dan shear cracking	age to beams, spalling of cover and	2%	1%
Collapse	Extensive cra	king and hinge formation	4%	Permanent

Performance based design procedures

Interest in performance based seismic design initiated in the 1980s amongst engineers engaged in seismic design and retrofit of existing buildings [1-3]. The roots of PBSD can be traced from the development of recommendation by the Structural Engineers Association of California (SEAOC, 1960), and the publication by the Portland Cement Association (PCA). Later Joint efforts of Federal Emergency Management Agency (FEMA) and Applied Technical Council (ATC) results in publication of document named ATC 40 (1996) [5].

First Generation procedures

ATC-40 procedure involves comparison between capacity of structure (Pushover curve) and demands on the structure (Demand spectrum) and their graphical instruction is termed as performance point. The target displacement is computed as maximum displacement of a linearly ESDOF system with time period T_{eq} and effective damping

ratio \square_{eq} [15]

Second Generation Procedure

FEMA 273 (1997) [6] provides simplest and straight forward method of estimating target displacement using ductility. It does not require converting the capacity curve to spectral coordinates. The nonlinear forcedisplacement relationship between base shear and displacement is replaced with an idealized bilinear relationship to calculate the effective initial lateral stiffness K_e and post yield stiffness K_s and effective yield strength V_y of the structure. The target displacement in displacement coefficient method (DCM) is computed as, $\Box_t \Box \Box \Box C_0 \Box C_1 C_2 \Box C_3 \Box S \Box_a \Box \Box^{T \sqcup e^2}_{2} \Box$ g

 C_0 = modification factor to relate spectral displacement of an equivalent SDOF system to the roof displacement of the building MDOF system.

 C_1 = modification factor to relate the expected maximum inelastic displacement calculated for linear elastic range.

 C_2 = modification factor to represent the effect of pinched hysteretic shape, stiffness degradation and strengthdecoration.

 C_3 = modification factor to represent increased displacement due to dynamics $P \Box \Box$ deffects.

Later FEMA 356 (2000), presents an incremental improvement to the first generation procedure i.e. FEMA 273 in respect of technical updates to the analytical requirement and acceptance criteria based on the information gained from the physical application in engineering practice and case study given by FEMA 349 [4, 7].

D	Particulars	Assumptions			
	1Type of structure	Multi-storie	ed rigid frame (moment re	esisting frame)	
	2Seismic zone	IV (table 2	I.S. 1893:2002(part 1)		
	3No. of stories	Ten storied	(G+9)		
	4Floor height	3m			
	5Tributary width	3m			
	6Imposed load	3 kN/m^2			
	7Materials	Concrete:			
		a. Weight j	per unit volume 25 kN/m ³		
		b. Mass pe	r unit volume 2.5485 Kg/	m ³	
		c. Modulus d. Poisson	s of elasticity (E_c)= 5000 v ratio (μ) 0.20	$f_{ck} = 25000 \text{ kNm}$	
		e. Coefficie	ent of thermal expansion ((α) 5.50 E-06	
		f. Shear m	odulus (G) 1041667 kN/r	n^2	
		g. Characte Reinforcen	eristic strength $(f_{ck}) = 250$ nent:	00 kN/m ²	
		a.	Weight per unit volur	ne 76.9729 kN/m ³	
		b.	Mass per unit volume	7.849 Kg/m ³	
		c.	Modulus of elasticity	$(E_{s}) = 2E + 08 \text{ kNm}$	
		d.	Poisson ratio (µ) 0.30		
		e.	Coefficient of therma	expansion (α) 1.17 E-05	
		f.	Shear modulus (G) 76	6923077 kN/m ²	
		g.	Yield strength (f _y) 41:	500 kN/m^2	
		h.	Minimum tensile stre	ss (f _u) 485000 kN/m ²	
		i.	Expected yield streng	th (f _e) 456500 kN/m ²	
		j.	Expected tensile stres	s (f _{ue}) 533500 kN/m ²	
8	8 Size of columns	(obtained	l from gravity analysis)		
		Floors S	ize of columns	Main bars(Tor)	Shear bars (Tor)
		01-03 65	50 mm x 650 mm 16 No-1	2 mm	10mm@ 110 mm c/c
		04-06 50	00 mm x 500 mm 10 No-1	2 mm	
) <u>Ciacofference</u>	07-10 40 Deth lea	00 mm x 400 mm 08 No-1	2 mm	08mm@ 100 mm c/c
2	Size of beams	Electro Si	gitudinal and lateral (obta	Main hars(Tar)	Shoon hone (Ton)
		01.03	200 mm x 450 mm	4No 12 mm	$\frac{110}{8}$
		04-06	$300 \text{ mm} \times 450 \text{ mm}$	4 No-12 mm	8mm@ 100 mm c/c
		07-10	300 mm x 450 mm	3 No-12 mm	8mm@ 100 mm c/c
1	0 Denth of slab	150 mm	thick	5 110-12 milli	omme 100 mm c/c
1	2 Type of soil	Rock	linex		
1	 a Response spectra 	As par I	\$ 1893.2002(part1) com	natible for 5 % damning	

Table 4: Assumed preliminary data required for analysis of frame

Next generation procedures

Both first generation (ATC 40, FEMA 273) and second generation (FEMA 356) methods have shortcomings as [11];

- 1. Current procedure predict structural response and demand based on the global behaviour but evaluates performance with reference to damage sustained by individual components resulting (poorest performing element) leading towards misunderstanding of actual structural response.
- 2. Much of the acceptance criteria contained in document are based on judgement irrespective of laboratory test results or evidence leads towards questioning the reliability of procedures.
- 3. The guidelines are extensively conservative compared to perspective design criteria.
- 4. Performance levels defined in document does not directly address primary concerns of owner and designer i.e. probable repair costs, downtime and casualties

Based on these shortcomings FEMA 440 proposed some improvements in capacity spectrum and displacement coefficient method. The improved capacity spectrum method presented in FEMA-440 document suggested empirical expression to calculate effective period and effective damping independent of hysteretic model type and Post-yield slopes. Improved displacement coefficient presented in FEMA 440 is accepted by ASCE-41. Modification of coefficient C_1 , C_2 , and C_3 is done [12].



Building frame

The example 2D- RC frame is 3 bays, 10 storied bare frame representing high rise RC building frame. The building is designed in accordance to IS 456: 2000(rev) [13] and IS 13920:1993 [15] ductility provision. The width of bay is 3m and height of each storey is 3m. Figure 1, describes dimension of building and member designation. The preliminary data assumed and gravity design result is presented in table 4. For the example building all floors carries a dead load of 4.75 kN/m^2 and live load of 3kN/m^2 except for roof level. The earthquake forces are calculated for the dead load plus the percentage of imposed load as defined in Table 8 of I.S 1893 (Part 1): 2002 [14]. The imposed load on roof is assumed to be zero as per clause No.7.3.2 of I.S 1893 (Part 1): 2002. The lumped masses of each floor, base shear force and vertical distribution of base shear (obtained as per clause no. 7.7.1 of I.S. 1893(part 1): 2002) are presented in table 5.

T-11. 5. Co

Storey Level	Weight (kN)	Mass (x 10 ³ kgs)	Vertical shear distribution (kN)	Modal time period (secs)	Modal frequency (rad/sec)	Lumped Stiffness (x 10 ³ kNm)
Roof 9 th floor	441.45 499.50	45.00 50.92	76.57 70.17	0.0309 0.0344	203.11 182.48	130.06 130.06
8 th floor	499.50	50.92	2 55.45	0.0366	171.60	130.06
7 th floor	553.16	56.39	47.01	0.0420	149.47	130.06
6 th floor	593.33	60.48	37.05	0.0526	114.84	317.57
5 th floor	593.33	60.48	25.73	0.0718	119.34	317.52
4 th floor	694.41	70.84	19.27	0.0718	87.471	317.52
3 rd floor	788.06	80.33	12.30	0.1047	59.972	906.90
2 nd floor	788.06	80.33	5.47	0.1857	33.825	906.90
1 st floor	788.06	80.33	1.37	0.4949	12.695	906.90

Pushover Analysis

Since mid 90s, pushover analysis finds its way to seismic guidelines viz. SEAOC (1996), ATC 40 (1996), FEMA 273/274 (1997), FEMA 356/357 (2000), ATC 55 (2005) and FEMA 440 (2005). Procedure consists of applying vertical distribution of lateral loads to a model which captures the material non-linearity of an existing or newly design structure. Loads are increased monotonically until the peak response of the structure is obtained on a base shear versus roof displacement plot.

Performance based evaluation procedures (ATC 40, FEMA 356, FEMA 440) documents have published modeling parameters, acceptance criteria, and procedures for pushover analysis. In present study second generation procedure FEMA 356 guidelines related to modeling parameter and acceptance criteria is adopted. The document put forth two sections to determine the yielding of frame member during the pushover analysis as shown in figure 2 viz. deformation-controlled (ductile action) or force-controlled (brittle action) of plastic hinge. Figure 2(a) represents the idealized inelastic force-deformation relationship for displacement-controlled action under flexure. Points labeled A, B, C, D, E represents various performance levels expressed directly in terms of strain, curvature, rotation, or elongation. Figure 2(b) represents force-deformation relationship for plastic hinge under force-control (shear failure) [7]

Table 6: Modeling parameters and numerical acceptance criteria for nonlinear procedures (reinforced concrete columns) [7]

Conditions		Modeling Parameters			Acceptance Criteria			
		Plastic rotatic angle (radian	on s)	Residual strength	Plasti	c rotation angle (Performance lev	(radians) vel	
P Trans.	V			ratio		IOCompor	nent type	
Reinf. A _g f _c	b d f'				Primary	LACE	Secondary	CD
	w c	a	b	с		LSCP	LS	CP
≤ 0.1 C	≤ 3	0.02	0.03	0.2	0.0	050.0150.02	0.02	0.03

The parameters (a, b) represents the portion after plastic deformation (yield). Parameter (c) represents reduced resistance after sudden reduction from C to D. Numerical values of a, b and c adopted for present example is presented in table 6 and table 7. These parameters depend on the sectional properties such as, percentage of steel (tension and compression), balanced percentage of steel, design shear strength, design axial load, characteristic strength and cross-sectional dimensions.

 Table 7: Modeling parameters and numerical acceptance criteria for nonlinear procedures (reinforced concrete beams) [7]

Conditions			Modeling Parameters			Acceptance Criteria			
		Plastic rotation		Residual	Plastic rotation angle (radians)				
			angle (ra	adians)	streng th	Perf	ormance le	vel	
ŰĽĤ	Trans.				ratio	IO	Compor	ient type	
	Reinf.					Pri	mary	Secon	dary
al bal		b _w d∖ f _c '	a	b	с	LS	CP	LS	CP
≥0.5	С	≤3	0.02	0.03	0.2	0.0050.01	0 0.02	0.02	0.03



Acceptance criteria or performance levels for the plastic hinge formed near the ends of columns and beams are represented by IO (Immediate Occupancy), LS (Life Safety), and CP (Collapse Prevention). Default values given in software SAP 2000 V 14.0 [16] is used to represent P-M interaction curve (ACI code 2000), stress-strain curve for concrete (Kent and Park), M- θ relationship which represents acceptance criteria corresponding to performance levels.

Seismic Performance

The present study aims to assess seismic response of ten storey building frame for preliminary data considered in table 4. The static nonlinear analysis (pushover analysis) of lateral seismic forces is preferably applied after initial pushover analysis for dead load plus live load combination. Figure 3 shows the capacity responses of deformation-control actions of application of forces in reference to FEMA 356 (2000) guidelines. The maximum value of base shear, ultimate roof displacement and the ratio of base shear value obtained from pushover analysis to IS 1893:2002 codes are presented in table 8.



Figure 3: Capacity curve of building

Table 8: Characteristics of performance point according to performance based evaluation procedure presented i
first, second and next generation procedures

Performance evaluation		Maximum	Ultimate displacement of	Ratio of maximum base shear to
procedure		base shear	roof (m)	base shear obtained by IS 1893:
		(kN)		2002 (part 1)
ATC 40 (CSM	A)	371.264	0.048	1.06
FEMA 356	(DCM)	404.247	0.068	1.154
FEMA 440	(ACSM)	382.553	0.054	1.092
FEMA 440	(MDCM)	420.168	0.078	1.20

Figure 4 represents the capacity response of two actions of the plastic hinges up to failure, once when the hinge is subjected to the shear failure and another one to flexural failure. The maximum base shear of the structure and the ultimate roof displacement are presented in table 9.



(a) Displacement-Controlled action (b) Force-Controlled action Figure 4: Capacity curve of building for different control actions for plastic hinge

Table 9: Characteristics of performance point for (a) displacement-controlled and (b) force-controlled options for plastic hinges according to performance based evaluation procedure presented in first, second and next generation procedures

Performance evaluation procedure	Maximum base shear	(kN)	Ultimate displacement of roof (m)		
	Displacement-	Force-	Displacement-	Force-	
	controlled	Controlled	controlled	Controlled	
ATC 40 (CSM)	371.264	733.870	0.048	0.057	
FEMA 356 (DCM)	404.247	674.184	0.068	0.052	
FEMA 440 (ACSM) FEMA 440 (MDCM)	382.553	733.871	0.054	0.057	
FEMA 440 (MDCM)	420.108	035.333	0.078	0.031	

Figure 5 shows the plastic hinge patterns at final load step of loading and control options which govern the behavior of plastic hinge during analysis. Performance levels are illustrated by appropriate color codes based on acceptance criteria.

Figure 6 shows the capacity curve of the frame structure according to FEMA 440 (MDCM) approach. Displacement ductility represents a simple quantitative indication of severity of the peak displacement to the displacement necessary to initiate yielding for the present case it works out to be 3.795. Ductility ratio directly affects hysteretic behavior in reinforced concrete structures. Lateral deformations at the performance point are checked against the deformation limits as illustrated in table 10. Maximum total drift is defined as storey drift corresponding to performance point. Maximum inelastic drift is the portion total drift beyond the effective yield point.





(a) Displacement-controlled option (b) Force-controlled option Figure 5: Plastic hinge patterns at final load step - displacement and force controlled actions of plastic hinge during analysis

Storey drift	ATC 40	FEMA 440		Р	erformance le	evel	
	(CSM)	(ACSM)	Immediate occupancy		Damage control	Life safety	Structural stability
Maximum	0.048	0.0	1 9	0.01	0.01-0.02	0.02	$0.33 \square S_i W_i \square$
total drift							(0.01853) at roof
Maximum	0.0288	0.03	48	0.005	0.005-	No limit	No limit
inelastic drift					0.015		
	File Static Nonlinear Case ACASE1 500. 450. 450. 300. 250. 200. 150. 100. 50. 0.17. 0.17. Mouse Point	Calcul B Calcul B Calcul Calcu	Lunits Ki Lunits Ki CO C1 C2 Sa Te Ti Ki Ki Ke Alpha R Vy Dy Weight Cm Dor	I, m, C Value 1.3046 1.10600 1.11 0.4000 0.4000 1.2249.6 0.1652 1.2249.6 0.1652 1.2249.6 0.1252 1.2249.6 1.2249.6 0.1252 1.2249.6	▼ ent Plot F F440P Add Moc 15 15 15 15 15 148 Shr	Units KN, m, C Grameters DDM1 Grameters Grameters Grameters Grameters Cement (V, D) S8, 0.078 W Calculated Values	

Figure 6: Capacity curve of the frame according to FEMA 440 (MDCM)

For the structural stability, the maximum total drift in story i at the performance point should not exceed the quantity of $0.33 \square S_i / W_i \square$, where S_i is the total calculated shear in story i and W_i is the gravity load at story i [7].

II. Conclusions

Performance evaluation procedure recommended in first, second and next generation procedure utilizes pushover analysis to estimate the capacity of RC structures towards given seismic supply. The documents provide acceptance criteria in terms of performance levels based on transient and permanent drift. In order to represent inelastic behavior structural elements are modeled with elastic hinges at the ends for both beams and columns. The formation of collapse mechanism by yielding of plastic hinges inelastic behavior of components can be concluded as:

- The maximum base shear of the structure and ultimate roof displacement obtained for first, second and next generation procedure are in close tolerance to values of base shear deduced from I.S 1893: 2002 (part 1).
- The document describes two actions to determine yielding of frame members during inelastic analysis viz.;
- (a) Displacement-controlled (flexure) and, (b) force-controlled (brittle) actions. When the frame was modelled for deformation-controlled action shows sequence of formation of plastic hinges in the beams only. This shows building clearly behaves like strong column-weak beam mechanism.
- When the frame was modelled for force-controlled (brittle) shows the formation of hinges in columns because of inadequate shear reinforcement.
- Lateral deformations of example building at the performance points for ATC 40 (CSM) and FEMA 440 (ACSM) when checked against maximum total drift, maximum inelastic drift and structural stability that it's safe for life against seismic loads.
- The ductility ratio of the frame structure according to displacement coefficient method FEMA 356 (DCM) and FEMA 440 (MDCM) gives a simple quantitative indication of the severity of the peak displacement relative to the displacement necessary to initiate yielding.

- [□] Comparing both the action i.e. displacement-controlled and force-controlled actions, force-controlled actions place the structure in the severity level.
- □ Present analysis shows that structural behaviour inelastic zone depends on design and ductility provision present in design codes any missing design data will lead towards the misjudging of performance.
- [□] Though the various performance evaluation procedures are unique in their methods but results in conflicting results rising question that, when and where they should be used.
- [□] The procedure results in formation of yield mechanism but fails to quantify actual damage occurred to building
- [□] There is a need of defining a proper damage indicator to estimate actual damage for ductility and structural stability.

III. Abbreviations

- PBSD Performance Based Seismic Design
- PCA Portland Cement Association
- SEAOC Structural Engineers Association of California
- ATC Applied Technological Council
- FEMA Federal Emergency Management Agency
- NRHA Nonlinear Response History Analysis
- NLSP Nonlinear Static Pushover Analysis
- ESDOF Equivalent Single Degree of Freedom
- CSM Capacity Spectrum Method
- DCM Displacement Coefficient Method
- MCSM Modified Capacity Spectrum Method
- MDCM Modified Displacement Coefficient Method

Conflict of interest

I (we) declares that there is no conflict of interest with any financial organization regarding the material discussed in the manuscript

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