

A Comparative Statistical Study of the Geochemistry of Geothermal Fields in Peninsular and Extra-Peninsular India

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Abstract

The present research is aimed at statistically analyzing two data sets drawn from two distinct geologic-tectonic regimes having two distinct geological and tectonic settings - one very tectonically active Alpine-Himalayan mountain chains of Extra-Peninsular and the other very stable landmass or Peninsular shield of India. The main thrust is to arrive at similarity or dissimilarity, if any, in their thermochemistry by applying the robust exploratory factor analysis. The results show that the thermal springs of Extra-Peninsular India are deep-seated hot acidic waters in contrast to shallower relatively less hot, with high pH alkaline waters of peninsular springs. The overall salt assemblage and concentration of F, Cl, SO₄, Na, K, Mg, and Ca suggest the existence of hydrothermal system operating in geotherms of extra-Peninsular regime. In contrast in case of Peninsular springs the water is heated by convective circulation: groundwater percolating downward through fracture, faults reaching great depths of a kilometre or more where the temperature of rocks is high because the normal temperature gradient of the Earth's crust is about 30 °C (54 °F) per kilometre in the first 10 km. The geochemical characteristic as established by the exploratory Factor Analysis distinguishes non-volcanic/magmatic thermal sources as K-Na-HCO₃ as against the magmatic Thermal Sources as Cl-HCO₃-SO₄-Na type of Extra-Peninsular springs, all suggestive of interactions of deep-seated magmatic fluids intermixing with meteoric water at shallow depth.

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I. Introduction

In view of the ever increasing demand as well as the dwindling resources of conventional energy resources like coal, oil, gas, etc., an urgent need was felt all over the world for all forms of alternative renewable energy resources. This enthused a high interest in the exploration and exploitation of geothermal resources, which gained momentum. India was also not far behind in harnessing the geothermal energy.

Table-1. Locations of Geothermal Springs of Peninsular and Extra-Peninsular

Location	Geotherm_Field	Lat_Long	Location	Geotherm_Field	Lat_Long	Location	Geotherm_Field	Lat_Long			
1	Agri kund	Baleshwar	22.8823,87.3666	23	Yumthang	Meghalaya	27.7932, 88.7084	65	Ungiya	Tapoban	30.0527,80.5313
2	Suryakund	Baleshwar	24.0500,85.4100	24	Raleig	Meghalaya	27.5502, 88.2228	66	Devkuna	Tapoban	29.5808,80.0856
3	BaleshwarKaveri	Baleshwar	23.5290,87.2500	25	Berang	NE_Himalaya	27.3457, 88.3277	67	Baliari	Tapoban	30.0853,80.2023
4	BaleshwarB	Baleshwar	23.5200,87.2500	26	Tahvani	Beas_Valley	32.0710,76.4310	68	Dobat	Tapoban	29.5150,80.3384
5	Altri	Mahanadi_Graben	20.1230,85.3045	27	Siac Kund	Beas_Valley	33.3821, 77.0838	69	Panamik	Puga_valley	34.4650,77.3240
6	Tarabala	Mahanadi_Graben	20.1595,85.1810	28	Manikaran	Parbati_Valley	32.0276, 77.3473	70	Puthang	Puga_valley	34.4525,77.3330
7	Athmalik	Mahanadi_Graben	20.4430,84.3010	29	Chuzha	Sutlej_Spiti	32.0345,78.3300	71	Changlung	Puga_valley	34.5640,77.2825
8	Gopalpur	Mahanadi_Graben	19.2647,84.8620	30	Jeevi	Sutlej_Spiti	31.5140,77.4700	72	Gul	Puga_valley	33.1620,75.0345
9	Taptapani	Eastern_Ghat	19.2995,84.2250	31	Napta	Sutlej_Spiti	31.3420,77.5820	73	Yuru	Puga_valley	33.4310,75.4430
10	Tatta	Demodar_Valley	23.4515,84.9012	32	Karunham	Sutlej_Spiti	31.5000,78.1050	74	Tatawin	Puga_valley	33.3030,75.5230
11	Matang	Demodar_Valley	23.4020,84.2040	33	Dikba	Sutlej_Spiti	31.2500,78.2220	75	Gahar	Puga_valley	33.2040,76.5620
12	Sitakund	Demodar_Valley	25.2200,86.3600	34	Jannacti	Tapoban	31.3420,77.5820	76	Ruge	Puga_valley	33.1500,78.1840
13	Lachkund	Demodar_Valley	25.0200,86.2500	35	Banas	Tapoban	30.5720,78.2500	77	Chumathang	Puga_valley	33.2200,78.2100
14	Rajpur	Demodar_Valley	25.0100,85.2800	36	Chaudasani	Tapoban	30.5802,78.3336	78	Sunani	Beas_valley	32.4210,76.0425
15	Tapoban	Demodar_Valley	24.5500,85.1000	37	Jhaya	Tapoban	30.9325,78.4012	79	Gahhad	Beas_valley	32.0785,76.1080
16	Satakund	Demodar_Valley	24.0500,85.4100	38	Tunja	Tapoban	30.5325,78.4330	80	Bajwah	Beas_valley	32.0310,76.4330
17	Tekshing	Subansiri_Valley	28.2000,93.1500	39	Gaurikund	Tapoban	30.3905,79.0135	81	Schivadi	Sohna	28.1500,77.0400
18	Chatu	Subansiri_Valley	28.2500,93.2600	40	Bediwahi	Tapoban	30.4485,79.2530	82	Sohna	Sohna	28.1500,77.0400
19	Naza	Subansiri_Valley	28.2730,93.2500	41	Ghorshila	Tapoban	30.4158,79.3520	83	Didwaka	Toda	26.3530,76.1930
20	Jakien	Meghalaya	25.5796,91.8708	42	Kankar	Tapoban	36.3250,79.3130	84	Redit	Toda	27.0000,76.5300
21	Unjarali	Meghalaya	25.4083,91.5385	43	Juna	Tapoban	30.2600,79.4810	85	Parai	Toda	24.1100,73.4110
22	Lhigden	Meghalaya	27.5332,88.4096	44	Tapoban	Tapoban	30.2930,79.373	86	Persad	Toda	24.1300,73.4240
								87	Gogbaso	Camby	21.4053,72.1544
								88	Gogbatw	Camby	21.4053,72.1544
								89	Dholsa	Camby	22.1500,72.1200
								90			
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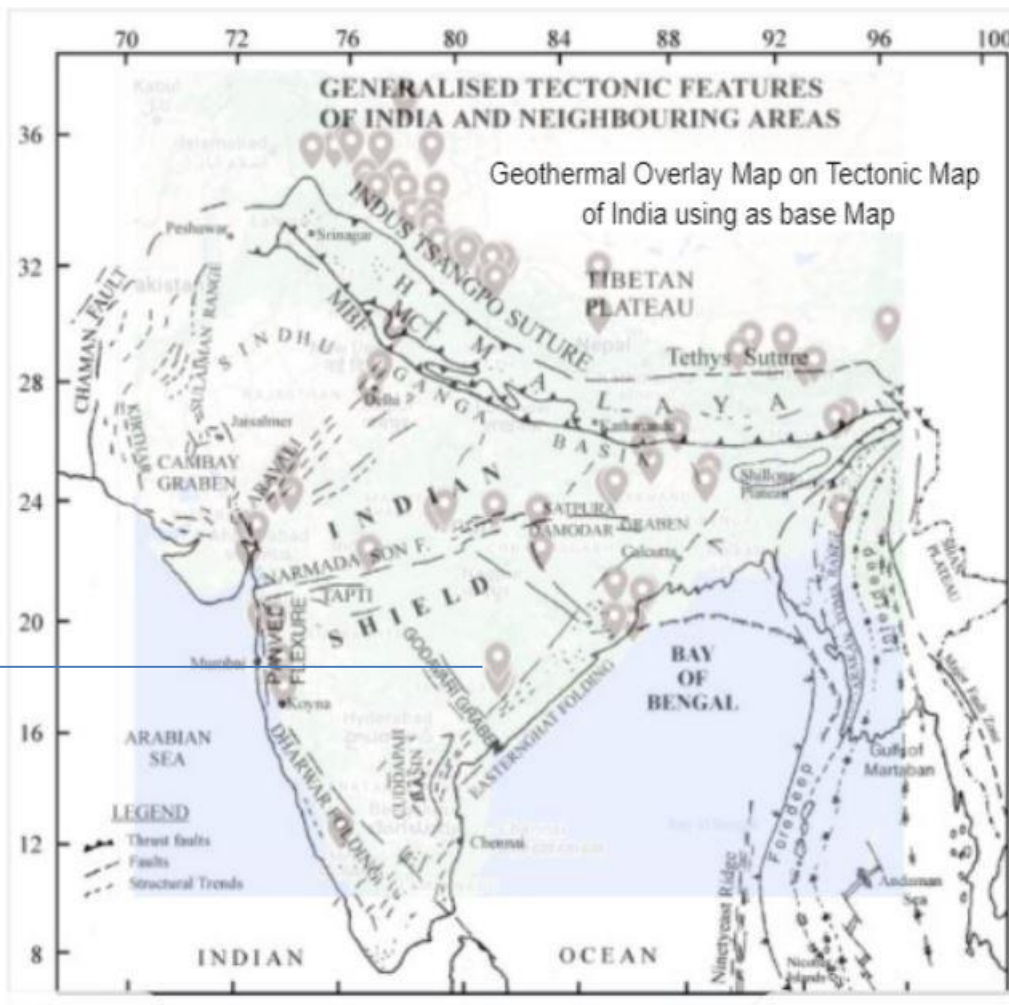


Fig. 1 Association of Geothermal Fields and Tectonic Settings

The surface manifestations of geothermal fields are the volcanoes, fumaroles, geysers, steaming grounds, and hot springs. There are about 340 hot springs spread over different parts of India, covering both the peninsular and extra-peninsular regions. The first attempt to list the hot springs in India was carried out by Schlagintweit in

1852, when he prepared an inventory of 99 thermal springs. Later, the government of India constituted a 'Hot Spring Committee' to examine the possibility of developing geothermal plants for power generation and other uses. In its 1968 report, the committee recommended that a systematic geothermal study and exploration be conducted in India in 1972. The GSI initiated geothermal exploration with the launch of the "Puga Project" in Jammu and Kashmir. In its search for hydrocarbons, , also collected significant geothermal data in sedimentary basins, both offshore' and 'on land, in the Peninsular region. The NGRI formed a 'Geothermic Group' for carrying out studies on 'heat flow values' in some parts of the country. The Central Electricity Authority (CEA) has associated itself with the UNDP geothermal project in India and with India in the Puga and Parvati projects for the utilisation of available geothermal resources for power generation. Mainly due to the ever increasing interest shown by various national agencies in geothermal energy, the growth rate of geothermal data has been constantly accumulated during the last few decades. The Geological Survey of India has brought out a special publication titled "Geothermal Atlas of India' (Ravi Shanker,1991) based on the data compiled from all sources of information, both published and unpublished, on geothermal activities in India. However, the lack of uniformity in data acquisition practices and data recording formats followed by different agencies and the manual handling of such huge quantities of data make the whole system of data storage, search, retrieval, and analysis laborious, cumbersome, and less efficient. This obviously necessitated computerized system that offers both speed and storage capabilities. The GSI being the repository of most of the information concerning geological and other related data in the country, included in its field season 1993-94 program an R&D item No. 7/WB-5 (A. Roy, 1994). (CEA) associated themselves with the UNDP geothermal project in India and with India in the in the valley Puga and Parvati projects for utilisation of available geothermal resources for power generation. Mainly due to this ever increasing interest shown by various National agencies in geothermal energy, the growth rate of geothermal data has been constantly accumulated during the last few decades. The Geological Survey of India has brought out a special Publication titled 'Geothermal Atlas of India' (1991) based on the data compiled from all sources of information both published and unpublished on geothermal activities in India. However, the lack of uniformity in data acquisition practices and data recording formats followed by different Agencies and also manual handling of such huge quantities of data make the whole system of data storage, searching retrieval and their analysis laborious, cumbersome and less efficient. This obviously necessitated computerized system that offer both speed and storage capabilities. The GSI being the repository of most of the information concerning geological and other related data in the country, included in its field season 1993-94 program an R&D item No. 7/WB-5 (A.Roy,1994).

The geological regions of India broadly follow three physical features, and may be grouped into three regions: the Extra Peninsular Himalayas and their associated group of mountains in the north, the Indo-Gangetic Plain in the middle; and the Peninsular Shield in the south. The peninsula is in the shape of a vast inverted triangle, bordered on the east by the Bay of Bengal and on the north by the Vindhya and Satpura ranges. The peninsular India comprises the Indian Shield, which is a geologically very old and stable part of the crust. exposed for long ages to denudation and approaching peneplanation. The Peninsula is mainly composed of Precambrian rocks and has Proterozoic and Phanerozoic cover. Along its coasts, there have been marine transgressions that have laid down sedimentary beds of the upper Gondwana, Cretaceous, and Tertiary ages. Major tectonic features/lineaments of Peninsular India include the West Coast areas of Maharashtra; the Son-Narmada-Tapi lineament zone at Salbardi, Satpura-Tapi areas in Maharashtra; Tattapani in Chhattisgarh, Rajgir-Monghyar in Bihar, Tatta and Jarom in Jharkhand, and the Eastern Ghat tracts of Orissa. 3. Rift and grabens of Gondwana basins of the Damodar, Godavari, and Mahanadi valleys The Extra-Peninsular India constitutes a part of the Alpine-Himalayan Tertiary Mountain Belt and is very active tectonically, falling within a severe seismic zone and being prone to earthquakes. The Extra-Peninsula is a region of folded and overthrust mountain chains, of geologically recent origin. The Extra-Peninsula is mainly composed of rocks from the Tertiary age.

Cause

A hot spring, hydrothermal spring, or geothermal spring is a spring produced by the emergence of geothermally heated groundwater onto the surface of the Earth. The groundwater is heated either by shallow bodies of magma or by circulation through faults to hot rock deep in the earth's crust by geothermal heat—heat from the earth's interior. In volcanic areas, water may come into contact with very hot rock heated by magma.

Geothermal fields are greatly correlated with the tectonic settings of a region. Their intimate association fits very well with the tectonic belts of India. The remarkable correlation between them has been observed when the two are superimposed upon each other. In the present study, all the geothermal springs were plotted onto the Google map by their GPS coordinates. Then this geothermal overlay map was superimposed onto the tectonic map of India, the latter serving as the base map.

Chemistry

Hot springs have an especially high mineral content, because heated water can hold more dissolved solids. This means a given hot spring can contain everything from calcium, magnesium, silica, lithium, and even radium. This means a given hot spring can contain everything from calcium, magnesium, silica, lithium, and even radium. The chemistry of hot springs ranges from acid sulfate springs with a pH as low as 0.8 to alkaline chloride springs saturated with silica and bicarbonate springs saturated with carbon dioxide and carbonate minerals. Some springs also contain abundant dissolved iron. Sulfur is an element that is frequently found in hot springs; it is dissolved in the springs through the surrounding rocks and soil. The most important microbial process that occurs in hot springs is the oxidation of sulfur, producing sulfuric acid. Hot springs stay clean either through a process of regularly replacing the water or by mixing in a chemical like chlorine, which kills bacteria and other pathogens by breaking down their chemical bonds.

Literature Review

Anirbid Sircar et.al. (2015) in their paper “Geothermal exploration in Gujarat: case study from Dholera”, mainly from the point of view of exploration of geothermal energy for power generation, tried to unearth subsurface picture using geoscientific data, for example, Gravity survey, Landsat imagery, magnetotelluric (MT) survey, and water chemistry. According to them Hot springs exist over gravity high, which is the surface manifestation of deep and shallow water sources.

D Rouwet (2017), in his paper “Fluid Geochemistry and Volcanic Unrest: Dissolving the Haze ...” also subscribes the origin of hot springs to degassing of magma.

F. Tassi et al (2010) in his paper titled “Fluid geochemistry of hydrothermal systems... (northern Chile)” based on chemical and isotopic composition, came out with four chemical facies of thermal discharges varying from Na-Cl - SO₄ rich waters to Na-Ca-Cl-SO₄, Ca-SO₄-HCO₃ and Ca-SO₄, all suggestive of interactions of deep-seated magmatic fluids intermixing with meteoric water at shallow depth.

H. Baioumy (2015) in his paper titled “Geochemistry and geothermometry of non-volcanic hot ...” subscribes to the view of degassing of magma.

Mohammad Noor et.al. (2021) in their paper “A geochemical comparison between volcanic and non-volcanic hot springs from East Malaysia: Implications for their origin and geothermometry” infer that **the** geochemical characteristic distinguishes non-volcanic thermal sources as K-Na-HCO, while volcanic thermal sources present the Cl-HCO₃-SO₄-Na type.

At the backdrop of the cited literature in relevance to my research topic, I may say while the goal may be the same, the gaps in knowledge and unresolved problems that is lacking in their studies has been addressed in my research by adopting a definitive approach of statistical/mathematical model study giving an insight into arriving at distinguishing two suites of distinct geotherms. The technique made comparison simpler and easier to follow between the fluid geochemistry inherent in the two distinctive geologic-tectonic environs - one very tectonically active Alpine-Himalayan Extra-Peninsular, and the other very stable landmass or Peninsular shield of India. There observed spectacular correlation between geothermal fields with tectonic zones with two very contrasting tectonic history with differing degree of severity - recent Himalayan thrust zones in Extra-Peninsula in the north as against the late Precambrian Proterozoic mobile belts in the Central Highland of Peninsular India..

Statistical Analysis of Multi-variate Geothermal Geochemistry

An attempt has been made in the present research to statistically analyze two data sets drawn from Peninsular and Extra-Peninsular regimes having two distinct geological and tectonic settings with a view to arriving at similarity or dissimilarity, if any, in their thermo-chemistry. Besides the basic descriptive statistical study, the main thrust is given here to the statistical analysis of two data sets, ideally representing two distinct geologic-tectonic environs, by applying the robust exploratory factor analysis. DATATAB statistics-calculator/factor-analysis software was employed for the present research study.

Data Set - 1 : Extra-Peninsular Geothermal Data.

NUM	TEMPC	pH	SPCMHO/cm	HCO3 mg/L	Cl mg/L	SO4 mg/L	TotHard	Ca mg/L	Mg mg/L	Na mg/L	K mg/L	F mg/L	B mg/L	SiO2 mg/L	TDS mg/L
1	59	8.1	1271	300	163	62	0	14	5	210	13	12	5	80	800
2	96	7.7	827	170	133	36	131	44	15	88	19	0.8	33	60	514
3	59	7.1	5260	490	855	1244	1214	342	87	600	109	3.6	138	30	4072
4	24	8.2	795	210	102	83	136	30	15	110	19	1.2	25	25	488
5	56	7.6	1280	342	232	26	72	26	1	260	16	10	10	107	870
6	44	7.6	2015	303	200	340	302	103	11	260	45	6	13	87	1280
7	50	8.3	525	173	45	28	40	13	2	103	5	10	3	23	363
8	90	7.9	1045	276	170	33	0	52	12	135	27	3	10	83	874
9	73	7.5	410	145	30	55	0	38	13	30	7	1	3	50	378
10	52	7.8	25	15	2	0	12	3	1	1	0	0.2	0	2	20
11	50	8.2	700	248	72	48	40	13	2	140	6	5	3	65	480
12	55	7.7	400	272	10	14	0	56	24	8	5	0.4	0	68	366
13	54	7.6	845	445	35	0	0	50	52	50	10	1.2	0	41	536
14	55	6.8	2630	112	1485	22	230	70	13	490	37	1.6	19	115	1630
15	25	7.7	139	103	8	29	0	45	44	24	10	0.7	2	30	442
16	81	8.1	315	117	15	30	0	34	3	30	5	1.6	0	22	245
17	62	8	1460	861	48	14	72	14	99	290	43	3	5	91	1015
18	59	7.8	465	278	12	27	214	42	26	15	8	0.5	1	69	360
19	32	6.7	95	38	5	0	0	6	7	2	1	0.4	0	11	42
20	32	8.3	2000	953	86	0	0	0	47	80	83	0	0	18	0
21	68	6.4	1239	734	12	5	200	64	10	180	38	2	1	130	860
22	56	6.9	770	439	41	21	215	40	23	163	15	4	2	34	510
23	76	7.7	720	254	13	99	32	13	0	135	6	12.5	2.8	101	570
24	28	7.1	770	363	17	66	132	40	8	120	7	10	2	53	575
25	66	7.7	2030	1610	85	57	34	10	2	580	48	10	8	130	840
26	40	7.2	3641	259	11	1484	1352	504	22	200	6	2.5	1	35	2557
27	12	7	1060	233	58	383	536	169	28	10	2	0.2	0	18	834
28	12	7.1	63	32	3	0	24	9	0	2	0	0.4	0	6	42
29	68	6.9	386	112	30	72	40	14	1	56	4	6	1	35	235
30	9	8	178	0	6	12	52	15	3	9	3	1	0.9	9	114
31	18	8.3	205	0	7	2	88	27	5	6	2	0.2	0.9	9	123
32	34	7.4	2668	415	596	16	190	41	21	370	30	3	8	20	1399
33	40	7.6	469	264	13	10	186	44	18	19	10	0.3	0	28	279
34	35	6.6	446	49	104	6	20	7	1	75	3	7	1	28	260
35	52	7.2	8160	435	10	28	113	27	11	133	10	2.1	0	80	565
36	38	7.4	16630	362	154	370	396	127	19	150	17	1	0	60	1017
37	38	7.7	9800	353	35	36	158	54	5	86	9	0	0	40	638

Data Set- 2 : Peninsular Geothermal Data

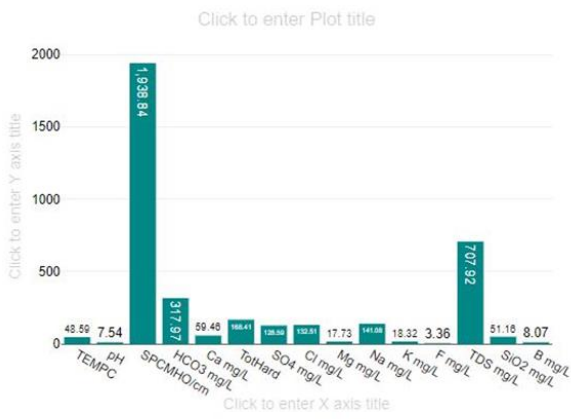
NUM	Temp_C	pH	SPCMHO	HCO3 mg/L	Cl mg/L	SO4 mg/L	TotHard	Ca mg/L	Mg mg/L	Na mg/L	K mg/L	F mg/L	Bmg/L	SiO2 mg/L	TDS mg/L
1	32	7.5	5090	154	1375	210	872	204	88	660	18	0.7	0	18	2981
2	44	7.3	1115	339	165	24	270	82	16	110	6	0.4	0.9	46	500
3	40	7.7	1010	315	130	33	0	110	12	70	25	0	0	58	630
4	0	7.3	1410	390	195	75	0	65	40	210	5	0	0.1	40	830
5	26	7.8	1050	500	140	5	340	70	40	130	2	1	1.2	30	650
6	35.5	7.1	550	290	50	5	230	60	20	30	1	0.3	1.2	30	320
7	40	7.1	28980	190	1347	5	0	390	250	6810	55	0	0	16	0
8	0	7.2	960	410	110	25	0	45	15	95	2	0	0	4.5	0
9	43.5	7.4	8350	150	2725	10	0	105	40	1900	30	0.2	3	31	4790
10	99	0	0	1534	2428	672	0	9	8	1167	145	0	0	0	5744
11	40	7.4	4190	195	1485	0	0	90	40	875	14	0	0	25	0
12	39	7.6	550	183	71	33	160	40	21	40	2	0	0	22	328
13	54	7.5	13620	13	4800	185	4680	186	10	955	13	0	0.4	87	1614
14	43	9	2950	11	850	130	432	170	0.1	368	7	2	0.4	50	1868
15	64	8.6	4950	14	1210	144	890	348	0.2	391	8.5	7.2	0	65	2704
16	35	8.3	883	18	78	242	109	40	15	155	2	2.5	0	60	563
17	35	8	1917	71	426	107	100	32	6	292	4	1.5	1	5	965
18	61	7.6	1457	30	375	100	147	56	1.8	231	7.8	4	0.4	122	955
19	0	8	0	63	265	108	210	80	44	148	6	0.1	0	60	188
20	91	0	0	177	67	70	0	3	1	133	0	3	0.5	96	511
21	0	7.5	0	364	30	8	100	35	3	110	16	0.3	0	57	0
22	0	7.4	0	99	457	128	100	42	2	360	19	0.5	0	70	0
23	0	8	0	366	257	55	530	96	70	98	15	0.2	0	45	855
24	33	7.8	765	171	50	120.6	0	50	7.9	95	7.4	4	0	35	484.5
25	29	7.6	1077	128.6	166	182	0	20	13.4	208	4	5	0	28	756

Descriptive Basic Statistics (Upper:Extra-Peninsula,Lower:Peninsula)

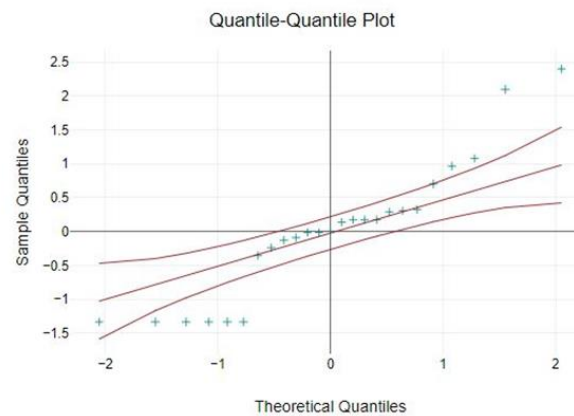
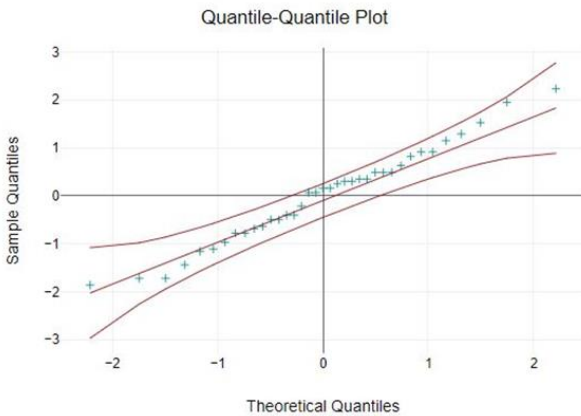
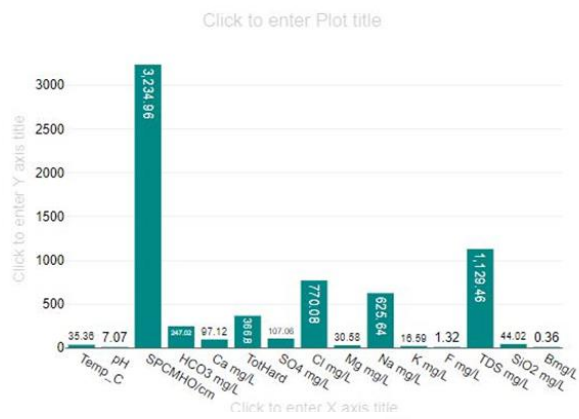
	TEMPC	pH	SPCMHO/cm	HCO3 mg/L	Ca mg/L	TotHard	SO4 mg/L	Cl mg/L	Mg mg/L	Na mg/L	K mg/L	F mg/L	TDS mg/L	SiO2 mg/L	B mg/L
Mean	48.59	7.54	1,938.84	317.97	59.46	168.41	128.59	132.51	17.73	141.08	18.32	3.36	707.92	51.16	8.07
Std. Deviation	21.26	0.51	3,258.28	309.16	96.54	296.42	315.61	283.27	22.52	155.34	23.27	3.77	761.64	36.04	23.16
Minimum	9	6.4	25	0	0	0	0	2	0	1	0	0	0	2	0
Maximum	96	8.3	16,630	1,610	504	1,352	1,484	1,485	99	600	109	12.5	4,072	130	138

	Temp_C	pH	SPCMHO/cm	HCO3 mg/L	Ca mg/L	TotHard	SO4 mg/L	Cl mg/L	Mg mg/L	Na mg/L	K mg/L	F mg/L	TDS mg/L	SiO2 mg/L	Bmg/L
Mean	35.36	7.07	3,234.96	247.02	97.12	366.8	107.06	770.08	30.58	625.64	16.59	1.32	1,129.46	44.02	0.36
Std. Deviation	26.53	2.17	6,209.25	303.73	96.64	933.93	137.52	1,126.61	50.93	1,361.05	29.3	1.93	1,476.2	29.52	0.68
Minimum	0	0	0	11	3	0	0	30	0.1	30	0	0	0	0	0
Maximum	99	9	28,980	1,534	390	4,680	672	4,800	250	6,810	145	7.2	5,744	122	3

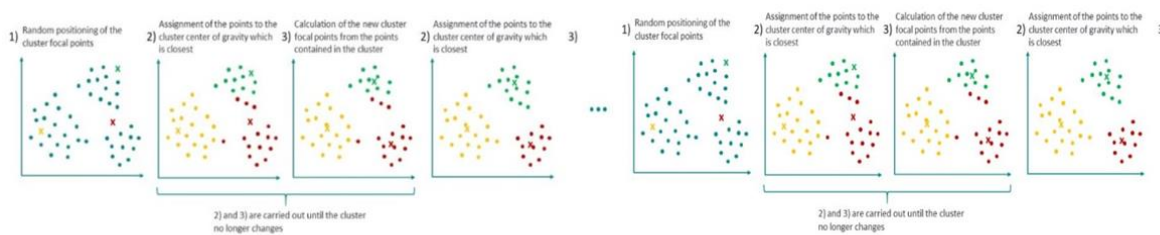
Extra-Peninsula Bar Chart



Peninsula Bar Chart



K-Mean Cluster

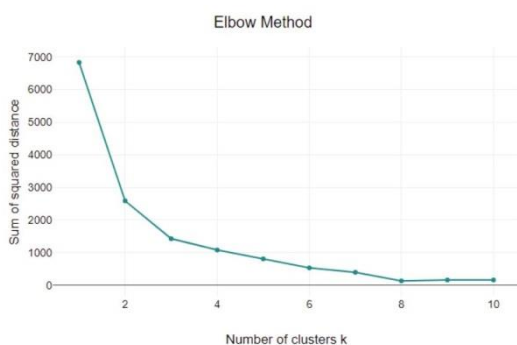


Interpreting the Results

Quantile-Quantile Plot : Purpose: Check If Two Data Sets Can Be Fit With the Same Distribution. The data sets are compared to the normal distribution, which forms the base distribution. Their quantiles are plotted along the X-axis as the theoretical quantile-quantile, while the sample quantiles are plotted along the Y-axis as sample quantiles. Now in the case of Data Set-1 (Extra-Peninsula), the points fall on the 45 degree reference line, which signifies that the data population is normally distributed. In the case of Data Set-2 (Peninsula), the data is distributed normally in the middle portion, but some points deviate on either end of the reference line, signifying heterogeneity of the data due to a number of causes, like the heterogeneous character of the Peninsula both in lithological and tectonic settings. Moreover, some of the springs located in the Gangetic region may also contribute to this skewed pattern. Contrarily, the extra-Peninsular Himalayan region is a homogenous entity both in rock types and its arcuate tectonic settings, which are beautifully exhibited in the Q-Q plots.

K-Means Clustering

Scaling data for k-means clustering : Since the variables under consideration do not have the same unit, the data has been first scaled before cluster analysis. The k-

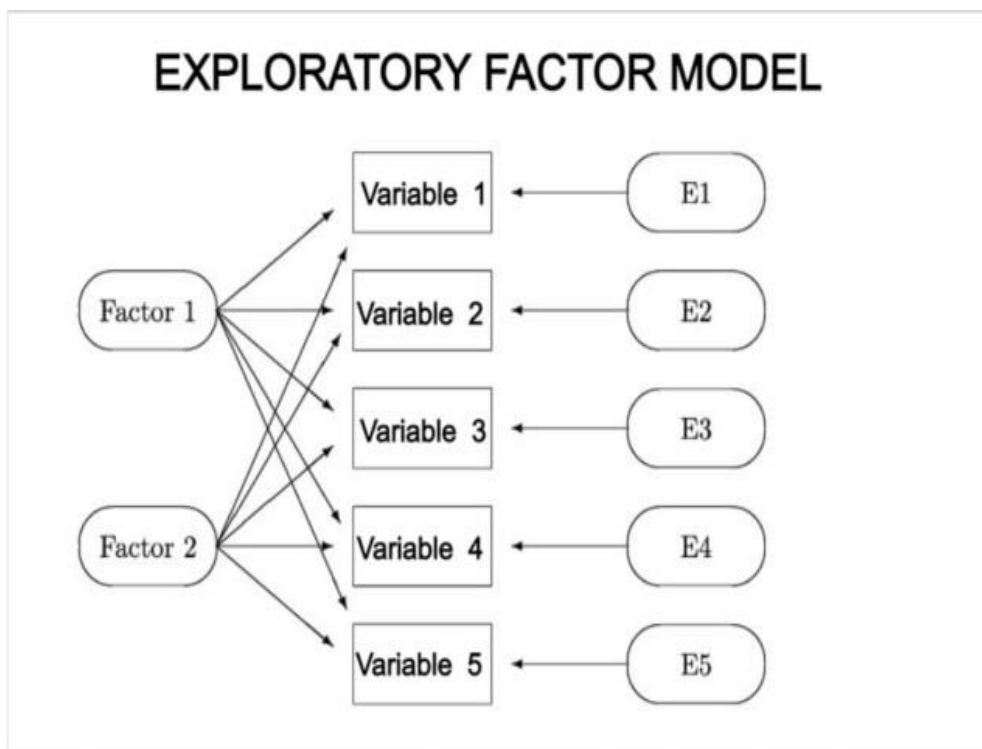


Means method, developed by MacQueen (1967), is one of the most widely used non-hierarchical methods. K-means clustering is a method of vector quantization, originally from signal processing, that aims to partition n observations into k clusters in which each observation belongs to the cluster with the nearest mean, serving as a prototype of the cluster. First, an initial partition with k clusters (given number of clusters) is created. Then, starting with the first object in the first cluster, Euclidean distances of all objects to all cluster foci are calculated. These steps are repeated

until each object is located in a cluster with the smallest distance to its centroid (center of the cluster). When you want to calculate a cluster analysis, often the big question is how many clusters should I take. The optimal cluster number is determined by elbow Curve method. In the present study three clusters are taken based on Elbow curve.

Exploratory Factor Analysis

The exploratory factor analysis is a procedure that aims to uncover structures in large sets of variables. If you have a data set with many variables, it is possible to separate significant few, that is some of them correlatable with each other from insignificant many. The prime aim therefore is to reduce a large number of correlating variables to a few independent latent variables, the so-called factors. In other words the aim of the latent variables is to clarify as much of the variance of the original variables as possible.



Basic Concept of Factor Analysis and its significance in interpretation

$$X_j = \sum_{r=1}^p C_{jr} f_r$$

where $f_r(r=1,2,3,\dots,p)$ represents common underlying factors and C_{jr} indicates the factor loadings of variable X_j on factor f_r . Theoretical unknown factors can then be expressed in terms of distinct groups of variables (in the present case fluid geochemical elements, which when correlated with the observed features of geothermal geochemistry of the area of investigation, provide significant insight into the causal factors (Roy. A., 1984).

To carry out this dimensional reduction of data, the following computational steps are necessary:

- Correlation Coefficient Matrix, the basis for factor analysis
 - Unrotated Principal component Analysis
 - Factor loading showing Variance explained by the variable on that particular factor matrix, Eigenvalues, Communality
 - Determination of number of factors to retain
 - Rotated (Varimax) Factor Analysis - Rotation method makes it more reliable to understand the output.
- There are a number of rotation methods available of which Varimax rotation method is used in the present study. Eigenvalues do not affect the rotation method, but the rotation method affects the Eigenvalues or percentage of variance extracted.

Correlation matrix - Extra-Peninsula

	TEMPC	pH	SPCMHO/cm	HCO3 mg/L	Cl mg/L	SO4 mg/L	TotHard	Ca mg/L	Mg mg/L	Na mg/L	K mg/L	F mg/L	B mg/L	SiO2 mg/L	TDS mg/L
TEMPC	1	0.05	-0.06	0.22	0.09	-0.05	-0.1	-0.06	0.03	0.25	0.17	0.26	0.18	0.55	0.14
pH	0.05	1	-0.11	0.05	-0.25	-0.2	-0.3	-0.26	0.04	-0.16	-0	0.04	-0.1	-0.12	-0.25
SPCMHO/cm	-0.06	-0.11	1	0.19	0.17	0.31	0.34	0.3	0.11	0.25	0.19	-0.13	0.13	0.13	0.34
HCO3 mg/L	0.22	0.05	0.19	1	0	0.03	0.05	0.01	0.35	0.57	0.6	0.23	0.09	0.51	0.21
Cl mg/L	0.09	-0.25	0.17	0	1	0.22	0.31	0.23	0.21	0.7	0.51	0.01	0.54	0.24	0.6
SO4 mg/L	-0.05	-0.2	0.31	0.03	0.22	1	0.96	0.97	0.34	0.37	0.35	-0	0.55	-0.09	0.83
TotHard	-0.1	-0.3	0.34	0.05	0.31	0.96	1	0.97	0.37	0.41	0.37	-0.1	0.56	-0.08	0.85
Ca mg/L	-0.06	-0.26	0.3	0.01	0.23	0.97	0.97	1	0.34	0.32	0.28	-0.12	0.46	-0.07	0.81
Mg mg/L	0.03	0.04	0.11	0.35	0.21	0.34	0.37	0.34	1	0.3	0.6	-0.26	0.48	-0.02	0.49
Na mg/L	0.25	-0.16	0.25	0.57	0.7	0.37	0.41	0.32	0.3	1	0.71	0.38	0.58	0.53	0.75
K mg/L	0.17	-0	0.19	0.6	0.51	0.35	0.37	0.28	0.6	0.71	1	0.03	0.7	0.25	0.62
F mg/L	0.26	0.04	-0.13	0.23	0.01	-0	-0.1	-0.12	-0.26	0.38	0.03	1	0.03	0.44	0.11
B mg/L	0.18	-0.1	0.13	0.09	0.54	0.55	0.56	0.46	0.48	0.58	0.7	0.03	1	-0	0.76
SiO2 mg/L	0.55	-0.12	0.13	0.51	0.24	-0.09	-0.08	-0.07	-0.02	0.53	0.25	0.44	-0	1	0.21
TDS mg/L	0.14	-0.25	0.34	0.21	0.6	0.83	0.85	0.81	0.49	0.75	0.62	0.11	0.76	0.21	1

Correlation matrix - Peninsula

	Temp_C	pH	SPCMHO/cm	HCO3 mg/L	Cl mg/L	SO4 mg/L	TotHard	Ca mg/L	Mg mg/L	Na mg/L	K mg/L	F mg/L	Bmg/L	SiO2 mg/L	TDS mg/L
Temp_C	1	-0.63	0.15	0.26	0.39	0.48	0.14	0.11	-0.13	0.15	0.45	0.33	0.15	0.17	0.53
pH	-0.63	1	0.1	-0.64	-0.14	-0.52	0.12	0.31	0.08	-0.07	-0.59	0.08	0.02	0	-0.36
SPCMHO/cm	0.15	0.1	1	-0.19	0.53	-0.13	0.33	0.78	0.8	0.93	0.22	-0.13	0.08	-0.1	0.06
HCO3 mg/L	0.26	-0.64	-0.19	1	0.1	0.59	-0.21	-0.28	-0.02	0.03	0.8	-0.34	-0.07	-0.44	0.46
Cl mg/L	0.39	-0.14	0.53	0.1	1	0.36	0.73	0.39	0.12	0.36	0.43	-0.18	0.24	0.02	0.59
SO4 mg/L	0.48	-0.52	-0.13	0.59	0.36	1	0.12	-0.12	-0.19	-0.04	0.73	0.13	-0.26	-0.13	0.65
TotHard	0.14	0.12	0.33	-0.21	0.73	0.12	1	0.32	-0.07	0	-0.07	-0.06	-0.01	0.31	0.13
Ca mg/L	0.11	0.31	0.78	-0.28	0.39	-0.12	0.32	1	0.62	0.65	0.08	0.15	-0.09	-0.01	0.14
Mg mg/L	-0.13	0.08	0.8	-0.02	0.12	-0.19	-0.07	0.62	1	0.87	0.22	-0.3	-0.07	-0.32	-0.09
Na mg/L	0.15	-0.07	0.93	0.03	0.36	-0.04	0	0.65	0.87	1	0.42	-0.19	0.06	-0.24	0.1
K mg/L	0.45	-0.59	0.22	0.8	0.43	0.73	-0.07	0.08	0.22	0.42	1	-0.25	-0.08	-0.33	0.65
F mg/L	0.33	0.08	-0.13	-0.34	-0.18	0.13	-0.06	0.15	-0.3	-0.19	-0.25	1	-0.13	0.35	0.06
Bmg/L	0.15	0.02	0.08	-0.07	0.24	-0.26	-0.01	-0.09	-0.07	0.06	-0.08	-0.13	1	-0.07	0.36
SiO2 mg/L	0.17	0	-0.1	-0.44	0.02	-0.13	0.31	-0.01	-0.32	-0.24	-0.33	0.35	-0.07	1	-0.2
TDS mg/L	0.53	-0.36	0.06	0.46	0.59	0.65	0.13	0.14	-0.09	0.1	0.65	0.06	0.36	-0.2	1

Extra-Peninsula

Peninsula

Explained Total Variance

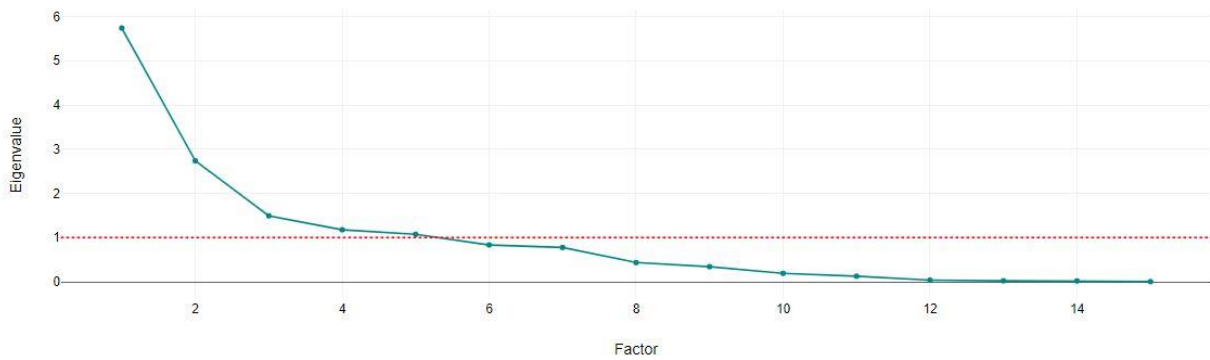
Communality

Explained Total Variance

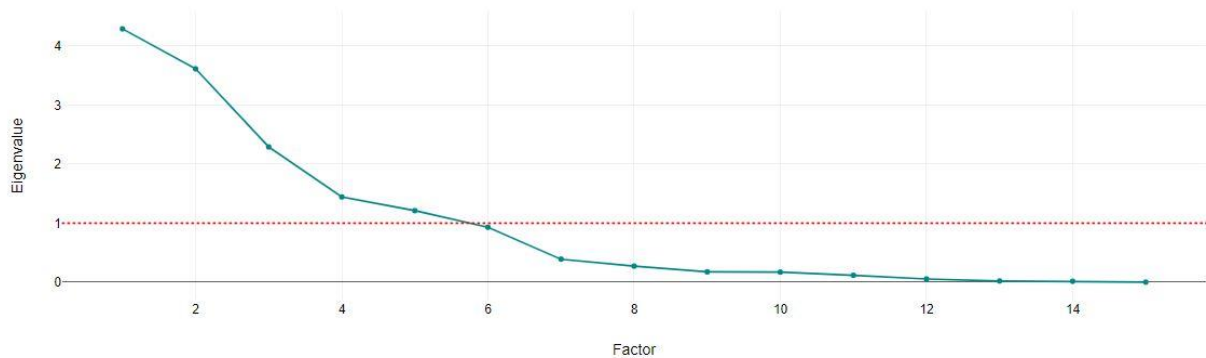
Communality

Component	Total	% of variance	Accumulated %	Extraction	Component	Total	% of variance	Accumulated %	Extraction		
1	5.74	38.26	38.26	TEMPC	0.39	1	4.29	28.6	28.6	Temp_C	0.7
2	2.74	18.24	56.5	pH	0.38	2	3.61	24.09	52.7	pH	0.64
3	1.49	9.94	66.45	SPCMHO/cm	0.31	3	2.29	15.27	67.97	SPCMHO/cm	0.96
4	1.18	7.84	74.29	HCO3 mg/L	0.83	4	1.44	9.63	77.6	HCO3 mg/L	0.87
5	1.07	7.15	81.44	Cl mg/L	0.82	5	1.21	8.08	85.68	Cl mg/L	0.92
6	0.83	5.55	86.99	SO4 mg/L	0.94	6	0.93	6.2	91.88	SO4 mg/L	0.78
7	0.78	5.17	92.16	TotHard	0.97	7	0.39	2.61	94.49	TotHard	0.67
8	0.43	2.9	95.06	Ca mg/L	0.94	8	0.27	1.82	96.3	Ca mg/L	0.81
9	0.34	2.28	97.34	Mg mg/L	0.74	9	0.17	1.16	97.47	Mg mg/L	0.92
10	0.19	1.27	98.61	Na mg/L	0.88	10	0.17	1.14	98.61	Na mg/L	0.92
11	0.13	0.84	99.45	K mg/L	0.88	11	0.12	0.78	99.38	K mg/L	0.92
12	0.04	0.25	99.7	F mg/L	0.56	12	0.05	0.36	99.75	F mg/L	0.7
13	0.02	0.15	99.85	B mg/L	0.77	13	0.02	0.14	99.89	Bmg/L	0.49
14	0.02	0.13	99.98	SiO2 mg/L	0.79	14	0.02	0.1	99.99	SiO2 mg/L	0.6
15	0	0.02	100	TDS mg/L	0.97	15	0	0.01	100	TDS mg/L	0.74

Extra-Peninsula



Peninsula



Unrotated Component Matrix

	Extra-Peninsula				Peninsula				
	Component				Component				
	1	2	3	4	1	2	3	4	
TEMPC	-0.14	0.58	0.16	0.02	Temp_C	0.59	-0.29	0.45	-0.26
pH	0.26	0.14	-0.49	0.23	pH	-0.54	0.55	0.07	0.2
SPCMHO/cm	-0.38	-0.09	0.08	0.38	SPCMHO/cm	0.52	0.83*	0.04	-0.07
HCO3 mg/L	-0.35	0.62*	-0.28	0.49	HCO3 mg/L	0.6*	-0.56	-0.44	0.04
Cl mg/L	-0.6*	0.19	0.05	-0.65*	Cl mg/L	0.69*	0.21	0.49	0.38
SO4 mg/L	-0.8*	-0.45	0.19	0.23	SO4 mg/L	0.64*	-0.55	0.14	-0.21
TotHard	-0.83*	-0.46	0.18	0.16	TotHard	0.21	0.26	0.68*	0.31
Ca mg/L	-0.77*	-0.49	0.22	0.23	Ca mg/L	0.35	0.77*	0.21	-0.24
Mg mg/L	-0.56	-0.04	-0.65*	0.08	Mg mg/L	0.38	0.75*	-0.43	-0.17
Na mg/L	-0.78*	0.51	0.07	-0.12	Na mg/L	0.6*	0.69*	-0.24	-0.17
K mg/L	-0.74*	0.34	-0.45	-0.07	K mg/L	0.89*	-0.27	-0.24	-0.09
F mg/L	-0.06	0.56	0.48	0.08	F mg/L	-0.2	-0.11	0.53	-0.6*
B mg/L	-0.78*	-0.01	-0.19	-0.35	Bmg/L	0.09	0.04	0.13	0.68*
SiO2 mg/L	-0.24	0.78*	0.32	0.17	SiO2 mg/L	-0.31	-0.01	0.67*	-0.22
TDS mg/L	-0.97*	-0.06	0.11	-0.05	TDS mg/L	0.73*	-0.32	0.25	0.22

Rotated Component Matrix (Varimax)

	Extra-Peninsula				Peninsula				
	Component				Component				
	1	2	3	4	1	2	3	4	
TEMPC	0.15	0.57	-0.07	-0.18	Temp_C	0.61	0.09	0.36	-0.43
pH	0.33	-0.11	-0.42	0.29	pH	-0.78*	0.15	0.01	0.08
SPCMHO/cm	-0.46	0.2	-0.16	0.17	SPCMHO/cm	-0.02	0.97*	0.12	0.03
HCO3 mg/L	0.01	0.61*	-0.67*	0.12	HCO3 mg/L	0.84*	-0.16	-0.14	0.34
Cl mg/L	-0.19	0.11	-0.05	-0.87*	Cl mg/L	0.3	0.45	0.79*	0.07
SO4 mg/L	-0.96*	0.03	-0.09	-0.08	SO4 mg/L	0.83*	-0.11	0.16	-0.21
TotHard	-0.97*	0	-0.09	-0.15	TotHard	-0.14	0.25	0.75*	-0.15
Ca mg/L	-0.97*	0	-0.04	-0.05	Ca mg/L	-0.12	0.86*	0.11	-0.24
Mg mg/L	-0.29	-0.16	-0.77*	-0.19	Mg mg/L	0	0.87*	-0.34	0.22
Na mg/L	-0.3	0.59	-0.33	-0.58	Na mg/L	0.18	0.93*	-0.13	0.12
K mg/L	-0.24	0.22	-0.73*	-0.48	K mg/L	0.91*	0.25	0.01	0.16
F mg/L	0.1	0.7*	0.22	-0.08	F mg/L	-0.06	-0.12	0	-0.83*
B mg/L	-0.45	-0.01	-0.36	-0.66*	Bmg/L	-0.1	-0.04	0.52	0.46
SiO2 mg/L	0.11	0.87*	-0.07	-0.14	SiO2 mg/L	-0.3	-0.16	0.3	-0.63*
TDS mg/L	-0.78*	0.24	-0.24	-0.48	TDS mg/L	0.68*	0.06	0.52	0.08

Interpreting the Results

Of the above computational steps, the most baffling issue is to determine the number of variables into a fewer number of factors i.e. to separate significant few from insignificant many. There are different criteria suggested by different researchers namely,

- Factors which have high eigenvalues
- The Eigenvalue > 1
- From the inflection point of scree or Elbow curve plot i.e. a graph of the eigenvalues (Y-axis) against the factors (X-axis) listed in the descending order.
- Communalities for each of the variables (somewhat like R² from Regression analysis) at least 0.5

- The factor loadings for each variable should be ≥ 0.6 (Awang, 2014).

Factor analysis is a way to condense the data in many variables into a just a few variables. For this reason, it is also sometimes called “dimension reduction”. In the present study trial runs of PCA analysis taking into consideration of all the above criteria for determination of number of factors, came to a comprised conclusion that in the present study four factors which accounts for $75 \pm 2\%$ of the total variance of the original variables “load” on a factor of Principal component is retained for rotation to avoid both overextraction and underextraction of factors that may have deleterious effects on the results. This also corroborates the criteria for communalities for each of the variable closer to one (0.9) and eigenvalue > 1

EXTRA-PENINSULA		PENINSULA	
Unrotated PCA	Rotated VARIMAX	Unrotated PCA	Rotated VARIMAX
F1 Cl-,SO4-,Ca-, Na-, K-,B-TDS-	F1 SO4, Ca, TDS	F1 HCO3, Cl, SO4, Na, K, TDS	F1 pH-, HCO3, SO4, K, TDS
F2 HCO3, SiO2	F2 HCO3, F, SiO2	F2 SPCMHO*,Ca, Mg, Na	F2 SPCMHO*,Ca,Mg, Na
F3 Mg-	F3 HCO3-, Mg-, K-	F3 SiO2	F3 Cl
F4 Cl -	F4 Cl-, F-	F4 B, F-	F4 F-, SiO2-

SPCMHO/Cm* - is correctly defined as the electrical conductance of 1 cubic centimeter of a solution at 25 °C used to estimate the salinity , ionic strength and concentrations of major TDS solutes in natural waters.

From the above Factor analysis Table, following points of Fluid geochemistry emerge:

- 1.The thermal springs of Extra-Peninsular region are hot acidic in contrast to relatively cold high pH alkalinity of Peninsular springs.
- 2.The overall salt assemblage and concentration of F, Cl, SO4, Na, K, Mg, and Ca suggest the existence of hydrothermal system operating in geotherms of Extra-Pensulaa. In contrast, Peninsular springs are K-Na-bI-carbonate rich waters with low SO₄⁻ content and relatively higher contents of HCO₃⁻ compared to other anions SO₄, Cl and F (Mohammad Noor, 2021).
3. Extra Peninsular sprngs are magmatic-hydrothermal manifestations, a phenomenon of magma progressively degassing in their decreasing order of solubility CO₂ < SO₂ < HCl < HF i.e. “CO₂-first till HF-last” (Giggenbach 1987).
- 4.In case of the non-volcanic/magmatic thermal springs of Peninsular India, the water is heated by convective circulation: groundwater percolating downward through fracture, faults reaching great depths of a kilometre or more where the temperature of rocks is high because of the normal temperature gradient of the Earth’s crust— about 30 °C (54 °F) per kilometre in the first 10 km.
5. The geochemical characteristic as established by the exploratory Factor Analysis as tabulated above distinguishes non-magmatic thermal sources as K-Na-HCO₃ of Peninsular springs as against the magmatic thermal sources as Cl-HCO₃-SO₄-Na type of Extra-Peninsular springs..
6. Unlike Extra-Peninsular Himalayan region which is an extension of active tectonic Alpine-Himalayan main thrust zone with a homogeneous lithology, there is a heterogeneity both in lithological as well as multi-directional tectonic settings. Naturally, these distinctive geologic-tectonic environs have definite bearing on their fluid geochemistry.

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