

Closed Loop Analysis of Single-Inductor Dual-Output Buck Converters with Mix-Voltage Conversion

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Abstract: A single-inductor dual-output (SIDO) buck converter has recently found applications in hand-held battery-powered electronic devices. The circuit operation and the functional interdependencies among basic converter parameters such as dc voltage gains, transistor duty cycles, and load current levels are much more complicated than those of the single-output counterpart. In this project, a rigorous analysis was conducted to develop dc equations in steady state operation for SIDO converters. More importantly, from the analysis results, a possibility of a new mode of operation, dubbed “mix-voltage” operation, will be pointed out. In the so-called “mix-voltage” operation, the converter is capable of working even when the input voltage is lower than one of the two output voltages. In the past, a SIDO buck converter has been used for providing “pure-buck” outputs, i.e., both output voltages are lower than the input voltage. Therefore, this possibility not only opens up new applications but also extends the operating battery range in existing applications. Experimental results confirmed the dc equations and the “mix-voltage” conversion of SIDO buck converters.

Keywords- DC Power converters, mix-voltage conversion, single inductor dual output (SIDO).

I. Introduction

A single-inductor dual-output buck converter has recently found applications in hand-held battery-powered electronic devices, which require dual outputs but no electrical isolation. The main attraction of a SIDO lies in the fact that dual regulated outputs can be provided with relatively low cost and small size. Fig. 1 shows the power circuit diagram of a SIDO buck converter. The circuit diagram may look simple but the circuit operation and the functional interdependencies among basic converter parameters such as dc voltage gains, transistor duty cycles, and load current levels are much more complicated than the counterparts of a conventional single-output buck converter. In this paper, rigorous analysis in steady-state operation would be conducted to develop useful equations for design purposes. More importantly, from the analysis results, a possibility of a new mode of operation, “mix-voltage” operation would be pointed out.

In the so-called “mix-voltage” operation, the input voltage can be lower than one of the output voltages, as opposed to conventional “pure-buck” operation in which input voltage must be higher than both output voltages. This implies that the input battery may operate down to a voltage level lower than previously thought possible. This may also mean that single battery, instead of two in series, is sufficient in some applications. In the paper, a basic review of SIDO buck converter will be given first. Analytical equations relevant to continuous and discontinuous conduction mode, dc voltage gains, and duty cycles will be developed for both the “pure-buck” and the “mix-voltage” operations. An equation will also be derived to estimate whether a mix-voltage conversion is possible for given specifications. Since a SIDO buck converter is mostly used in low voltage applications, semiconductor switch conduction voltage drops will be included in the analysis for accuracy.

II. Literature Review

A basic review of SIDO buck converter will be given first. Analytical equations relevant to continuous and discontinuous conduction mode, dc voltage gains, and duty cycles will be developed for both the “pure-buck” and the “mix-voltage” operations. An equation will also be derived to estimate whether a mix-voltage conversion is possible for given specifications. Since a SIDO buck converter is mostly used in low voltage applications, semiconductor switch conduction voltage drops will be included in the analysis for accuracy. Experimental results will also be shown to validate the analytical results. Literature survey gives an overview about these proposed systems. These are the supporting papers of my work. This literature survey extracts information from some of the literature available on this subject. It does not claim to be complete nor does it take a position towards the opinions expressed in these concepts.

III. Operation of SIDO Buck Converter

A SIDO buck converter can be operated in both the continuous conduction mode and discontinuous conduction mode just like a conventional single-output buck converter. Fig. 2 shows the waveforms of the inductor current and transistor duty cycles with a time multiplexing control scheme for both the CCM and DCM

operations. According to the relative magnitude of transistor Q_1 duty cycle D_1 and transistor Q_2 duty cycle D_2 , the waveforms are given for three cases: Case A ($D_1 < D_2$), Case B ($D_1 = D_2$), and Case C ($D_1 > D_2$). In the CCM operation, there are three periods: T_1 is the duration when both transistors Q_1 and Q_2 are ON. During this period, diodes D_a and D_b are OFF and the power is provided to V_{O1} only. The period T_2 is the period when only one of the transistors is in conduction. If Q_1 , instead of Q_2 , is in conduction, then the inductor current flows through D_b and the power is provided to V_{O2} only. Otherwise, it flows through D_a and the power is provided to V_{O1} only. The period T_3 is the period when both transistors are OFF. The inductor current is then flowing through D_a and D_b , and the power is provided only to V_{O2} . Notice that D_1 is, therefore, equal to T_1/T_S or $(T_2 + T_2)/T_S$, where T_S is the conversion switching period, depending upon whether it is Case A, B, or C. The same situation applies to D_2 . It is also clear that there is no T_2 period for Case B. All of these are shown along with the waveforms in Fig. 2. For the DCM operation, there is an additional period T_d when the inductor current stays at zero and none of the switches is on. The duty cycle D_d is defined as T_d/T_S .

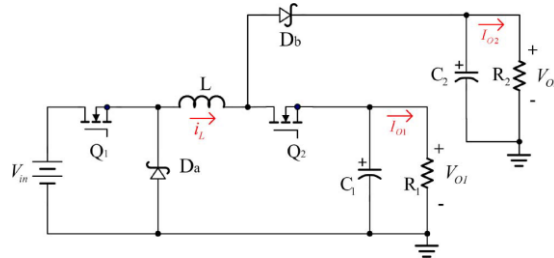


Fig.1 SIDO buck converter circuit diagram

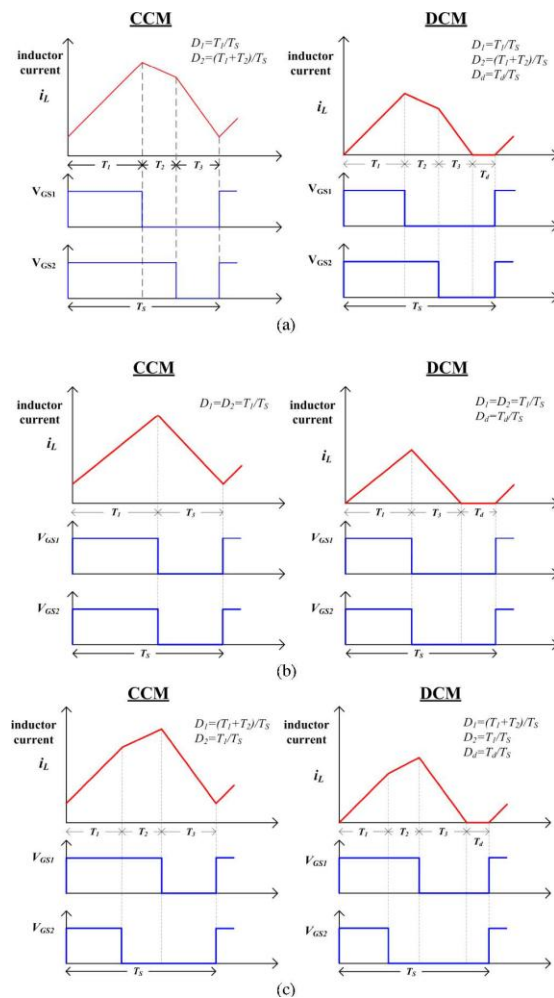


Fig.2 Operating waveforms of a SIDO buck converter

IV. SIDO Buck Converter Dc Equations

In this section, dc equations of the SIDO converters in steady state operation will be derived. The derivation starts with an inductor current waveform that varies according to the case of converter operation described in Section II. Only Case A will be used as an example for detailed derivation. As mentioned earlier, semiconductor switch conduction voltage drops will be included in the derivation. From the waveform, the input average current I_{in} is the average of the $Q1$ current, i.e., the area below the inductor current waveform during the $T1$ period divided by the total period T_s . This leads to (1). Similarly, (2) can be obtained by equating the output current I_{O1} to the average of the inductor current of the $Q2$ current. And (3) can be obtained by equating the output current I_{O2} to the average of the D_b current. In the equations, V_{in} is the input voltage, V_D and V_{DS} are, respectively, the conduction voltage drops of diodes and transistors, and V_{O1} and V_{O2} are the output voltages. I_X is the valley of the inductor current as shown in Fig. 3, and T_s is the conversion switching period.

$$I_{in} = T_s/2L (V_{in} - 2V_{DS} - V_{O1}) D_{21} + I_X D_1 \quad (1)$$

$$I_{O1} = T_s/2L [V_{in} D_1 (2D_2 - D_1) - V_{O1} D_2^2 + V_{DS}(D_1^2 - 2D_1 D_2^2) - V_D(D_2 - D_1)^2] + I_X D_2 \quad (2)$$

$$I_{O2} = T_s/2L (V_{O2} + 2V_D) (1 - D_2^2) + I_X (1 - D_2) \quad (3)$$

$$V_{in} I_{in} = V_{O1} I_{O1} + V_{O2} I_{O2} + V_{DS}(I_{in} + I_{O1}) + V_D (2I_{O2} + I_{O1} - I_{in}). \quad (4)$$

Using the principle of conservation of energy, (4) can be obtained, where the left-hand side is the total input power, the first two terms of the right-hand side represent the total output power, and the remaining two terms are the power losses of the MOSFET and diode switches. From the four simultaneous equations (1)–(4), the two variables I_X and I_{in} can be eliminated. Two independent equations remain. These two independent equations can be simplified further using (5), which can be obtained from a consideration of the inductor volt-second balance in the steady state.

$$(V_{in} - V_{O1} - 2V_{DS})D_1 = (V_{O1} + V_{DS} + V_D) (D_2 - D_1) + (V_{O2} + 2V_D)(1 - D_2) \quad (5)$$

DC equations for Case A of CCM can then be obtained as (6) and (7). Group I in CCM consists of variables V_{O1} , V_{O2} , D_1 , and D_2 ; Group II consists of converter component values V_D , V_{DS} , and L ; and Group III consists of converter operating conditions T_s , I_{O1} , I_{O2} , and V_{in} . Normally, the values of the latter two groups are given. The values D_1 and D_2 can then be found by solving the two simultaneous (6) and (7), if the values of V_{O1} and V_{O2} are specified. On the other hand, the values V_{O1} and V_{O2} can be found by solving the same set of equations, if the values D_1 and D_2 are specified. The DC equations for the other two Cases of CCM operation can be obtained in a similar fashion. It should be pointed out that besides the equation complexity, the voltage gains in a SIDO converter depend not only on duty cycles but also on inductor value, load currents, and switching period.

Table I
Dc Equations of A SIDO Buck Converter in CCM

Case	DC equations in CCM
Case A ($D_1 < D_2$) or Case B ($D_1 = D_2$)	$I_{O1} = \frac{[I_{O1}(V_{in} + V_{DS} + V_D) + I_{O2}(V_{O1} + 2V_{DS})]D_1}{(V_{in} - V_{DS} + V_D)D_1} + \frac{I_s}{2L} (V_{O1} + 2V_{DS})(1 - D_1)(D_2 - D_1) \quad (6)$ $I_{O2} = \frac{[I_{O1}(V_{in} + V_{DS} + V_D) + I_{O2}(V_{O1} + 2V_{DS})](1 - D_2)}{(V_{in} - V_{DS} + V_D)D_1} - \frac{I_s}{2L} (V_{in} + V_{DS} + V_D)(1 - D_2)(D_2 - D_1) \quad (7)$
Case C ($D_1 > D_2$)	$I_{O1} = \frac{[I_{O1}(V_{in} + V_{DS} + V_D) + I_{O2}(V_{O1} + 2V_{DS})]D_2}{(V_{in} - V_{DS} + V_D)D_1} - \frac{I_s}{2L} (V_{O1} + 2V_{DS})(1 - D_1)(D_1 - D_2) \quad (8)$ $I_{O2} = \frac{[I_{O1}(V_{in} + V_{DS} + V_D) + I_{O2}(V_{O1} + 2V_{DS})](1 - D_2)}{(V_{in} - V_{DS} + V_D)D_1} + \frac{I_s}{2L} (V_{in} + V_{DS} + V_D)(1 - D_2)(D_1 - D_2) \quad (9)$

The DC equations of a SIDO converter in DCM operation will be derived as follows. Compared to a CCM operation, there are two differences in writing the equations for DCM operation. First, I_X is zero and an additional variable, duty cycle D_d , is involved. Setting I_X equal to zero and including the variable D_d in (2) and (3) leads, respectively, to (10) and (11). From the consideration of the inductor volt second balance in the steady-state DCM operation, (12) can be obtained.

TABLE II: DC EQUATIONS OF A SIDO BUCK CONVERTER IN DCM

Case	DC equations in DCM
Case A ($D_1 < D_2$)	$I_{O1} = \frac{T_s}{2L} [(V_{in} + V_D - V_{DS})(2D_2 - D_1)D_1 - (V_{O1} + V_{DS} + V_D)D_2^2]$ (10)
or	$I_{O2} = \frac{T_s}{2L} (V_{O2} + 2V_D)(1 - D_2 - D_1)^2$ (11)
Case B ($D_1 = D_2$)	$(V_{in} - V_{O1} - 2V_{DS}) \cdot D_1 = (V_{O1} + V_{DS} + V_D)(D_2 - D_1) - (V_{O2} + 2V_D)(1 - D_2 - D_1)$ (12)
	$I_{O1} = \frac{T_s}{2L} (V_{in} - V_{O1} - 2V_{DS})D_2^2$ (13)
Case C ($D_1 > D_2$)	$I_{O2} = \frac{T_s}{2L} [(V_{O2} + 2V_D)(1 - D_2 - D_1)^2 - (V_{in} + V_D - V_{DS})(D_1 - D_2)^2]$ (14)
	$1 - D_2 = \frac{(V_{in} + V_D - V_{DS})D_1 + (V_{O2} + V_D - V_{DS} - V_{DS})D_2}{V_{O2} + 2V_D}$ (15)

V. Mix-Voltage Conversion for SIDO Buck Converter

Three examples will be given. From the results, one can also see if “mix-voltage” conversion is possible for the specifications.

Example 1: Converter specifications are given in the following. $V_{O1} = 1.8V$, $V_{O2} = 3.3V$, $I_{O1} = 500mA$, $I_{O2} = 200mA$, $L = 10 \mu H$, $V_{DS} = 0.01 V$, $V_D = 0.4 V$, and $T_S = 5 \mu s$. The maximum input voltage $V_{in \max} = 5 V$. Find the duty cycle information and the minimum operable input voltage $V_{in \min}$. *Step 1:* V_{in} is first set at 5 V and proceeded as follows: Two sets of solutions are obtained using (13)–(15). $(D_1, D_2, D_d) = \{(-0.6763, -0.7931, 2.255)$ and $(0.6763, 0.7931, -0.2546)\}$. MATHCAD software was used for solving the simultaneous equations. *Step 2:* Since D_d is outside the range of $[0, 1]$ for both solutions, the converter works in CCM; therefore, go to Step C3. *Step C3:* One set of solution is obtained $(D_1, D_2) = (0.5335, 0.6478)$ using (8) and (9). *Step C4:* D_1 and D_2 stay within boundary. *Step C5:* Need to check if $D_1 > D_2$. It turns out D_1 is less than D_2 . This means the assumption in Step C3 and the equation used to obtain D_1 and D_2 were incorrect. Therefore, go to Step C7. The duty cycles need to be recalculated. *Step C7:* Solving for D_1 and D_2 using (6) and (7). $(D_1, D_2) = (0.5268, 0.6670)$. The data given earlier were obtained for $V_{in} = 5V$. For each selected V_{in} value, the operating duty cycle values can be found as described earlier. It turns out that the converter operates in the CCM for the entire input range. As V_{in} is decreased, the D_1 curve intersects with the $D_1 = 1$ line at $V_{in \min}$. This crossover point is the minimum input voltage that the converter specifications can still be met by the converter because D_1 must be no more than unity. From the figure, $V_{in \min}$ is about 2.36 V, which lies between V_{O1} and V_{O2} . So, mix-voltage conversion exists in this example. This example shows that the converter is capable of operating even when the input battery voltage is well below V_{O2} value of 3.3 V.

Example 2: The converter specifications are the same as those of Example 1 with the exception of the load current values: $I_{O1} = 100 mA$ and $I_{O2} = 500 mA$. In this case, the converter operates in the CCM also for the entire input voltage range. However, $V_{in \min}$ is greater than both output voltages, which implies that mix-voltage conversion is not possible.

Example 3: The converter specifications are the same as those of Example 1 except that the load current levels are smaller: $I_{O1} = 50mA$ and $I_{O2} = 20mA$. By applying the same procedure, it was found that this is a DCM case.

VI. CONCLUSION

A SIDO buck converter was analyzed for steady-state operation. The various operating modes were explored and design equations were developed. These equations allow the designer to find out intricate relationships among output voltages, transistor duty cycles, and output currents. From the results, a mix-voltage operation was pointed out and demonstrated. This new mode of operation opens up new applications and may also extend the input battery operable range for existing applications.

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