Optimum Support Design for Openings Considering Intact Rockmass in Production Level of Maddhapara, Granite Mine, Maddhapara, Dinajpur, Bangladesh

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Abstract: Maddhapara Granite mine is the only Hardrock underground mine, which is contributing to infrastructure development of Bangladesh. It was established in 1995 by the North Korean contractor (NAMNAM). Over the past few years it was observed that in some of the vital area of the pit bottom, appears to be vulnerable, where needs to be taken special consideration to make sure the safe working environment for the miners and equipment machinery as well. The authors of this research have taken an attempt to identify and overcome such problem by a research program. In this research, our outcome has been established that the, optimum support have to be determined by using Rock Support Interaction Analysis for rock mass in production level. During design stage, it was considered that the total rock mass is intact (based on initial geological survey data), means there are no wedges along the opening. However a little amount of geological abnormality anticipated in the production level during construction phase. Due respect to that, our research recommended that, there has to be a little amount of support is needed for any kinds of openings in first category of rock, in second category it has to be considered by shotcreting of different thickness of lining in roof and the sidewall. In third category of rock, support system has to be considered by rock bolting and latter shotcrete the roof and side wall. Finally 2.3, 4.6 and 10.73 m openings in third category of rock there needs to be 0.0095m, 0.015m and 0.026m fiber reinforced shotcrete and 3m bolt length and bolt spacing with 1.5, 1, 0.95m respectively in roof and inside wall 0.006m, 0.015 and 0.045m shotcrete lining have to be considered for safe mining work.

Keywords: Support equation, Data analysis, Intact rock mass, Broken rock mass, Uniaxial compressive strength.

I. INTRODUCTION

Maddhapara Granite Mining Company (MGMC) which is the first experience of underground hard rock mining and second major mining project in Bangladesh. The MGMC lies between latitude 25° 23’43” and 25°34’43” N and longitude 89°03’34”E and 89°05’04” E. It is about 23kms north east of Phulbari Railway station. The Bangladesh map and location map of the study area is in figure 1 and Figure: 2, the map of the production level is shown in figure: 3. The principle objective is to design the minimum underground support to make the tunnel stable resisting from further deformation. In order to design the support of production level the sequences of calculations of Rock Support Interaction Analysis and support equations of Hoek and Brown’s 1982 have been followed. And at last the suitable supports for particular openings with in the production Level have been determined.

Figure: 1, Map of Bangladesh
II. METHODOLOGY

In order to use Rock Support Interaction Analysis for support design the following steps have been followed:

1. Firstly the load deformation curves of different categories of rock have been generated considering the tunnel deformation and support pressure values.

2. Secondly the support stiffness and maximum support pressure have been calculated by using the equations of Hoek and Brown 1982. In the graph where support pressure and support stiffness of particular support system have satisfied the load deformation curves then the support has been considered for support estimation.

A program (Appendix-A) has been generated by following the sequence of calculation of Rock Support Interaction Analysis (Hoek and Brown, 1982). The values of support pressure and tunnel deformation have been determined by using this program. In case of preparing load deformation curves of different categories of rock the minimum value of load deformation has been taken to zero.

In selection of support system, the interactive nature of the load deformation characteristics of both rock mass and support system have been considered as proposed by Hoek and Brown 1982.

III. SUPPORT EQUATIONS

To have the support reaction the following equations of Hoek and Brown 1982 have been used.

For Shotcrete:

Support stiffness and maximum support pressure have calculated by using the following equations (Hoek & Brown, 1982)

\[
K_s = \frac{E_r(r_i^2 - (r_t - t)^2)}{(1 + \delta_r)(1 + 2\delta_r)r_t^2 + (r_t - t)^2)}
\]

\[
P_{r,max} = \frac{1}{2} \sigma_{r,conc} \left[ 1 - \frac{(r_i - t)^2}{r_i^2} \right]
\]
Here,
$E_c$ = modulus of elasticity
$\gamma_c$ = Possions ratio
$t_c$ = thickness of lining
$r_i$ = tunnel radius
$\sigma_{c,con}=\text{Uniaxial compressive strength}$

For Rock bolts:
Support stiffness and maximum support pressure for rock bolt have been calculated by using the following equations (Hoek & Brown, 1982)-

$$\frac{1}{K_b} = \frac{S_i S_j}{\eta_i} \left[ \frac{4Z}{\pi d_b E_b} + Q \right]$$

$$P_{s,\text{max}} = \frac{T_{bf}}{S_c S_l}$$

Here,
$l$ = bolt length
$d_b$ = bolt diameter
$E_b$ = elastic modulus
$Q$ = load deformation constant
$T_{bf}$ = Ultimate failure load
$r_i$ = tunnel radius
$S_c$ = Circumferencial bolt spacing
$S_l$ = Longitudinal bolt spacing

Combined support Calculation Sequence:
To use the combined support of shotcrete and rock bolt, the following sequences of combined support of Hoek & Brown, 1982 have been followed.
(a) $U_{max1}=r_i P_{s,\text{max1}}/K_1$
(b) $U_{max2}=r_i P_{s,\text{max2}}/K_2$
(c) $U_{12}=r_i P_i/(K_1 K_2)$
(d) For $U_{12}<U_{max1}<U_{max2}$

$$\frac{U_i}{\eta_i} = \frac{U_{in}}{\eta_i} + \frac{R_i}{(K_1 + K_2)}$$

(e) For $U_{12}>U_{max1}<U_{max2}$

$$P_{s,\text{max1}} = U_{max2}(K_1 + K_2)/\eta_i$$

(f) For $U_{12}>U_{max2}<U_{max1}$

$$P_{s,\text{max2}} = U_{max1}(K_1 + K_2)/\eta_i$$

Here,
$K_1$ = Support stiffness for system 1
$P_{s,\text{max1}}$ = maximum support pressure for system 1
$K_2$ = Support stiffness for system 2
$P_{s,\text{max2}}$ = maximum support pressure for system 2
$U_{in}$ = Initial tunnel deformation before installation of support

**IV. DATA ANALYSIS**

For Rock support Interaction Analysis certain types of data have been used to generate the load deformation curves.

Material Constants:
Material constants for intact rock and for broken rock mass have been used for Rock Support Interaction Analysis. These are given as follows-

For Intact Rock Mass:
The material constant value for different categories of rock with respect to rockmass rating determined by Badrul, 2006 (CSIR and NGI classification) have been estimated by using of Hoek and Brown 1982.
Table: 1. CSIR and NGI classification

<table>
<thead>
<tr>
<th>Category</th>
<th>Rock mass Rating</th>
<th>Quality</th>
<th>Material Constant Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>1&lt;sup&gt;st&lt;/sup&gt;</td>
<td>CSIR-92;NGI-24.25</td>
<td>Good</td>
<td>m-2.5;s-0.004</td>
</tr>
<tr>
<td>2&lt;sup&gt;nd&lt;/sup&gt;</td>
<td>CSIR-67;NGI-8.86</td>
<td>Fair</td>
<td>m-0.5;s-0.0001</td>
</tr>
<tr>
<td>3&lt;sup&gt;rd&lt;/sup&gt;</td>
<td>CSIR-39;NGI-5.12</td>
<td>Poor</td>
<td>m-0.13;s-0.00001</td>
</tr>
</tbody>
</table>

For Broken Rock Mass:
Material constant for different categories of rock has been taken from “Underground Excavation in Rock, Hoek and Brown, 1982”.

Table: 2. Material constant for different categories of rock

<table>
<thead>
<tr>
<th>Categories of rock</th>
<th>Material Constant</th>
</tr>
</thead>
<tbody>
<tr>
<td>1&lt;sup&gt;st&lt;/sup&gt;</td>
<td>m-0.13;s-0.00001</td>
</tr>
<tr>
<td>2&lt;sup&gt;nd&lt;/sup&gt;</td>
<td>m-0.025;s-0.0</td>
</tr>
<tr>
<td>3&lt;sup&gt;rd&lt;/sup&gt;</td>
<td>m-0.020;s-0.0</td>
</tr>
</tbody>
</table>

Table: 3. The average data of uniaxial compressive strength for different categories of rock

<table>
<thead>
<tr>
<th>Categories</th>
<th>Uniaxial Compressive Strength (Mpa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1&lt;sup&gt;st&lt;/sup&gt;</td>
<td>116.76</td>
</tr>
<tr>
<td>2&lt;sup&gt;nd&lt;/sup&gt;</td>
<td>67.86</td>
</tr>
<tr>
<td>3&lt;sup&gt;rd&lt;/sup&gt;</td>
<td>38.27</td>
</tr>
</tbody>
</table>

Table: 4. The strength ratio to the first category of rock.

<table>
<thead>
<tr>
<th>Category</th>
<th>Modulus of Elasticity(Mpa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1&lt;sup&gt;st&lt;/sup&gt;</td>
<td>67000</td>
</tr>
<tr>
<td>2&lt;sup&gt;nd&lt;/sup&gt;</td>
<td>38949.88</td>
</tr>
<tr>
<td>3&lt;sup&gt;rd&lt;/sup&gt;</td>
<td>21965.98</td>
</tr>
</tbody>
</table>

Table: 5. The Possion’s ratio for different categories of rock, geotechnical report of NAMNAM, 1998.

<table>
<thead>
<tr>
<th>Category</th>
<th>Possion’s ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>1&lt;sup&gt;st&lt;/sup&gt;</td>
<td>0.26</td>
</tr>
<tr>
<td>2&lt;sup&gt;nd&lt;/sup&gt;</td>
<td>0.23</td>
</tr>
<tr>
<td>3&lt;sup&gt;rd&lt;/sup&gt;</td>
<td>0.20</td>
</tr>
</tbody>
</table>


Uniaxial Compressive Strength:
Uniaxial compressive strength was carried out by Malek, (Unpublished thesis, 2003). The average data of uniaxial compressive strength for different categories of rock has been used in this analysis.

Table: 7. The average data of uniaxial compressive strength for different categories of rock

<table>
<thead>
<tr>
<th>Categories</th>
<th>Uniaxial Compressive Strength (Mpa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1&lt;sup&gt;st&lt;/sup&gt;</td>
<td>116.76</td>
</tr>
<tr>
<td>2&lt;sup&gt;nd&lt;/sup&gt;</td>
<td>67.86</td>
</tr>
<tr>
<td>3&lt;sup&gt;rd&lt;/sup&gt;</td>
<td>38.27</td>
</tr>
</tbody>
</table>

Modulus of Elasticity:
The modulus of elasticity of first category of rock has been taken from geological report of Korea South-South Cooperation Corporation (NAMNAM) 1998 and the values for other two categories of rock have been taken by using the strength ratio to the first category of rock.

Table: 8. The strength ratio to the first category of rock.

<table>
<thead>
<tr>
<th>Category</th>
<th>Modulus of Elasticity(Mpa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1&lt;sup&gt;st&lt;/sup&gt;</td>
<td>67000</td>
</tr>
<tr>
<td>2&lt;sup&gt;nd&lt;/sup&gt;</td>
<td>38949.88</td>
</tr>
<tr>
<td>3&lt;sup&gt;rd&lt;/sup&gt;</td>
<td>21965.98</td>
</tr>
</tbody>
</table>

Poisson’s Ratio:
The possion’s ratio for different categories of rock has been taken from geotechnical report of NAMNAM, 1998.


<table>
<thead>
<tr>
<th>Category</th>
<th>Possion’s ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>1&lt;sup&gt;st&lt;/sup&gt;</td>
<td>0.26</td>
</tr>
<tr>
<td>2&lt;sup&gt;nd&lt;/sup&gt;</td>
<td>0.23</td>
</tr>
<tr>
<td>3&lt;sup&gt;rd&lt;/sup&gt;</td>
<td>0.20</td>
</tr>
</tbody>
</table>

Insitue Stress Magnitude:
The Insitue stress magnitude in the production level is 7.78 Mpa (NAMNAM, 1998).

Circular Equivalent Radius:
As the tunnel consists of vertical walls and arched roof, calculations have been made in the manner of circular equivalent from the following equation (NAMNAM, 1998)
The circular equivalent radius of different types of openings are given as follows:

<table>
<thead>
<tr>
<th>Type of opening</th>
<th>Width (m)</th>
<th>$K_{type}$</th>
<th>$R_{equivalent}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Loop way</td>
<td>2.3</td>
<td>0.83</td>
<td>1.39</td>
</tr>
<tr>
<td>Main way</td>
<td>4.6</td>
<td>0.85</td>
<td>2.70</td>
</tr>
<tr>
<td>Crossing</td>
<td>9.2</td>
<td>0.87</td>
<td>5.29</td>
</tr>
<tr>
<td>Station</td>
<td>10.73</td>
<td>0.89</td>
<td>6.03</td>
</tr>
</tbody>
</table>

Table: 6. The circular equivalent radius of different types of openings data for shotcrete and rock bolt (Hoek and Brown, 1982)

In preparing the load deformation curves of different categories of rock by following the Hoek and Brown’s Rock Support Interaction Analysis the minimum value of radial deformation was taken to zero as tunnel deformation can not be less than zero. Selections of support system have been taken in to account the interactive nature of load deformation characteristics of the rock mass and support system as proposed by Hoek and Brown, 1982.

1st Category of Rock and Support System

By using the program of rock support interaction Analysis (Appendix-A) and the data (section 2.3) different types of values (support pressure, tunnel deformation etc) have been derived. Support pressure and tunnel deformation values have been plotted. From this plots the load deformation curve of roof, sidewall and floor for all kinds of openings in first categories of rock have been generated (figure-1.3). From the graph it is clear that the deformation curves are not increasing but decreasing on and on and introduction of small amount of support in the graph creates a steep support reaction with load deformation curves of roof, sidewall and floor. So, the loop ways in 1st category of rock would not collapse without support or very little amount of support is needed. Here the tunnel deformation $U$ is limited by proximity of the tunnel face which provides a significant amount of resistance.

![Figure 4(a): Load deformation curve and support reaction of 2.3 m opening in first category of rock.](image)
Optimum Support Design for Openings Considering Intact Rockmass in Production Level of

Figure 4(b): Load deformation curve and support reaction of 4.6 m opening in first category of rock.

Figure 4(C): Load deformation curve and support reaction of 9.2 m opening in first category of rock.

Figure 4(D): Load deformation curve and support reaction of 10.7 m opening in first category of rock.

2nd Category of Rock and Support System

Support pressure and load deformation curves have been driven by using the program (Appendix-A) By using these values load deformation curves for roof, sidewall and floor of different types of openings have been generated (figure: 4 a, b, c & d). The graphs show that, the load deformation curves of sidewall and floor are not increasing. It indicates that there are no needs of support, but the load deformation curves of the roof are increasing from their minimum value. It indicates that support is necessary for roof of the openings. The support for sidewall has also been considered for better stability of the tunnel. In case of floor, the openings Support has not been considered because it has no impact on stability of the openings. Support stiffness and support pressure have been calculated by using the support equations of Hoek and Brown, 1982.

By using the data in the equations of support of Hoek and Brown, 1982, the support pressure and support stiffness values have been driven. The support suitable for particular opening has been

Determined by varying the thickness of lining and considering the load deformation curves (figure: 4 a, b, c &d). It is found that the shotcrete linings have enough support pressure and stiffness for all kinds of openings to make all of them stable, resisting from further deformation. The support for particular openings is given in Table: 8, behind the point where the load deformation curves begin to increase from their minimum tunnel deformation.
Optimum Support Design for Openings Considering Intact Rockmass in Production Level of

<table>
<thead>
<tr>
<th>Opening (m)</th>
<th>Circular equivalence</th>
<th>For Roof Thickness of lining(m)</th>
<th>Support pressure (Mpa)</th>
<th>For sidewall Thickness of lining(m)</th>
<th>Support pressure (Mpa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.30</td>
<td>1.39</td>
<td>0.003</td>
<td>0.0743801</td>
<td>0.0021</td>
<td>0.0496096</td>
</tr>
<tr>
<td>4.60</td>
<td>2.70</td>
<td>0.008</td>
<td>0.1020708</td>
<td>0.0041</td>
<td>0.0510733</td>
</tr>
<tr>
<td>9.2</td>
<td>5.29</td>
<td>0.023</td>
<td>0.1496939</td>
<td>0.013</td>
<td>0.0756874</td>
</tr>
<tr>
<td>10.73</td>
<td>6.03</td>
<td>0.027</td>
<td>0.1541318</td>
<td>0.015</td>
<td>0.0976874</td>
</tr>
</tbody>
</table>

Table: 8. Support for second category of rock

Figure: 5(a), Load deformation curve and support reaction of 2.3m opening in second category of rock.

Figure: 5(b), Load deformation curve and support reaction of 4.6m opening in second category of rock.

Figure: 5(C), Load deformation curve and support reaction of 9.2m opening in second category of rock.
Figure 5(d): Load deformation curve and support reaction of 10.73m opening in second category of rock.

3rd Category of Rock and Support System

Tunnel deformation and support pressure values of different types of openings have been derived by using the program of Rock Support Interaction (Appendix-A). From these values the load deformation curves of roof, sidewall and floor of the openings have been generated (figure: 5a, b, c &d), from these graph it appears that the load deformation curves of floor and sidewall are not increasing. There is no necessity of support installation. The load deformation curves of the roof are increasing steeply from there minimum value. It indicates the necessity of high amount of support installation to make the openings stable. Supports have been considered for sidewall for better stability of the openings. Supports have not been considered for floor because it will not affects the stability of the openings. In order to have effective support for roof shotcrete and rock bolt supports have been considered together as high amount of support needed over there, for sidewall shotcrete support has been considered for sidewall of the openings as less amount of support is needed.

Figure 6(a): Load deformation curve and support reaction of 2.3m opening in Third category of rock.

Figure 6(b): Load deformation curve and support reaction of 4.6m opening in Third category of rock.
Figure 6(c): Load deformation curve and support reaction of 10.73 m opening in Third category of rock.

The support reaction curves have been generated by using the data in the equations of supports (Hoek and Brown, 1982 and following the combined support calculations of Hoek and Brown 1982 (section 2.2). The supports have been estimated for particular openings by considering the load deformation curves and support reactions (figure: 6a, b & c). The support system suitable for different types of openings in third category of rock is given in Table: 9.

<table>
<thead>
<tr>
<th>Openings</th>
<th>Circular equivalence</th>
<th>Roof Shotcrete lining (m)</th>
<th>Circumference bolt spacing</th>
<th>Longitudinal bolt spacing</th>
<th>Support pressure (Mpa)</th>
<th>Sidewall Shotcrete lining (m)</th>
<th>Support pressure (Mpa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.30</td>
<td>1.39</td>
<td>0.0075</td>
<td>1.35</td>
<td>1.35</td>
<td>0.2241753</td>
<td>0.0060</td>
<td>0.148599</td>
</tr>
<tr>
<td>4.60</td>
<td>2.70</td>
<td>0.025</td>
<td>1.0</td>
<td>1.0</td>
<td>0.2865526</td>
<td>0.015</td>
<td>0.191613</td>
</tr>
<tr>
<td>10.73</td>
<td>6.03</td>
<td>0.026</td>
<td>0.95</td>
<td>0.95</td>
<td>0.4531680</td>
<td>0.045</td>
<td>0.256502</td>
</tr>
</tbody>
</table>

Table: 9, Support requirements for third category of rock

V. CONCLUSION

In case of 1st category of rock mass, there has to be considered negligible amount of support or even it can be ignored. In case of 2nd category of rock mass for 2.3, 4.6, 9.2 and 10.73 m openings it has to be considered 0.003, 0.008, 0.023 and 0.027m shotcrete lining in roof and 0.0021, 0.004, 0.013 and 0.015m shotcrete lining in sidewall respectively. Finally for 3rd category of rock mass has to be handle very carefully and special care has to be considered for the 2.3, 4.6, 9.2 and 10.73m openings needs to be 0.0095, 0.015, 0.026m shotcrete lining with 3m long bolt has to be rock bolted with a spacing of 1.15, 1.0, 0.95m respectively in roof and for sidewall 0.006, 0.015 and 0.045m shotcrete linings respectively.

REFERENCES

Reports:

Books:

Theses:

Theses report:

APPENDIX

Rock Support Interaction Analysis Program [followed the sequence of calculations of Rock Support Interaction Analysis (Heok and Brown, 1982)].

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REAL B, PO, QC, SLA, C, U, E, P1, M, V, D, N, PR, PF, AI, L, R, EAV, K, UI, PS
PRINT*, 'ENTER YOUR VALUE FOR M. C. OF INTACT ROCK, B'
READ(*, *) B
PRINT*, 'ENTER YOUR VALUE FOR M. C. OF INTACT ROCK, SI'
READ(*, *) SI
PRINT*, 'ENTER YOUR VALUE FOR IN-SITU STRESS MAGN., PO'
READ(*, *) PO
PRINT*, 'ENTER YOUR VALUE FOR UNIAXIAL COM. STRE. QC'
READ(*, *) QC
PRINT*, 'ENTER YOUR VALUE FOR M. C. OF BROKEN ROCK, MR, A'
READ(*, *) A
PRINT*, 'ENTER YOUR VALUE FOR M. C. OF BROKEN ROCK, SR, C'
READ(*, *) C
PRINT*, 'ENTER YOUR VALUE FOR POISSON RATIO, U'
READ(*, *) U
PRINT*, 'ENTER YOUR VALUE FOR MODULUS OF ELASTICITY, E'
READ(*, *) E
PRINT*, 'ENTER YOUR VALUE OF SUPPORT, MPA, P1'
READ(*, *) P1
M = (0.5 * (((B/4)**2) + ((B*PO)/QC) + SI)**0.5) - (B/8)
WRITE(*, *) M
V = (PO - (M*QC))
D = ((-B)/(B + (4 * (((B*V)/QC) + SI)**0.5)))
WRITE(*, *) D
N = 2 * (((V/(A*QC)) + (C/(A)**2))**0.5)
WRITE(*, *) N
IF (P1 .GE. V) THEN
K = (((1+U)/E)*(PO - P1))
WRITE(*,*) 'THE VALUE OF U/ri'
WRITE(*,*) K
ELSE
UR = (((1+U)/E)*(M*QC))
WRITE(*,*) 'PLASTIC FAILURE'
I = EXP(-2 * ((P1/(A*QC)) + (C/(A)**2))**0.5)
WRITE(*,*) I
RE = I**2.47
IF (I .GE. 1.73) THEN
R = 1.1 * D
ELSE
IF (I .LE. 1.73) THEN
R = (2 * D**(ALOG(I)))
END IF
END IF
EAV = (2*UR*(I**2))/(((I**2)-1)*(1+(1/R)))
WRITE(*,*) 'THE VALUE OF EAV'
WRITE(*,*) EAV
A = ((2*UR)-EAV)**(I**2)
PRINT*, 'THE VALUE OF A'
WRITE(*,*) A
K = 1 - ((1-EAV)/(1+A)**0.5)
END IF
U = K**2.47
PRINT*, 'DEFORMATION OR DISPLACEMENT, M'
WRITE(*,*) U
PR = (P1 + (0.03*(RE-2.47)))*PO
PRINT*, 'P1 FOR THE ROOF WALL, MPA'
WRITE(*,*) PR
PF = (P1 - (0.03*(RE-2.47)))/PO
PRINT*, 'P1 FOR THE FLOOR WALL, MPA'
WRITE(*,*) PF
PS = P1/PO
PRINT*, 'P1 FOR THE SIDE WALLS OF TUNNEL, MPA'
WRITE(*,*) PS
STOP
END