Neural – Adaptive Control Based on Feedback Linearization for Electro Hydraulic Servo System

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Abstract: Neural Adaptive based on feedback linearization is used in this study to control the velocity and recognition of an electro hydraulic servo system (EHSS) in the presence of flow nonlinearities as well as internal friction and noise. This controller consists of four parts: PID controller, feedback linearization controller, neural network controller and the neural network identifier. The feedback linearization controller is used to prevent the system state in a region where the neural network can be accurately trained to achieve optimal control. The combination of controllers produces a stable system which adapts to optimize performance. This technique, as shown, can be prosperously used to stabilize any selected operating point of the system with noise and without interference. All consequences achieved are validated by computer simulation of a nonlinear mathematical model of the system. The fore mentioned controllers have a vast range to control the system. We compare Neural Adaptive based on feedback linearization controller results with feedback linearization, back stepping and PID controller.

Keywords: Electro Hydraulic servo system; feedback linearization; RBF; EHSS.

I. INTRODUCTION

An introduction to the hydraulic systems liquids is also uncompressible. This property has caused to use liquids as a proper means to exchange and transport work. Therefore, they can be used in designing which why simple can move extra resisting power with little motivating force, this property is called hydraulic. Nowadays, in very industrial process is, transporting power as a very cheap and highly accurate method is aimed at. In this regard, applying compressed liquid to transport and control power is a spreading in all industrial branches [1, 2].

Applications of liquid power are divided into two important branches of hydraulic and pneumatic. Pneumatic is used in cases where relatively low forces (about ton) and high speed movement is needed (such as the systems used in moving parts). Pneumatic is used in cases where relatively low forces (about ton) and high speed movement is needed (such as the systems used in moving parts of robots. While hydraulic system applications are basically in cases where high power and speedy accurate controls are desired [1, 2].

Because the EHSS has proper control over inertial and torque loads, it is widely used in industry. Furthermore it yields precise and immediate answers [1, 2]. EHSS can be classified according to the aimed function, velocity, torque, force etc. In the past, dozens of studies have been carried out regarding different ways of handling methods of electro hydraulic servo system (EHSS). Reference [3] gives more information in this regard. An intelligent CMAC, FNN neural controller that uses a feedback error learning approach appears in [4, 5] which is highly complicated and [3] explain ways based on feedback linearization and back stepping However, it is not easy , nor is it simple to design such controllers. Other control methods will appear in [6-13].

Here, we intend to analyze and propose an adaptation based on the feedback linearization controller as well as the identifier for the EHSS system.

The rest of the paper is arranged as follows. Part II, contains the mathematical model of the EHSS system. Part III deals with the RBF controller, identifier, PID controller and adaptive controller in detail. Section IV discusses the simulation results of the proposed control strategies. In the end, the conclusion is given in Section V.

II. COMPOSE A MATHEMATICAL MODEL OF THE SYSTEM

An outline of an electro hydraulic velocity servo system is shown in Fig. 1. The basic components of this system are: 1. Hydraulic power supply, 2. Accumulator, 3. Charge valve, 4. Pressure gauge device, 5. Filter, 6. Two-stage electro hydraulic servo valve, 7. Hydraulic motor, 8. Measurement device, 9. Personal computer, and 10. Voltage - to- current converter.



Fig. 1. Electro hydraulic velocity servo system

A mathematical representation of the system is derived using Newton's Second Law for the rotational motion of the motor shaft. It is assumed that the motor shaft does not change its direction of rotation, $x_1>0$. This is a practical assumption and in order to be satisfied, the servo valve displacement x_3 does not have to move in both directions. This assumption restricts the entire problem to the region where $x_3>0$. If the state variables are as follows:

1. x_1 is hydro motor angular velocity.

- 2. x_2 is load pressure differential.
- 3. x_3 is valve displacement.

Then the model of the EHSS is given by:

$$\dot{x}_{1} = \frac{1}{j_{t}} \left\{ -B_{m}x_{1} + q_{m}x_{2} - q_{m}c_{f}p_{s} \right\}$$

$$\dot{x}_{2} = \frac{2B_{e}}{v_{o}} \left\{ -q_{m}x_{1} - c_{im}x_{2} - c_{d}wx_{3}\sqrt{\frac{1}{\rho}(p_{s} - x_{2})} \right\}$$

$$\dot{x}_{3} = \frac{1}{T_{r}} \left\{ -x_{3} + \frac{k_{r}}{k_{q}}u \right\}$$
(1)

 $y = x_1$

Where the nominal values of parameters are: $j_t = 0.03~kgm^2$ - Total inertia of the motor and load referred to the motor shaft, $q_m = 7.96 \times 10^{-7}~m^3/rad$ – volumetric displacement of the motor, $B_m = 1.1 \times 10^{-3}~Nms$ – viscous damping coefficient, $C_f = 0.104~$ -dimensionless internal friction coefficient, $V_O = 1.2 \times 10^{-4}~m^3~$ - average contained volume of each motor chamber, $B_e = 1.391 \times 10^9~pa~$ - effective bulk modulus, $C_d = 0.61~$ - discharge coefficient, $C_{im} = 1.69 \times 10^{-11}~m^3/pa.s~$ - internal or cross-port leakage coefficient of the motor, $P_S = 10^7~pa~$ - supply pressure, $\rho = 850~kg/m^3~$ - oil density, $T_r = 0.1~s~$ - valve time constant, - $k_r = 1.4 \times 10^{-4}~m^3/s.v~$ - valve gain, $k_a = 1.66^{-4}~m^2/s~$ - valve flow gain, $w = 8\pi \times 10^{-3}~m~$ - surface gradient.

The control objective is stabilization of any chosen operating point of the system. It is readily shown that equilibrium points of system are given by:

 X_{1N} : Arbitrary constant value of our choice

$$X_{2N} = \frac{1}{q_m} \left\{ B_m x_{1N} + q_m c_f p_s \right\}$$

$$X_{3N} = \frac{q_m x_{1N} + c_{im} x_{2N}}{c_d w \sqrt{\frac{1}{\rho} (p_s - x_{2N})}}$$
(2)

With very simple linearization we can find out that the system is minimum phase which allows application of many different design tools. In [14] Alleyne and Liu developed a control strategy that guarantees global stability of nonlinear, minimum phase single-input single-output (SISO) systems in the strict feedback form by using a passivity approach and they later used this strategy to control the pressure of an EHSS.

NEURAL-ADAPTIVE CONTROLLER

The In this study it was tried to design a velocity controller for electrohydraulic servo system which is adaptive based on feedback linearization controller. This controller, as shown in figure 3, consists of four parts: linear feedback controller, a nonlinear feedback linearization controller, an adaptive neural network controller and a neural network identifier. The total control signal is computed as follows:

$$u(t) = u_{pid} + m(t)u_{bk} + (1 - m(t))u_{ad}$$

III.

Where u_{pid} is the linear feedback control, u_{ad} is the adaptive neural network control and u_{bk} is the feedback linearization control. The function m(t) allows a smooth transition between the feedback linearization and adaptive neural network controllers, based on the location of the system state:

$$\begin{cases} m(t) = 0 \quad x(t) \in A_d \\ 0 < m(t) < 1 \quad otherwise \\ m(t) = 1 \quad x(t) \in A_c \end{cases}$$
(4)

Where the regions might be defined as in Fig.2.



Fig. 2. Membership functions

The feedback linearization controller is used to keep the system state in a region where the neural network can be accurately trained to achieve optimal control. The linear feedback controller is turned on (and the neural controllers is turned off) whenever the system drifts outside this region. The combination of controllers produces a stable system which adapts to optimize performance.

It should be noted that this neural controller and neural identifier uses the radial basis neural network. The linear feedback control is PID controller and the feedback linearization control is input-output controller.



Fig. 3. block diagram of the Neural – Adaptive Controller

A. RBF neural network

In this study, we use a type of neural networks which is called the radial basis function (RBF) networks. These networks have the advantage of being much simpler than the Perceptrons while keeping the major property of universal approximation of functions[15]. RBF networks are embedded in a two layer neural networks, where each hidden unit implements a radial activated function. The output units implemented a weighted sum of hidden unit outputs.

(3)

The input to a RBF network is nonlinear while the output is linear. Their excellent approximation capabilities have been studied in [16]. The output of the first layer for a RBF network is:

$$\emptyset_{i}(x) = \exp(-\frac{\|x - c_{i}\|^{2}}{2\delta_{i}^{2}}), i = 1, 2, ..., n.$$
(5)

The output of the linear layer is:

$$y_{i} = \sum_{i=1}^{n} w_{ji} \mathcal{O}_{i}(x) = w_{j}^{T} \mathcal{O}, j = 1, 2, ..., n.$$
(6)

Where $x \in \mathbb{R}^n$ and $y \in \mathbb{R}^m$ are input vector and output vector of the network, respectively, and $\mathcal{Q} = [\mathcal{Q}_1, \dots, \mathcal{Q}_n]^T$ is the hidden output vector, n is the number of hidden neurons, $w = [w_{j1}, \dots, w_{jn}]^T$ is the weights vector of the network, parameters c_i and δ_i are centers and radii of the basic functions, respectively. The adjustable parameters of RBF networks are w, c_i and δ_i . Since the network's output is linear in the weights, these weights can be established by least square methods. The adaptation of the RBF parameters c_i and δ_i is a non-linear optimization problem that can be solved by gradient-descent method.

B. RBF Identifier for EHSS

The output RBF1 neural network variable, (u) will be used as the signal-input for establishing a RBF2 neural network model to calculate the identifier law, \tilde{z}_1 . The output of the identifier based on RBF2 networks is:

$$\tilde{z}_{1} = \sum_{i=1}^{n} v_{i} \exp(-\frac{\left\|u - M_{i}\right\|^{2}}{2\theta_{i}^{2}}) = v^{T}Q, i = 1, 2, ..., n.$$
(7)

Where n is the number of hidden layer neurons, parameters M_i and θ_i are centers and radii of the basic functions and \tilde{z}_1 is the final closed-loop identifier input signal.

$$z_1 = x_1 - x_{1d}$$

$$E = (z - \tilde{z})^2$$
(8)

$$E = (z_1 - \tilde{z}_1)^2$$

Updated equation of the weighting parameters is:

$$v_{new} = v_{old} - \eta_2 \frac{\partial E^2}{\partial v}$$

$$v_{new} = v_{old} - 2\eta_2 \frac{\partial E}{\partial v}$$
(10)

$$\frac{\partial E}{\partial v} = \frac{\partial \tilde{z}_1}{\partial v} = Q \tag{11}$$

Finally we can find updating rule as follow:

$$v_{new} = v_{old} + 2\eta_2 EQ$$
(12)

C. RBF controller for EHSS

The error variable, (e) will be used as the single-input signal for establishing a RBF1 neural network model to calculate the control law, u. Then for the single-input and single-output case in this paper, the output of the controller based on RBF1 networks is:

 $\langle 0 \rangle$

$$u = \sum_{i=1}^{n} w_i \exp(-\frac{\|e - c_i\|^2}{2\delta_i^2}) = w^T \emptyset, i = 1, 2, ..., n$$
⁽¹³⁾

Where n is the number of hidden layer neurons and u is the final closed-loop control input signal. Updated equation of the weighting parameters is:

$$w_{new} = w_{old} - \eta_1 \frac{\partial e^2}{\partial w}$$
(14)

$$w_{new} = w_{old} - 2\eta_1 e \frac{\partial e}{\partial w}$$
(15)

$$\frac{\partial e}{\partial w} = \frac{\partial z_1}{\partial w} = \frac{\partial z_1}{\partial u} \times \frac{\partial u}{\partial w}$$
(16)

$$\frac{\partial z_1}{\partial u} = \frac{\partial \tilde{z}_1}{\partial u} \tag{17}$$

$$\frac{\partial \tilde{z}_1}{\partial u} = \frac{\partial \tilde{z}_1}{\partial Q} \times \frac{\partial Q}{\partial u}$$
(18)

$$\frac{\partial \tilde{z}_1}{\partial u} = -2v \frac{u-M}{\theta^2} Q \tag{19}$$

$$\frac{\partial u}{\partial w} = \emptyset$$
(20)

Finally we can find updating rule as follow:

$$w_{new} = w_{old} + 4\eta_1 \times e \times Q \times \emptyset \frac{u - M}{\theta^2}$$
(21)

D. PID controller for EHSS

PID controllers are used in industrial control systems vast because they have a few parameters which need to be adjusted its parameters includes control signals which are proper with error between reference and real output (p), Integral and differential of error (I) and (D).

$$u(t) = k_p \left(e(t) + \frac{1}{T_i} \int_0^t e(\tau) d(\tau) + T_d \frac{d}{dt} e(t) \right)$$
(22)

Which u(t) and e(t) are control signals and error. k_p , T_i and T_d are parameters should be adjusted. Transfer function equation 2 as follow:

$$u(s) = k_p \left(1 + \frac{1}{T_i s} + T_d s \right)$$
⁽²³⁾

The main characteristics of PID controllers are their capacity to remove stable state error in response to step input (because of Integration factor) and predict the output variance (if differential factor is used).

IV. SIMULATION RESULTS

In this section, the results of simulation are shown. The parameters of the PID controller are chosen $k_{i}, k_{i}, \dots, k_{d}$ = 0.0217, 0.0405 = 14.05 × 10⁻⁴

such that
$$p^{\mu}$$
, r^{μ} and a^{μ} are 0.0317, 0.0405 and 4.05 × 10 respectively.
The Neural Adaptive controller has been compared with feedback linearization controller, back stepping and PID controller. They are show in figures (4, 5, 6, and 7). Figures (4, 5, 6, and 7) show the system output, the

signal controller and the system states without the presence of output noise. Figure 8 show the function m(t). To show the capabilities of the controller introduced in this paper, Gaussian noises with follow property have been applied to the aimed system.

 $0.01 \times N(0,1)$: *amp* = 0.01, *vae* = 1, *avr* = 0

 $0.1 \times N(0,1)$: *amp* = 0.1, *vae* = 1, *avr* = 0

 $1 \times N(0,1)$: *amp* = 1, *va*1 = 1, *avr* = 0

Figures (9, 10, and 11) show the results of the experiment with the presence of output Gaussian noise.



Fig. 4. Simulation result x_1 without output noise for $x_{1n} = 200 rad / s$



Fig. 5. Simulation result x_2 without output noise for $x_{2n} = 1.3 \times 10^6 pa$



Fig. 6. Simulation result x_3 without output noise for $x_{3n} = 1.17 \times 10^{-4} m$





Results show that Neural Adaptive controller delivers the Hydro motor angular velocity to the desired velocity much more quickly than feedback linearization, back stepping and PID controllers and has shorter settling time than other controllers also show that in presence output noise Neural Adaptive controller is robust controller. In table I we compare Neural Adaptive based on feedback linearization controller result with other controllers.

Number	Controller	Maximum signal control (volt)	Settling time (SEC)
1	Neural Adaptive based on feedback linearization [purpose]	1.4	0.5
2	PID[4]	-10	3
3	FEL[17]	2.5	2.5
4	Neural Networks[5]	5	6
5	Feedback Linearization[3]	1.5	7
6	Back Stepping[3]	1.4	7
7	PDC[17]	3.5	3
8	Mamdani Fuzzy[4]	1.4	11
9	Neural Fuzzy[4]	30	4

Table I. Comparison results controllers

Table I show that Neural Adaptive based on feedback linearization controller has shorter settling time than other controllers and it has less Maximum signal control competed with other controllers.

V. **CONCLUSIONS**

This paper introduced Neural Adaptive based on feedback linearization method for control and identification of electrohydraulic servo system which has practical uses in many industrial systems.

In this paper, a Neural Adaptive control method for EHSS is proposed, which consists of four parts: the linear feedback controller, the feedback linearization control, the neural network controller and the neural network identifier. It should be noted that the linear feedback controller is PID controller type and this neural controller and neural identifier used the radial basis function (RBF) network controller and the radial basis function (RBF) network identifier. The radial basis output is a linear function of the network weights, which allows faster training and simpler analysis than is possible with multilayer networks. Neural Adaptive controller is designed for stabilization of EHSS system to the desired point in the state space. Results obtained from the simulation show the superiority of the control system suggested in this paper. Neural Adaptive controller has shorter settling time than other controllers. It is also robust in presence of output noise applied to the aimed system.

REFERENCES

- [1] Z. Jianhui and C. Sigin, "Modeling and simulation for application of electromagnetic linear actuator direct drive electro-hydraulic servo system," in Power and Energy (PECon), 2012 IEEE International Conference on, 2012, pp. 430-434.
- [2] P. N. Pham, K. Ito, and S. Ikeo, "The application of simple adaptive control for simulated water hydraulic servo motor system," in Industrial Technology (ICIT), 2013 IEEE International Conference on, 2013, pp. 204-209.
- M. Jovanovic, "Nonlinear control of an electrohydraulic velocity servosystem," in American Control Conference, 2002. [3] Proceedings of the 2002, 2002, pp. 588-593 vol.1.
- S. A. Mohseni, M. Aliyari, and M. Teshnehlab, "EHSS Velocity Control by Fuzzy Neural Networks," in Fuzzy Information [4] Processing Society, 2007. NAFIPS '07. Annual Meeting of the North American, 2007, pp. 13-18.

- [5] H. Azimian, R. Adlgostar, and M. Teshnehlab, "Velocity control of an electro hydraulic servomotor by neural networks," in Physics and Control, 2005. Proceedings. 2005 International Conference, 2005, pp. 677-682.
- [6] M. A. Shoorehdeli, H. A. Shoorehdeli, M. Teshnehlab, and J. Yazdanpanah, "Velocity Control of an Electro Hydraulic Servosystem," in Networking, Sensing and Control, 2006. ICNSC '06. Proceedings of the 2006 IEEE International Conference on, 2006, pp. 985-988.
- [7] F. Poloei, M. Zekri, and M. Aliyari Shoorehdeli, "Fuzzy-LQR hybrid control of an electro hydraulic velocity servo system," in Hybrid Intelligent Systems (HIS), 2011 11th International Conference on, 2011, pp. 5-9.
- [8] A. C. Aras, E. Kayacan, Y. Oniz, O. Kaynak, and R. Abiyev, "An adaptive neuro-fuzzy architecture for intelligent control of a servo system and its experimental evaluation," in Industrial Electronics (ISIE), 2010 IEEE International Symposium on, 2010, pp. 68-73.
- [9] J. Tai and X. Zhao, "Simulation study on the electrohydraulic servo system based on the fuzzy control algorithm," in Informatics in Control, Automation and Robotics (CAR), 2010 2nd International Asia Conference on, 2010, pp. 218-221.
- [10] L. Manlin, L. Guanghua, C. Shuangqiao, and F. Yongling, "ADR algorithm applied in electro-hydraulic servo system," in Electronic and Mechanical Engineering and Information Technology (EMEIT), 2011 International Conference on, 2011, pp. 1888-1891.
- [11] H.-y. Yu and L.-p. Shi, "The study of tracking control of electro-hydraulic servo system with feed forward and fuzzy-integrate control," in Electronic and Mechanical Engineering and Information Technology (EMEIT), 2011 International Conference on, 2011, pp. 4409-4412.
- [12] I. C. Yeh, Z. Xin-Ying, W. Chong, and H. Kuan-Chieh, "Radial basis function networks with adjustable kernel shape parameters," in Machine Learning and Cybernetics (ICMLC), 2010 International Conference on, 2010, pp. 1482-1485.
- [13] Z. A. S. Dashti, M. A. Shoorehdeli, M. Gholami, and M. Teshnehlab, "Neural Adaptive control for electro hydraulic servo system," in Control Conference (ASCC), 2013 9th Asian, 2013, pp. 1-6.
- [14] A. G. Alleyne and L. Rui, "Systematic control of a class of nonlinear systems with application to electrohydraulic cylinder pressure control," Control Systems Technology, IEEE Transactions on, vol. 8, pp. 623-634, 2000.
- [15] N. Jifu, "Conditions for radial basis function neural networks to universal approximation and numerical experiments," in Control and Decision Conference (CCDC), 2013 25th Chinese, 2013, pp. 2193-2197.
- [16] S.-F. Su, J.-T. Jeng, Y.-S. Liu, C.-C. Chuang, and I. J. Rudas, "Robust radial basis function networks based on least trimmed squares-support vector regression," in IFSA World Congress and NAFIPS Annual Meeting (IFSA/NAFIPS), 2013 Joint, 2013, pp. 1-6.
- [17] A. Zare and M. Aliyari, "Design Fuzzy Controller For Electro Hydraulic Servo System By Using LMI" presented at the 13th student college of Iranian confrences 2011.