# Optimization of Consignment Stock Policy Using Particle Swarm Algorithm

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**Abstract:** In recent years, companies have strengthened their supply agreements, and even the management of their inventories. To this aim, a particular VMI policy, known as Consignment Stock (CS) represents an interesting strategy to stock monitoring and control for both the buyer and the supplier, and it has been progressively considered and introduced in several companies. CS has been previously analyzed for single vendor single buyer case (1986). In this project, we have analyzed analytical model for single vendor multi buyer CS policy. Four types of models, basic CS model, CS with delay, CS with delay with information sharing; CS with crashing lead time. The main objective of this work is to optimize the Joint Total Economic cost of each model. Analytical model is solved with enumeration technique up to five buyers. For more than five buyers, solving analytical model with complete enumeration becomes computationally expensive. To overcome this problem Particle Swarm Algorithm (PSO) is proposed for finding optimum for the case of more than five buyers. PSO model is developed and can solve more than ten buyers. So Particle Swarm Algorithm (PSO).

Keywords: Numerical approach, Total cost, Taguchi,

# I. Introduction

### **1.1 Consignment stock policy strategies:**

The consignment stock policy was developed for three different models in the case of single vendor – single buyer and single vendor –multi buyer. For single vendor –single buyer: basic consignment stock policy, consignment stock policy with delay deliveries, and consignment stock policy with controllable lead times. For single vendor –multi buyer: Basic consignment stock policy, Consignment stock policy with delay deliveries, Consignment stock policy with information sharing with delay deliveries, consignment stock policy with controllable lead times.

## 1. CSP model:

This is a basic model in which basic concepts and a condition of the consignment stock has been implemented.

**2. CSP model with delay deliveries:** The basic CSP model may not be suitable for the limited periods because the maximum level of the buyer's inventory may reach immediately. Therefore consignment stock policy with delayed delivery is an alternate policy. In this model, the last delivery is delayed until it reaches that there is no further increase in the maximum level already reached. That means it has to delay the stock always whenever maximum level inventory stock at the buyer is reached. Hence it doesn't allow exceeding the maximum limit 'S' in the buyer's inventory. In this situation the shipments if any with vendor has to wait at vendor's place.

## 3. CSP with delay with information sharing:

In the previous model we have not considered the effect of information sharing on the inventory. There are four common types of information sharing strategies for a supply chain of a single product:

(1) Order information sharing where every stage of the supply chain only knows the orders from its immediate downstream stage;

(2) demand information sharing where every stage of the supply chain has full information about consumer demand;

(3) Inventory information sharing where each stage shares its inventory and demand information with its immediate upstream stage; and

(4) Shipment information sharing where every stage shares its shipment data with its immediate upstream stage Order information sharing is common between two parties. Inventory and shipment information sharing will lead to reduction in the inventory cost. Due to information sharing vendor will know inventory status of the buyer all the time. Vendor can thus decide which buyer can accommodate the delayed delivery and the delayed delivery from one buyer is transferred to that buyer. Here principle assumption made to simplify the problem is that the shifted quantity to another buyer will be same as his economic order quantity and vendor will make necessary changes in the shipment size.

### 4. CSP with controllable lead time:

In recent years industries have devoted considerable attention in reducing the inventory cost. The characteristics of JIT systems are consistent high quality, small lot sizes, frequent delivery, short lead time and close supplier ties. Hence the control of lead time is one of the key factors to the success of JIT production. Traditionally the lead time of an inventory model is hypothesized as known (Kim and Park, 1985) or with certain probability distribution (Foot et al.1988). Actually, lead time can be reduced by an additional crashing cost, so as to improve customer service level, and reduce inventory in safety stocks i.e., it is controllable. When the assumption of deterministic consumer demand is assumed to be stochastic, lead time becomes an important issue and its control leads to many benefits. The Japanese experience of using JIT production shows that there are advantages and benefits associated with their efforts to control lead time. In many practical situations lead time can be reduced at an added cost. Lead time is reduced one at a time starting from the first independent component because it is having minimum unit crashing cost of the buyer. Since lead time is a decision variable in this model, the extra costs incurred by the vendor will be fully transferred to the buyer if shortened lead time is requested.

### **1.2 Limitations of analytical model:**

All four models are developed for two, three and four buyers. Solving analytical model becomes computationally more expensive as the number of buyers increases. For one vendor three buyers CS with delay with information sharing, its taking more than 1 hour to calculate the optimum whereas for one vendor four buyers CS with delay with IS, results could not be obtained even after 48 hours. Therefore solving analytical model by complete enumeration is almost impossible for more than five buyers. One of the solutions to above problem is to develop a heuristic algorithm to solve the model. We propose a Particle Swarm Algorithm to find optimum values of variables that will give minimum joint total cost.

## II. Generalizing The Basic Cs Model For Multiple Buyers

 $\begin{array}{l} \textbf{2.1 For basic CS model:} \\ \textbf{T}_{c} = \frac{s + \sum_{i=1}^{y} A_{i} + \sum_{i=1}^{y} n_{i} \cdot At_{i}}{c} + h_{v} \frac{c}{2p} [\sum_{i=1}^{y} \frac{D_{i}^{2}}{n_{i}}] + \sum_{i=1}^{y} \left(\frac{h_{bi}}{2} \left\{ D_{i}c - (n_{i} - 1)D_{i} \left[\frac{D_{i}c}{n_{i}p} + \sum_{i \neq j} \frac{D_{i}c}{n_{j}p} \left(\frac{n_{i}}{n_{j}}\right)\right] \right\} \right) + \sum_{i=1}^{y} \left(hb_{i} \cdot z \cdot \sigma_{i} \cdot Li + i = 1y\pi i \cdot \sigma_{i} \cdot Li \cdot \phi zc - \cdots (1) \right)$ 

# 2.2 CS with Delay Model For Multiple Buyers:

$$\mathbf{T}_{\mathbf{c}} = \frac{s + \sum_{i=1}^{y} A_{i} + \sum_{i=1}^{y} n_{i} \cdot At_{i}}{c} + h_{v} c \left\{ \frac{1}{2p} \left[ \sum_{i=1}^{y} \frac{D_{i}^{2}}{n_{i}} \right] + \sum_{i=1}^{y} \left( \frac{D_{i}}{n_{i}} \frac{(p-D_{i})}{n_{i}p} \frac{(k_{i}+1)}{2} k_{i} \right) \right\} + \sum_{i=1}^{y} \left\{ \frac{hb_{i}}{2} \left\{ (n_{i} - k_{i}) \frac{D_{i}c}{n_{i}} - n_{i} - h_{i} - h_{$$

## 2.3 CS with Delay and Information Sharing:

 $\mathbf{T}_{\mathbf{c}} = \frac{s + \sum_{i=1}^{y} A_{i} + \sum_{i=1}^{y} n_{i} \cdot A_{i}}{c} + h_{v} c \left\{ \frac{1}{2p} \left[ \sum_{i=1}^{y} \frac{D_{i}^{2}}{n_{i}} \right] + \sum_{i=1}^{y} \left( \frac{D_{i}}{n_{i}} \frac{(p-D_{i})}{n_{i}p} \frac{(k_{i}-m_{i}+1)}{2} (k_{i}-m_{i}) \right) \right\} + \sum_{i=1}^{y} \left\{ \frac{hb_{i}}{2} \left\{ \left( n_{i} - k_{i} + \frac{hb_{i}}{2} \left( n_{i} - hb_{i} + hb_{i} + hb_{i} + \frac{hb_{i}}{2} \left( n_{i} - hb_{i} + hb_{i} +$ 

# 2.4 Cs with Crashing Lead Time Model For Multiple Buyers:

 $\mathbf{T}_{c} = \frac{s + \sum_{i=1}^{y} A_{i} + \sum_{i=1}^{y} A_{i}}{c} + h_{v} \frac{c}{2p} \left[ \sum_{i=1}^{y} \frac{D_{i}^{2}}{n_{i}} \right] + \sum_{i=1}^{y} \left( \frac{h_{bi}}{2} \left\{ D_{i}c - (n_{i} - 1)D_{i} \left[ \frac{D_{i}c}{n_{i}p} + \sum_{i\neq j} \frac{D_{i}c}{n_{j}p} \left( \frac{n_{i}}{n_{j}} \right) \right] \right\} \right) + \sum_{i=1}^{y} \left( hb_{i} \cdot z \cdot \sigma_{i} \cdot Li + i = 1y\pi i \cdot \sigma_{i} \cdot Li \cdot \phi zc + i = 1yCLic - ---(4) \right)$ 

## III. Iterative Algorithm For The Proposed Pso Model

**Step 1:** Initialize the swarm, P(t), of particles such that the position  $X_i(t)$  of each particle Pi belongs to P(t) is random within the hyperspace (starting with t = 0).

**Step 2:** Initialize a swarm of velocity V(t), such that the velocity  $V_i(t)$  of each particle  $P_i$  belongs to V(t) is random within the hyperspace with t = 0 and follows the following function:

$$V_{i}(t) = -\begin{cases} -4 & \text{if} & V_{i}(t) \leq -4 \\ V_{i}(t) & \text{if} & -4 \leq V_{i}(t) \leq 4 \\ 4 & \text{if} & V_{i}(t) \geq 4 \end{cases}$$

Step 3: Now evaluate the performance of  $F_i(t)$  for each particle  $P_i(t)$ , using its current position  $X_i(t)$ .

**Step 4:** Now the position  $X_i(t)$  of particle  $P_i(t)$  is set as Pbest i(t). **Step 5:** Compare the performance of each individual to its best performance thus far:  $F(X_{i}(t)) < F(X_{i}(t-1))$ If Then set.  $X_i(t) = Pbest_i(t)$  $X_i(t-1) = pbest_i(t)$ . orelse Step 6: Compare the performance of each particle with that of the best particle of the swarm.  $F(X_i(t)) < F(gbest)$ If  $X_i(t) = gbest(t).$ Then set. **Step 7:** Now change the velocity vector for each particle  $P_i(t)$ :  $V_{i}(t+1) = W(t)^{*}(V_{i}(t)) + c_{1}^{*}r_{1}^{*}(X_{ipbest}(t) - X_{i}(t)) + c_{2}^{*}r_{2}^{*}(X_{igbest} - X_{i}(t));$ Where, W = inertia weight. = acceleration constants = 1, 2 respectively  $c_{1}, c_{2}$ = positive constants = 0.2, 0.3 respectively.  $r_1, r_2$ Step 8: now update the positions of the particles, using their new velocities  $X_i(t+1) = X_i(t) + V_i(t+1)$ Now, t = t+1. Step 9: Go to step 3 and repeat until the given number of iterations. HERE,

## IV. Results And Discussion

This study is focused around the implementation of an evolutionary particle swarm optimization technique on consignment stock policy models. This section carries the results and few discussions over the same. For the result, the input data (Table.1) is taken from HANS SIJADI et. Al.(2005). This input is for single vendor two buyers and three buyer problem but has now been extended to ten buyers

### The input data is tabulated below:

Table 1:	Input data
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		VENDOR							
PRODUCTI	ON	HOLD	NG	SET UP	SHORTAG	FΕ			
RATE/TOT	AL	COST	PER	COST(Rs)	COST FO	R			
DEMANI	)	UNIT(	Rs)		BUYER(R	s)	INPUT DATA FROM		
							HANS SIJAI	DI .ET. AL (2005),	
2.5		4		200	50		EXTENDED TO TEN BUYERS		
					BUYERS				
NO.OF	DEMAND STANDAR		ANDARD	HOLDING	Т	RANSPORTATION	ORDERING	Lead	
BUYERS	(U	JNITS	DF	VIATION	COST PER		COST(Rs)	COST(Rs)	time(d
	PER	R YEAR)	OF	DEMAND	UNIT(Rs)				ays)
1	1	0000		50	8		30	100	7
2	1	3000		60	8		30	100	7
3	5	8000		30	8		30	100	7
4	1	7000		60	5		30	100	7
5	(	6000		30	7		30	100	7
6	1	0000		50	8		30	100	7
7	5	8000		30	7		30	80	7

8	5000	30	7	30	80	7
9	10000	50	8	30	100	7
10	12000	50	7	20	80	7

S.NO.	LEAD TIME	CRASHING COST
1	7	0
2	5.25	0.7
3	3.5	2.8
4	2.62	7.2

**Table 2:** lead time components with crashing costs

Table 3: shows results of the above example by particle swarm approach. Optimum cycle time, optimum number of shipments for each buyer and optimum shipment size has also been calculated and tabulated as well. The maximum inventory that a buyer can have has also been listed in Table 3.

NO.OF BUYERS	TYPE OF MODEL	PSO RESULTS			
DerEks	MODEL	OPTIMUM CYCLE TIME(YRS)	OPTIMUM NO.OF SHIPMENTS	OPTIMUM SHIPMENT SIZE	MAX INVENTORY OF BUYER
1V-2B	CS-BASIC	0.100	n <sub>1</sub> =9,n <sub>2</sub> =3	$q_1=112$ $q_2=433$	b <sub>1MAX</sub> =667
	CS-DELAY	0.106	$n_1=5, n_2=9$ $K_1=1, K_2=2$	$q_2 = 433$ $q_1 = 212$ $q_2 = 154$	b <sub>1MAX</sub> =531 b <sub>1MAX</sub> =615 b <sub>2MAX</sub> =731
	CS-IS	0.113	$\begin{array}{c} n_1 = 10, n_2 = 10 \\ K_1 = 7, K_2 = 4 \\ M_1 = 3, M_2 = 1 \\ J_{12} = 1, j_{21} = 1 \end{array}$	$q_1 = 113$ $q_2 = 147$	b <sub>1MAX</sub> =339 b <sub>2MAX</sub> =700
	CS-CLT	0.105	n <sub>1</sub> =4,n <sub>2</sub> =3	$q_1=263$ $q_2=455$	b <sub>1MAX</sub> =738 b <sub>2MAX</sub> =1028
1V-3B	CS-BASIC	0.107	$n_1=3, n_2=3$ $n_3=1$	$q_1=357$ $q_2=463$ $q_3=856$	b <sub>1MAX</sub> =807 b <sub>2MAX</sub> =1047 b <sub>3MAX</sub> =870
	CS-DELAY	0.116	$\begin{array}{c} n_1 {=} 10, n_2 {=} 9 \\ n_3 {=} 1, K_1 {=} 2 \\ K_2 {=} 1, K_3 {=} 1 \end{array}$	$q_1=116$ $q_2=168$ $q_3=928$	b <sub>1MAX</sub> =625 b <sub>2MAX</sub> =890 b <sub>3MAX</sub> =384
	CS-IS	0.107	$n_{1}=10, n_{2}=9$ $n_{3}=9, K_{1}=7$ $K_{2}=6, K_{3}=4$ $M_{1}=5, M_{2}=5$ $M_{3}=4, j_{12}=3$ $j_{23}=1, j_{33}=1$	$q_1=107 \\ q_2=155 \\ q_3=106$	b <sub>1MAX</sub> =387 b <sub>2MAX</sub> =740 b <sub>3MAX</sub> =566
	CS-CLT	0.107	$n_1=10, n_2=7$ $n_3=4$	$q_1=107$ $q_2=196$ $q_3=214$	b <sub>1MAX</sub> =711 b <sub>2MAX</sub> =942 b <sub>3MAX</sub> =613
1V-4B	CS-BASIC	0.115	$n_1=7, n_2=2$ $n_3=3, n_4=2$	$\begin{array}{c} q_1 = 165 \\ q_2 = 747 \\ q_3 = 307 \\ q_4 = 977 \end{array}$	$\begin{array}{c} b_{1MAX} = 1133 \\ b_{2MAX} = 1223 \\ b_{3MAX} = 689 \\ b_{4MAX} = 1982 \end{array}$
	CS-DELAY	0.104	$\begin{array}{c} n_1 {=} 10, n_2 {=} 10 \\ n_3 {=} 8, n_4 {=} 7 \\ K_1 {=} 5, K_2 {=} 1 \\ K_3 {=} 2, K_4 {=} 1 \end{array}$	$\begin{array}{c} q_1 = 104 \\ q_2 = 136 \\ q_3 = 104 \\ q_4 = 253 \end{array}$	$\begin{array}{c} b_{1MAX}\!\!=\!\!376 \\ b_{2MAX}\!\!=\!\!811 \\ b_{3MAX}\!\!=\!\!430 \\ b_{4MAX}\!\!=\!\!1031 \end{array}$
	CS-IS	0.102	$\begin{array}{c} n_1\!\!=\!\!9,\!n_2\!\!=\!\!8\\ n_3\!\!=\!\!7,\!n_4\!\!=\!\!8\\ K_1\!\!=\!\!8,\!K_2\!\!=\!\!7\\ K_3\!\!=\!\!6,\!K_4\!\!=\!\!7\\ M_1\!\!=\!\!7,\!M_2\!\!=\!\!6\\ M_3\!\!=\!\!5,\!M_4\!\!=\!\!4\\ j_1\!\!=\!\!6,\!j_{23}\!\!=\!\!5\\ J_{34}\!\!=\!\!4,\!j_{41}\!\!=\!\!2\\ \end{array}$	$\begin{array}{c} q_1 = 115 \\ q_2 = 166 \\ q_3 = 117 \\ q_4 = 217 \end{array}$	b <sub>1MAX</sub> =360 b <sub>2MAX</sub> =745 b <sub>3MAX</sub> =356 b <sub>4MAX</sub> =967
	CS-CLT	0.101	$n_1=8, n_2=7$ $n_3=6, n_4=4$	$\begin{array}{r} q_1 = 127 \\ q_2 = 188 \\ q_3 = 135 \\ q_4 = 430 \end{array}$	$\begin{array}{c} b_{1MAX}{=}680 \\ b_{2MAX}{=}890 \\ b_{3MAX}{=}553 \\ b_{4MAX}{=}1230 \end{array}$

**Table 3:** result of the given example.

Table 4 shows the various costs, included in the given PSO model. Total cost, incurred by vendor and the same incurred by individual buyer has also been tabulated in table5.4. The data shows that the cost, incurred by buyers in each model is less than that of their corresponding basic model. Percentage savings, obtained in

different models with respect to basic model has also been enlisted below. It is very obvious, from the Table5.4 that the joint total economic cost of models (like: CS-delay, CS-information sharing, & CS-crash lead time) comes out to be less than that of their corresponding basic CS model.

NO.OF BUYERS	TYPE OF MODEL	PSO RESULTS				
		COST, INCURRED BY VENDOR	COST, INCURRED BY BUVERS	JTEC	% SAVING DUE TO PSO	
1V-2B	CS-BASIC	2029	b <sub>1</sub> =4956 b <sub>2</sub> =4941	11926	NA	
	CS-DELAY	2327	b <sub>1</sub> =4752 b <sub>2</sub> =3159	10238	14.1539	
	CS-IS	2250	b <sub>1</sub> =3625 b <sub>2</sub> =4230	10110	15.2691	
	CS-CLT	2240	b <sub>1</sub> =3035 b <sub>2</sub> =4180	9455	20.1044	
1V-3B	CS-BASIC	2239	$b_1=4933$ $b_2=4882$ $b_3=2558$	14666	NA	
	CS-DELAY	2789	$b_1=3882$ $b_2=4669$ $b_3=2221$	13561	14.3529	
	CS-IS	2057	$b_1=4894$ $b_2=4601$ $b_3=3165$	12782	23.7556	
	CS-CLT	2013	$b_1=2550$ $b_2=3874$ $b_3=2614$	11051	31.4673	
1V-4B	CS-BASIC	2523	$b_1=5647$ $b_2=5202$ $b_3=4733$ $b_4=3510$	21615	NA	
	CS-DELAY	2541	$b_1=5258$ $b_2=4845$ $b_3=3433$ $b_4=3070$	19148	11.4133	
	CS-IS		NA	18500	14.3974	
	CS-CLT	2116	$b_1=4515$ $b_2=4187$ $b_3=3176$ $b_4=3087$	17092	20.9252	

 Table 4: various costs, incurred by buyers and vendor in given model.

# 4.1 A Comparative view of CPU time, consumed by particle swarm approach and analytical approach.

Table 5 shows a comparison between the computational time, elapsed in calculating, the results of different CS models, by analytical approach and by PSO approach. A pictorial comparison of the same can be viewed in Fig5.

**Table 5:** CPU time elapsed in analytical and PSO approach

NO.OF BUYERS	TYPE OF MODEL	ANALYTICAL APPROACH	PSO APPROACH	%SAVING OF CPU TIME IN PSO	
		CPU TIME (s)	CPU TIME(s)		
1V-2B	CS-BASIC	0.09	0.77	-88.311	
	CS -DELAY	1.89	0.85	122.35	
	CS -IS	9.28	1.15	706.95	
	CS -CLT	0.28	1.06	-73.58	
1V-3B	CS-BASIC	0.73	1.64	-55.48	
	CS-DELAY	NA	1.72	NA	
	CS-IS	NA	1.89	NA	
	CS-CLT	2.75	0.74	271.62	
1V-4B	CS-BASIC	7.89	1.50	426.00	
	CS-DELAY	NA	2.06	NA	
	CS-IS	NA	2.07	NA	
	CS-CLT	28.03	2.06	1260.67	

## 4.2 Pictorial Representation of Foremost Results of Given PSO Model.

Few focal results, obtained after complete particle swarm enumeration of the given example have been pictorially sorted out in this section.



## fig 1: no. of populations

CS model, it also indicates the working speed of algorithm with 1v-2b and 1v-3b basic CS models. Fig 1 shows the response of given algorithm with respect to basic CS 1v-2b and 1v-3b model. Fig 2 shows the variations in the joint total economic costs of different consignment stock policy models. Fig 3 shows the percentage savings of CS –delay, CS- with information sharing and CS-crashing lead time models over basic CS model.Fig5. Shows the percentage saving of CPU time in PSO over analytical approach.



Fig 2: various models with their jtec.



fig 3: percentage saving of diff.cs models with respect to basic cs model.



fig4: percentage saving in cpu time by pso over analytical approach.

# V. Conclusion

1. An attempt is made to develop mathematical models for CSP in VMI and optimization of these models has been done by enumerative technique. Solving these mathematical models for many buyers is time consuming and may not be computationally economical.

2. The optimization of the same CS problem has been done by applying particle swarm optimization technique. The PSO models have been developed for CS problem and it has shown that the execution of PSO, leading to the optimal solutions, has taken a short span of time and thus, computationally better solutions have been obtained for number of buyers (currently upto four buyers).

3. JTEC for various buyers has been calculated and it took nearly 2 s for four buyer model against several hours of enumerative techniques.

4. The efficiency of the models has been tested thoroughly and it is found that solving the CS models for various buyers by using PSO is better, than, the same solved by enumerative techniques. Solving the JTEC for CS models by PSO is much better technique. A sensitivity analysis upto four buyer has also been done.

5. The results show that the CS-delay model, CS-IS model, CS-CLT model, all are incurring less JTEC than that of CS-basic model, irrespective of the buyer sizes. The percentage savings of each model with respect to CS-basic model has also been enlisted.

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