Volatility in Indian Stock Market: A study to assess volatility, persistence and GARCH effects.

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Abstract: This paper examines stock market volatility in India choosing S&P BSE Sensex as the market. Daily closing prices of S&P Sensex for 3740 days over the period 2000-14 were used in the study. The study finds that using absolute change in the Sensex or stock price to measure volatility is deceptive. Only large percentage change in price need be taken as the stock volatility. Though standard deviation is generally used as a measure of volatility, it fails in circumstances of time-varying scedasticity. Time-adjusted standard deviation as a measure of volatility resembles with the standard deviation without time-adjustment. Both measures indicates only a moderate volatility in India lower than the volatility prevailed upon during the Great Depression of 1929 and the Great market Crash of 1987. The study found a strong relationship between volatility and summed daily returns. The empirical analysis also results in the finding of evidences of volatility clustering and moderate volatility persistence when GARCH (1,1) model is applied. Key words: Absolute, Clustering, Depression, Persistence, Scedasticity.

I. Introduction

After the global recession which erupted in 2007, almost all countries felt its ripples in a level unheard before. Stock market volatility was frequent and overwhelming which significantly affected investor confidence all over the world. Press media vehemently propagated the intensity of the volatility of the market by observing the daily stock price or index difference. Indian stock market was one of the few markets stood relentless or less affected by the recessionary waves which rocked the whole world. It does not mean that Indian stock market is insensitive to the global recession. It only means that the Indian stock market shows volatility in stock prices at a lesser degree than the other countries. Whether the volatility is high or low, the investors and the public generally view it as a menace. It is interesting to study the volatility features of Indian stock market over years to determine whether the market is stable and secured for investment.

A volatile market cannot be considered as a safe haven for investment. When a market is volatile there will be uncertainty as to the price and return from securities. In fact, volatility is a creation of uncertainty. Under such circumstances investors lose confidence in market and like to keep off. As a strategy they will dispose of their holdings at the current price to minimize losses. This attitude of stock holders will push the market down. Thus volatility brings uncertainty and uncertainty in its turn creates panic to further volatility. The forces that pave the way for volatility act and react with each other so as to perpetuate volatility in market for ever.

Volatility arises when current stock price differs from the previous. It is the variation of the current price from the expected past average price of a stock. Volatility is the dispersion of current stock price from the expected price. Volatility can be measured by using the statistic standard deviation. When the standard deviation is high volatility is said to be high and vice versa. Volatility, as a matter of fact, is the reason for returns from investment. Stock return is nothing but the difference between the current price and previous day’s price. If the current price is higher than the previous day’s price there is return. If the previous day’s price higher than the current price then the stock is at a loss. Loss or gain, it is an offshoot of volatility. Therefore volatility that brings return to investor is prospective, but volatility that engenders loss is a doom. As such volatility is good when the market is going up while it is bad when the market is down.

Terminng absolute change in price as volatility is undesirable. It may lead to fallacious conclusions. Every change in price cannot be considered as volatility. Only a large percentage change in price can be treated as volatility. Percentage change in price is calculated as follows: Percentage change in price \( = \frac{P_t-P_{t-1}}{P_{t-1}} \times 100 \)
Where \( P_t \) is the current price and \( P_{t-1} \) is the previous day’s price.

Volatility occurs when there is large change in prices. Change in price which is called volatility happens when new information reaches the market. Whenever information reaches the market investors respond towards it by way of maintaining a long or short position. Long position results in the purchase of stocks and short position in the disposal of stocks already held. This response from the investors either push or pull the price prompting a change in price. The new information that reaches the market may be micro or macro. Such information will be significant as to future profitability of the stocks. These information which necessitate a
price change are called shocks or surprises. Presently market is fully equipped to capture all information related to the stocks due to the advancement of information technology. There is no time-lag in getting information and processing the same due to IT revolution. The number and frequency of information are aplenty and responses are accordingly immanent and instantawing to the presence of advanced financial services and liquidity provided by the financial institutions in the market.

Investors perceive volatility as a risk of investment. Investors are inherently risk-averse. If the market is volatile investments get shy. Investors always envisage a stable market without much volatility. It should be possible to (a) measure and estimate volatility and (b) predict volatility to build investor-confidence in the market. One important method of measuring volatility is using standard deviation. Standard deviation represents dispersion from the mean. Accordingly a greater standard deviation tells a greater volatility and a lower standard deviation about a lower volatility.

Volatility is to be seen as a risk related to stock investment. Greater the volatility of stock market, greater will be the market risk. When the risk is high stock price tends to fall. Therefore volatility in an upmarket does less harm than in a down market. If volatility can be predicted investors will be able to plan their investment accordingly. Estimation of volatility on the basis of historical data will tell only the volatility of the past. Future investments require future volatility that is for the t+1 period. Standard deviation as a measure of volatility is useful to estimate only the past volatility.

Prediction of volatility is a subject of controversy over years. Financial economists have difference of views as to the predictability of stock volatility. Those who follow Efficient Market Hypothesis (EMH) maintain that market is efficient, returns from stocks are normally distributed, returns series are uncorrelated and variation in price is caused by new information. The new information may be of anything which affect the profitability of the stocks concerned such as declaration of dividend, quarterly results of the company, change in the industrial policy, change in the repo rate and so on. When new information reaches, the market will, then and there, assimilates the news making necessary adjustment to the stock price and reflect it immediately in no time. If there is no new information stock price remains unchanged. Stock price changes due to the flow of new information. New information occurs as a surprise since it is totally unknown. The information that brings change to the price is stochastically unknown, identically and independently distributed (iid), statistically white noise with the property of N(0,1) denoting normal distribution having zero mean and unit variance. Therefore, the protagonists of EMH deny the predictability of stock volatility.

But EMH content of efficient market has been seriously challenged by many studies of recent periods. The assumption of normal distribution of equity returns is found fluid. Many recent researches reveal that equity returns of time-varying nature are distributed non-normally. Such distributions were found to be having high positive or negative skewness and excess kurtosis. Moreover return series were seen serially correlated indicating dependence between t and t-1 outcomes. It all confirms that the empirical findings do not support EMH view.

Hence, under non-normal environment surprises cannot be considered absolutely random though a stochastic element is there in such surprises. An important element that determines the future volatility is apart from surprises is the past volatility. Current volatility is supposed to be springing from the immediate past. Today’s volatility is depending upon yesterday’s volatility. Or volatility at t period is conditional upon t-1 period. Engel’s ARCH [1] and Bollerslev’s [2] GARCH (1, 1) models strive to predict future volatility wherever the volatility is found conditional and heteroscedastic.

Volatility is usually expressed as variance from the expected value. Variance statistically is the square of standard deviation. If standard deviation can be denoted by sigma (σ), then, variance is σ². Under normal condition variance will be stable, can be plotted as a straight line parallel to X axis. It can also be called as long run variance or volatility. But conditional variance vary at times. Conditional variance sometimes vary at constant rates calls homoscedastic and sometimes vary differently at different times called heteroscedastic.

This paper is intended to study stock market volatility in Indian stock market over 15 years’ daily data. The remaining part of the paper is organized in such way that section 2 will deal with the review of literature, section 3 relates to the statement of objectives of the study, section 4 deals with the data and methodology, section 5 states the empirical test made in the study, section 6 is concerned with the empirical analysis and section 7 relates to summary and conclusions.

**II. Review of literature**

In this section an attempt is made to review other research works related to market volatility relevant to this study. Tagliafichi Ricardo A. [3] in a study to explore the possibility of finding an appropriate beta to set a best portfolio detects that the returns are not linear and not following the behavior of classical hypothesis applied to the capital market. He used non-linear models to assess the heteroscedasticity in pursuit for ascertaining best estimators to set right portfolio with maximum benefits and minimum variances.Tim Bollerslev [4] in his seminal work generalized the application of auto regressive conditional heteroscedasticity (ARCH)
introduced by Engels to bring past conditional variances to current conditional variance equation in order to set a new model called Generalized Auto Regressive Conditional heteroscedasticity (GARCH) to predict future volatility. Beta and other parameters are estimated with the help of the maximum likelihood function and concluding with an empirical example related to the uncertainty of inflation rate.

Timothy J. Brailsford [5] in a study examines the empirical relationship between the trade volume and returns and volatility. The study found evidence for supporting an asymmetric model for the purpose. The relationship between the price change and volume is found significant. There are evidences for supporting the hypothesis that the volume-price change slope for negative returns is less steep than the slope for positive returns. It confirms the asymmetric relationship between volume and price change. The study examined the trading volume in the context of conditional volatility using GARCH model and found a reduction in the significance and magnitude of GARCH coefficients, and reduction of persistence of variance. In this way the study finds that if trading volume is proxies for the rate of information arrival ARCH effects and persistence of variance can be explained.

Carla Inclan and George C. Tiao [6] in the article deals with the problem of multiple change points in the variance of a sequence of independent observations. The study proposes a procedure to detect variance based on an iterated cumulative sums of squares (ICSS) algorithm. The study claims that ICSS yield results without much computational burden compared to Bayesian approach or Maximum Likelihood function. Dima Alberg, Haim Shalit, and Rami Yosef [7] analyze empirically the mean return and conditional variance of Tel Aviv Stock Exchange indices by using various GARCH models. The paper compares the forecasting performances of several GARCH models and finds that EGARCH skewed student t model as the most promising for characterizing the dynamic behavior of returns Tel Aviv Stock Exchange indices because it reflects the underlying process in terms of serial correlation, asymmetric volatility clustering and leptokurtic innovation.

Kenneth R. French, G. William Schwert, and Robert F. Stambaugh [8] examine the relationship between stock returns and stock market volatility. The study finds evidence of positive relation between expected risk premium on stocks and the level of variability that can be predicted. The study also finds a strong negative relation between the unpredictable part of stock market volatility and excess holding period returns. Zsuzsanna Horvath and Ryan Johnston [9] in their paper examine the various attributes of a time series data for financial returns. In the study they were able to find stationarity and differencing in both the continuous and discrete series. The study recommends GARCH model as the best fit for analyzing variance of financial returns. Pankunni. V [10] examines the significance of beta and its impact on stock return with the 20 stocks of BSE India from the period 1999 to 2013. The study put to test the linearity between beta and equity returns and attempted to find whether the market price and value of stocks coincide. The study finds that there is significant relation between beta and equity returns. But the relationship cannot be exactly defined as linear. The t test, P values and R² tests employed in the study reject linearity between beta and returns and confirm non-linear elements in the equity returns series.

M. T. Raju, Anirban Ghosh [11] study stock market volatility of India as a comparison with other countries. The study finds that mature/developed markets provide a relatively high return with low volatility over long period. It also finds that only India and China among emerging countries provide high returns with low volatility. Indian market shows less skewness and kurtosis compared to the developed countries. G. William Schwert [12] states that stock market volatility is unusually low since 1987 stock market crash. In the paper Schwert compares volatility of returns to US stock indices at monthly, daily, and intraday intervals and shows the volatility of returns to stock indices by trade option contracts. Schwert also compares the volatility of US stock market returns with the volatility of returns of stock markets in the UK, Germany, Japan, Australia and Canada. The paper finds that the volatility has been very low in the decade since 1987 crash. Amita Batra [13] examines the time variation in volatility in Indian stock market during 1979-2003. The study focuses on whether there is any volatility persistence in Indian stock market on account of the process of liberalization in India. The paper examines shifts in volatility and the factors that cause shifts in volatility. The study finds that the most volatility period in India was during around the BOP crisis and the period of initialization of the process of liberalization. It also finds that stock return volatility in India was mostly due to internal reasons and not due to global reasons.

Debesh Bhowmik [14] evaluates the multidimensional framework of stock market volatility. The study finds that high indices of stock market implies less variability of volatility. The volatility caused by country’s depression or recession cannot be cured in the short-run. Stock market volatility has negative impact on the growth of the country that is high volatility reduces growth rate. High volatility also crosses boundaries to affect other countries. The negative impact of high volatility reduces volume of trade and increases current and capital account deficits. Giorgio De Santis and Selhattin Imrohoroglu [15] study the dynamic behavior of stock returns and volatility in emerging financial markets. The study finds strong evidence of predictable time-varying volatility in almost all countries. Changes in volatility are found persistent. Finds that investors are not rewarded for market wide risk. Fischer Black [16] examines the relationship between volatility and stock returns. The paper finds that the volatility in stock return is not at uniform rate but at varying rate. The volatility is highly
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dynamic and there is strong relationship between equity returns and change in volatility. Finding regression between equity returns and change in volatility it is possible to predict the change in volatility on the basis of the change in equity returns.

Reena Aggarwal, Carla Inclan and Ricardo Leal [17] discuss about the kind of events that cause shift in stock market volatility. The study collates large changes in volatility and the global and local events during the period of increased volatility. It finds that most events that affect shifts in volatility are local. Rob Reider [18] in the paper presents three objectives of volatility forecast. They are (1) risk management, (2) asset allocation, and (3) for taking bets on future volatility. The paper suggests that the simplest method for computing volatility is the historical standard deviation. But much improved methods of volatility forecasting like different GARCH models such as GARCH(1,1), EGARCH, IGARCH, and ARCH(1) can also be used for asymmetric situations. The paper presents a detailed analysis of the asymmetric GARCH models for volatility forecasting. George Tauchen[19] explores the relationship between volume and jumps in stock price. The study uses various jump tests developed by the financial economists and finds that stock prices composes of a geometric Brownian motion and a jump part. The study finds evidences towards jumps being a result of common knowledge shocks.

III. Statement of Objectives

This paper intends to study the following:
1. The volatility of Indian stock market
2. Volatility estimate and rate of change in volatility in Indian stock market
3. The relation between stock returns and volatility estimate and rate of change in volatility.
4. GARCH effects in Indian stock market.

IV. Data and Methodology

S&P BSE Sensex Index is selected to represent Indian stock market. Daily closing price of 3740 days’ Sensex index of S&P BSE has been collected for 15 years for the period from January 1, 2000 to December 31, 2014. Percentage change in price is calculated to study the daily volatility of stock prices. 25 highest one day increases and decreases are calculated. Summary statistics such as mean, standard deviation, skewness and kurtosis are ascertained. On the basis of percentage change and summary statistics, volatility condition of Indian stock market is studied.

The total period of observation over 15 years is divided into 180 intervals of 21 days in order to work out monthly standard deviation. Monthly standard deviations are multiplied by the square root of actual number of trading days to obtain time adjusted monthly standard deviation. 25 highest volatile days are located with time adjusted standard deviation.

The volatility estimate is worked out as follows: Daily returns are summed on monthly basis and then they are squared and multiplied with 252/21 to obtain annualized summed and squared returns. Volatility estimate is calculated by finding the root square of the annualized summed and squared returns.

Rate of change in volatility is worked out by finding the percentage change in volatility estimate. Rate of change in volatility is regressed with summed monthly returns to enable prediction of future change in volatility. GARCH (1, 1) model is applied to test volatility clustering and conditional heteroscedasticity. Volatility persistence is also estimated on the basis of the GARCH parameters.

V. Empirical Test

Stock volatility is understood as the large percentage change in prices. The volatility cannot be represented by a change in absolute quantity. Equation (1) can alternatively be stated as below.

\[
\text{Percentage change or daily variance} = \frac{P_t - P_{t-1}}{P_{t-1}} \times 100 \tag{2}
\]

Here, \(P_t\) is the current price, and \(P_{t-1}\) is the previous day’s price.

The larger the percentage change the larger the daily volatility. Usually standard deviation is used to measure stock volatility. Daily standard deviation can be calculated by using the equation:

\[
\sigma = \frac{\sum_{n=1}^{n} (y - \mu)^2}{n} \tag{3}
\]

Here, \(y\) is the daily percentage change, \(\mu\) is the average and \(n\) is the number of observation. When \(n\) becomes large \(\mu\) will be nearing zero and \(n\) always will be 1. Therefore \(y\) will become the daily variance.

25 highest single day increases and 25 highest single day decreases in the Sensex will tell the volatility situation of the stock market. The whole period of 15 years is divided into 180 intervals of 21 actual trading days and based on the daily returns standard deviation is calculated for each interval. Since each month has more or less 21 days of trading days, the intervals become monthly and standard deviation for the interval will be monthly standard deviation. Time-adjusted standard deviation is found by the following equation:

\[
\text{Time-adjusted standard deviation} = \sigma \sqrt{N} \tag{4}
\]
Where, $\sigma$ denotes standard deviation and $N$ denotes number of trading days in the interval.

In order to assess the volatility of Indian stock market based on the time adjusted standard deviation a comparison is made with the standard deviation during the Great World Depression of 1929 and the standard deviation of the Great Market Crash of 1987.

Volatility estimate and volatility change are assessed with the help of the method recommended by Fischer Black. Accordingly, volatility estimate is calculated through the following steps.

1) Daily returns are summed for the interval.
2) Summed daily returns are squared.
3) Summed daily returns squared are multiplied with 252/21 to annualize them.
4) Found the square root of the annualized summed daily returns.

The change in the volatility estimate is assessed as:

$$\text{Change in volatility} = \frac{\text{Current interval volatility} - \text{Previous interval volatility}}{\text{Previous interval volatility}}$$ (5)

Regressing the summed returns and volatility change, the constants and the coefficients are ascertained so as to understand the relationship between them.

The presence of heteroscedasticity is tested by the application of GARCH (1, 1) model.

GARCH (1, 1) model is defined below as

$$\varepsilon_t = z_t \sigma_t$$

$$\sigma_t^2 = \omega + \sum_{i=1}^{q} a_i \varepsilon_{t-i}^2 + \sum_{j=1}^{p} b_j \sigma_{t-j}^2$$ (6)

Where, $a_i, b_j > 0, \sigma_t > 0$

$$a_1 + b_1 < 1$$

GARCH (1, 1) model has two equations. They are (1) Mean equation and (2) Variance equation.

Mean Equation:

$$Y_t = \alpha_0 + \beta Y_{t-1} + \varepsilon_t$$ (7)

Variance Equation:

$$\sigma_t^2 = \omega + a_1 \varepsilon_{t-1}^2 + b_1 \sigma_{t-1}^2$$ (8)

Here, $\varepsilon_{t-1}^2$ denotes Residual Square of the previous day, $\sigma_{t-1}^2$ represents variance of the residuals for the previous day, and $\sigma^2$ shows the conditional variance of current period $t$. $\omega$ is the long run variance. $a_1$, and $b_1$ are coefficients of $\varepsilon_{t-1}^2$ and $\sigma_{t-1}^2$, respectively.

Mean equation is solved by applying Ordinary Least Square (OLS) and residuals are obtained. Residuals are put to test for the volatility clustering and heteroscedasticity. The test is organized to perceive whether high volatility is followed by high volatility for a prolonged period and low volatility is followed by low volatility for a prolonged period. If it happens so, then, volatility is said to be subject to clustering and showing signs of heteroscedasticity. Parameters are subject to non-negativity conditions. The sum of $\omega$, $a_1$, and $b_1$ are supposed to be equal to 1.

VI. Empirical Analysis

This paper estimates stock market volatility in India based on 3740 days daily data of BSE Sensex comprising a period of 15 years from 2000 to 2014. Though numerous methods are available for ascertaining volatility, none can be considered as perfect. Large percentage change in price is generally perceived as volatility. The statistical tool Standard Deviation denoted by the Greek letter $\sigma$ (sigma) is in use in the academic circle to measure stock volatility. Time-adjusted standard deviation is also in use to relate the volatility with time. Fischer Black has introduced a method for predicting future volatility and rate of change in future volatility. Under conditions of conditional heteroscedasticity, Generalized Auto Regressive Conditional Heteroscedastic (GARCH) method is successful in ascertaining stock market volatility.

In this paper, Stock market volatility is assessed in the following ways:

1) Large Percentage change in Price
2) Using Standard deviation
3) Using time-adjusted standard deviation
4) Fischer Black’s method of volatility estimate and Change in volatility estimate.
5) GARCH (1, 1) Model.

6.1. Volatility as a large percentage change in return or price.

When volatility is referred, media and the public usually get sensitive and count on the big quantitative change in prices as stock volatility. The change in price in absolute terms does mark volatility in general way but it does not mark the magnitude of volatility. The change with reference to the point of change is to be reckoned up to know the volatility. Therefore percentage change in price has to be considered as the measure of volatility rather than the absolute change in price. Change in absolute term is elusive and may lead to wrong direction. But people usually get excited at the absolute change as if it were the real volatility. The quantitative change may be large but the relative change may not be that much large. Here 25 highest one day increases and 25 highest decreases of S&P BSE Sensex are given. The daily index, change in the index and percentage change in the index, are also shown in TABLE 1.

TABLE 1 shows that the highest one day increase in Sensex is on 24 Jul 2000. The change in the index on that day was 5376.03 point. The percentage change was 120.44%. Note the difference between the absolute change and the percentage change. The second highest one day increase in the Sensex was on 18th May 2009. The change was 2110.79 point and the percentage change was only 17.34%. The third highest one day increase in the Sensex was on 18th May 2004 with only 8.25%, the absolute change being 371.86 point. The increase in the index on 24th July 2000 was not followed by the other days. It appears to be an exceptional occurrence.

TABLE 1: Showing 25 highest increases and decreases

<table>
<thead>
<tr>
<th>Sl.No.</th>
<th>Date</th>
<th>Close change</th>
<th>% Change</th>
<th>Sl.No.</th>
<th>Date</th>
<th>Close change</th>
<th>% Change</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>24-Jul-00</td>
<td>9839.69</td>
<td>5376.03</td>
<td>12</td>
<td>22-Jan-08</td>
<td>16729.94</td>
<td>4336.2</td>
</tr>
<tr>
<td>2</td>
<td>18-May-00</td>
<td>14284.21</td>
<td>2110.79</td>
<td>2</td>
<td>17-May-09</td>
<td>4505.16</td>
<td>-5503.49</td>
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<td>3</td>
<td>18-May-04</td>
<td>4877.02</td>
<td>371.86</td>
<td>3</td>
<td>24-Oct-08</td>
<td>8701.07</td>
<td>-1070.63</td>
</tr>
<tr>
<td>4</td>
<td>12-Oct-08</td>
<td>9788.80</td>
<td>743.55</td>
<td>4</td>
<td>21-Jan-08</td>
<td>17605.35</td>
<td>-1408.35</td>
</tr>
<tr>
<td>5</td>
<td>13-Oct-08</td>
<td>11309.09</td>
<td>781.24</td>
<td>5</td>
<td>7-Jan-09</td>
<td>9586.88</td>
<td>-749.05</td>
</tr>
<tr>
<td>6</td>
<td>7-Apr-09</td>
<td>5219.2</td>
<td>352.47</td>
<td>6</td>
<td>4-Apr-00</td>
<td>4691.46</td>
<td>-361.48</td>
</tr>
<tr>
<td>7</td>
<td>15-Jun-06</td>
<td>9545.06</td>
<td>615.62</td>
<td>7</td>
<td>10-Oct-08</td>
<td>10527.85</td>
<td>-800.51</td>
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<tr>
<td>8</td>
<td>25-Jan-08</td>
<td>18361.66</td>
<td>1139.92</td>
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<td>18-May-06</td>
<td>11391.43</td>
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<tr>
<td>9</td>
<td>4-May-09</td>
<td>12134.75</td>
<td>731.64</td>
<td>9</td>
<td>11-Nov-08</td>
<td>9839.69</td>
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<tr>
<td>10</td>
<td>25-Mar-08</td>
<td>16217.49</td>
<td>928.09</td>
<td>10</td>
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<td>11</td>
<td>23-Jul-08</td>
<td>14942.28</td>
<td>838.08</td>
<td>11</td>
<td>14-May-04</td>
<td>5069.87</td>
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<td>26-Oct-08</td>
<td>9050.08</td>
<td>498.52</td>
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<td>3540.65</td>
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<td>13</td>
<td>10-Nov-08</td>
<td>10536.16</td>
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<td>9810.46</td>
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<td>6-Oct-08</td>
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<td>21-Nov-08</td>
<td>8915.21</td>
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<td>17-Oct-08</td>
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<td>19-Sep-08</td>
<td>14052.32</td>
<td>726.72</td>
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<td>17-Apr-00</td>
<td>4880.71</td>
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<td>2-Jul-08</td>
<td>12664.62</td>
<td>702.94</td>
<td>20</td>
<td>22-Sep-00</td>
<td>4032.37</td>
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<td>10-Dec-08</td>
<td>9654.9</td>
<td>492.28</td>
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<td>14-Sep-01</td>
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<td>3725.03</td>
<td>184.38</td>
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<td>17-Sep-01</td>
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<tr>
<td>24</td>
<td>23-Mar-09</td>
<td>9424.02</td>
<td>457.34</td>
<td>24</td>
<td>3-Mar-08</td>
<td>16677.88</td>
<td>-900.84</td>
</tr>
<tr>
<td>25</td>
<td>4-May-00</td>
<td>4553.92</td>
<td>218.63</td>
<td>25</td>
<td>22-Jan-08</td>
<td>16729.94</td>
<td>-875.41</td>
</tr>
</tbody>
</table>

The difference between the absolute change and percentage change in the index is obvious. TABLE 1 also demonstrates the 25 highest single day decreases in BSE Sensex. The first highest decrease took place on 25 July 2000. The Sensex change was -5503.49 points whereas the percentage change was -55.93%. See the difference between the percentage change and the absolute change in the index. The second highest decrease was 17th May 2004 where the absolute change was -564.71 points but the percentage change was only -11.14%.

The third highest decrease in the index was occurred on 24th Oct., 2008 with a -1070.63 points decrease in the index, the percentage fall of which was only 10.96%. The other major decreases can be seen from the TABLE 1. All decreases were less than 8%. The sharp decrease on 25 July 2000 was the immediate fall after the sharp increase in the index in the previous day. This fall in the index appears to be exceptional since it is not followed by the other trading days.

6.2. Standard Deviation as a measure of volatility

The simplest tool to measure volatility is the standard deviation. Standard deviation is the dispersion of the occurrences from the expected value or mean. When standard deviation is squared variance is obtained. Standard deviation is used when the change in volatility is uniform. Standard deviation is valid only when the
distribution is normal. Under non-normal conditions when the price changes are dissimilar and time series correlates within, standard deviation will not be successful. Moreover, standard deviation will be showing only the volatility of the historical data. Volatility estimation for the future cannot be possible with the standard deviation.

TABLE 2 shows the summary statistics of the historical data of the S&P BSE Sensex for the period 2000-14 which includes the standard deviation for the period.

<table>
<thead>
<tr>
<th>TABLE 2: Showing summary statistics</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean</td>
</tr>
<tr>
<td>0.07</td>
</tr>
</tbody>
</table>

TABLE 2 shows the standard deviation of the historical daily data of S&P BSE sensex for the entire period. The standard deviation is 2.68%. During the great market crash the standard deviation of US stocks was 10% (G. William Schwert). During the period of Great Depression 1929-39 the standard deviation was recorded at 20%. Comparing to the standard deviation of great two market crises referred earlier the standard deviation for the entire period of 15 years 2.68% is very low.

6.3. Time-adjusted Standard Deviation

The standard deviation 2.68% shown in TABLE 2 is a flat rate for the entire period uncorrelated with the time. Equity returns are time-varying series showing dependence on time. The standard deviation given earlier is constant and irresponsible to the impact of time. The time-adjusted standard deviation has the advantage of relating the standard deviation with the time.

Here, the entire 3740 observations are divided in to 180 intervals of 21 days and standard deviation is calculated on the daily returns of the intervals. The standard deviation obtained thus is multiplied with the root square of trading days of the intervals. TABLE 3 shows the time adjusted standard deviation for 180 months (a month usually has 20-21 days trading days).

<table>
<thead>
<tr>
<th>TABLE 3: Time-adjusted standard deviation</th>
</tr>
</thead>
</table>

As per TABLE 3 in Jan 2000 the standard deviation was 8.49% and in Dec. 2014 it was only 3.96%.

Barring a few intervals the standard deviation was steadily diminishing. The overall tendency of the standard deviation series is to diminish.

TABLE 4 shows the standard deviation in the order of its magnitude. The standard deviation for the interval July 2000 is the highest with 135.64%. It was the highest volatility interval of the entire 15 year period.

The second highest is in the interval October 2008 with a standard deviation of 23.02%. The third highest is in May 2009 with a standard deviation of 17.44%. The lowest standard deviation was in November 14 with 1.73%.

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The Fig. 1 indicates that the standard deviation was high from interval 1 to interval 113 with around 10% barring the standard deviation in July 2000 of 135.64%.

From 120 intervals to the last of the series the standard deviation was considerably lower about less than 4%. Trend line projected in Fig. 1 shows the overall trend of the standard deviation. The trend is that of steady decrease in the standard deviation. The actual standard deviation in interval 7 was 135.64% whereas the predicted was only about 10%. The reason for such tremendous difference between the actual and the projected is exceptional. The high kurtosis of leptokurtic nature tells the inordinate increase in the return.

6.4. Volatility Estimate and Change in Volatility*.

*(The method is recommended by Fischer Black in his paper titled “Studies of Stock Market Volatility Changes”, 1976.)

Volatility is estimated from the summed daily returns of a 21 days interval. The root square of the annualized squared sum of daily returns of the intervals is called the volatility estimate for that interval.

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TABLE 5: Showing the volatility estimate & volatility change

<table>
<thead>
<tr>
<th>Interval</th>
<th>Summed Return</th>
<th>Summed Value</th>
<th>Annualise Volatility</th>
<th>Volatility Estimate</th>
<th>Change</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jan.00</td>
<td>-2.87%</td>
<td>0.08%</td>
<td>0.99%</td>
<td>10%</td>
<td></td>
</tr>
<tr>
<td>Feb.00</td>
<td>5.13%</td>
<td>0.26%</td>
<td>3.16%</td>
<td>18%</td>
<td>79%</td>
</tr>
<tr>
<td>Mar.00</td>
<td>-8.15%</td>
<td>0.66%</td>
<td>7.97%</td>
<td>28%</td>
<td>59%</td>
</tr>
<tr>
<td>Apr.00</td>
<td>-5.84%</td>
<td>0.34%</td>
<td>4.09%</td>
<td>20%</td>
<td>-28%</td>
</tr>
<tr>
<td>May.00</td>
<td>-3.88%</td>
<td>0.15%</td>
<td>1.81%</td>
<td>13%</td>
<td>-34%</td>
</tr>
<tr>
<td>Jun.00</td>
<td>7.15%</td>
<td>0.51%</td>
<td>6.13%</td>
<td>25%</td>
<td>84%</td>
</tr>
<tr>
<td>Jul.00</td>
<td>57.26%</td>
<td>32.79%</td>
<td>393.45%</td>
<td>198%</td>
<td>701%</td>
</tr>
<tr>
<td>Aug.00</td>
<td>4.65%</td>
<td>0.22%</td>
<td>2.59%</td>
<td>16%</td>
<td>-92%</td>
</tr>
<tr>
<td>Sep.00</td>
<td>-8.51%</td>
<td>0.72%</td>
<td>8.69%</td>
<td>29%</td>
<td>83%</td>
</tr>
<tr>
<td>Oct.00</td>
<td>-9.43%</td>
<td>0.89%</td>
<td>10.67%</td>
<td>33%</td>
<td>11%</td>
</tr>
<tr>
<td>Nov.00</td>
<td>7.72%</td>
<td>0.60%</td>
<td>7.15%</td>
<td>27%</td>
<td>-18%</td>
</tr>
<tr>
<td>Dec.00</td>
<td>-0.42%</td>
<td>0.00%</td>
<td>0.02%</td>
<td>1%</td>
<td>-95%</td>
</tr>
<tr>
<td>Jan.01</td>
<td>8.73%</td>
<td>0.76%</td>
<td>9.15%</td>
<td>30%</td>
<td>1939%</td>
</tr>
<tr>
<td>Feb.01</td>
<td>-1.61%</td>
<td>0.03%</td>
<td>0.31%</td>
<td>6%</td>
<td>-82%</td>
</tr>
<tr>
<td>Mar.01</td>
<td>-15.52%</td>
<td>2.41%</td>
<td>28.90%</td>
<td>54%</td>
<td>864%</td>
</tr>
<tr>
<td>Apr.01</td>
<td>-1.85%</td>
<td>0.03%</td>
<td>0.41%</td>
<td>6%</td>
<td>-88%</td>
</tr>
<tr>
<td>May.01</td>
<td>3.24%</td>
<td>0.11%</td>
<td>1.26%</td>
<td>11%</td>
<td>75%</td>
</tr>
<tr>
<td>Jun.01</td>
<td>-4.78%</td>
<td>0.23%</td>
<td>2.74%</td>
<td>17%</td>
<td>48%</td>
</tr>
<tr>
<td>Jul.01</td>
<td>-3.59%</td>
<td>0.13%</td>
<td>1.55%</td>
<td>12%</td>
<td>-25%</td>
</tr>
<tr>
<td>Aug.01</td>
<td>-2.52%</td>
<td>0.06%</td>
<td>0.76%</td>
<td>9%</td>
<td>-30%</td>
</tr>
<tr>
<td>Sep.01</td>
<td>-13.56%</td>
<td>1.84%</td>
<td>22.06%</td>
<td>47%</td>
<td>438%</td>
</tr>
<tr>
<td>Oct.01</td>
<td>6.36%</td>
<td>0.40%</td>
<td>4.85%</td>
<td>22%</td>
<td>-53%</td>
</tr>
<tr>
<td>Nov.01</td>
<td>9.68%</td>
<td>0.94%</td>
<td>11.24%</td>
<td>34%</td>
<td>52%</td>
</tr>
<tr>
<td>Dec.01</td>
<td>-0.61%</td>
<td>0.00%</td>
<td>0.04%</td>
<td>2%</td>
<td>-94%</td>
</tr>
<tr>
<td>Jan.02</td>
<td>1.59%</td>
<td>0.03%</td>
<td>0.30%</td>
<td>6%</td>
<td>163%</td>
</tr>
</tbody>
</table>

TABLE 5 shows 25 intervals of volatility estimate and change in volatility. The volatility of the first interval January 2000 was 10%. The standard deviation as per TABLE 3 for January 2000 was 8.49%. The volatility estimate for Feb. 2000 was 18% whereas the standard deviation for the same interval was 11.13%. The volatility estimate for the interval March 2000 was 28%. But the standard deviation for the same interval as per TABLE 3 was 8.73%. In this way standard deviation as per TABLE 3 more or less resembles the volatility estimate shown in TABLE 5.

Going through TABLE 5 it can be understood that there is a relationship between the summed returns and volatility estimate. When the summed return was -2.87 in Jan-2000 the volatility estimate against that was 10%. When the summed return increased to 5.13% in Feb-2000 the volatility estimate also increased to 18%.

For 278% increase in the summed returns the volatility increases by 80%. The change in volatility is 80% during this period. In March 2000 the summed return decreases to -8.15%. Consequently to that the volatility estimate though increases to 28%, the rate of change in volatility reduced to 55%. In July 2000 the summed return was -9.43%, against which the volatility estimate was 18%. From this it can be inferred that the summed returns of intervals and volatility estimates are positively correlated. When the summed returns are regressed with a constant and volatility estimate to find the intimacy, by making the volatility estimate as the dependent variable (Y) and the summed returns as the independent variable (X), the coefficients obtained are as follows.

TABLE 6: Regression Coefficients

<table>
<thead>
<tr>
<th>Coefficients</th>
<th>Standard Error</th>
<th>t Stat</th>
<th>P-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>0.24569247</td>
<td>0.051567817</td>
<td>4.764454</td>
</tr>
<tr>
<td>X Variable</td>
<td>2.11718588</td>
<td>0.38785659</td>
<td>5.458682</td>
</tr>
</tbody>
</table>

TABLE 6 implies that the volatility estimate will be 2.12 times that of the summed returns of the intervals. The P-value for the intercept and beta coefficient both are less than 5%. Therefore they are significant. As the P-value is less than 5% the null hypothesis that the coefficient b1=0 is rejected and the alternative hypothesis that beta> 0 is accepted. Hence, it can be deduced that the relation between the summed returns and volatility estimate is very strong.

TABLE 5 also shows the change in volatility. The estimated volatility as per the TABLE 5 never remains constant. It changes for every change in the summed returns. The change in volatility in the first
instance was 79%, then, 59%, then by -28%, and then by -34% and so on. The rate of change in volatility is not constant. Regressing the rate of change and the summed return it can be seen that for a 1% change in the summed return the volatility changes by 2.5% negatively. There is a very strong relation between the summed return and the change in volatility.

6.5. GARCH (1,1) Model

Standard deviation or variance is always constant. When standard deviation is used to represent volatility the assumption is that the volatility is also constant over a period. If volatility changes from time to time, especially it is true in the case of time-varying series, standard deviation fails. Equity returns are time-varying series. Moreover, the studies reveal that equity returns series are serially correlated. There are evidences for interdependency within the return series. TABLE 2 shows non-normality of equity returns due to the presence of large amount skewness and kurtosis. Since returns are interdependent within series, volatility too becomes interdependent. Due to dependency, it becomes true that today’s return dependent upon the volatility of yesterday. Similarly, Current volatility may depend upon previous day’s volatility. Accordingly, current return is conditional upon the previous day’s return and current volatility is conditional upon previous day’s volatility. This situation is called Generalized Auto Regressive Conditionally Heteroscedastic (GARCH) effect in the series. In terms of GARCH (1,1) terms -

\[ Y_t = (Y_t / Y_{t-1}) \] (9)

\[ \sigma^2_t = (\sigma^2_t / \sigma^2_{t-1}) \] (10)

Where, \( \sigma^2_t \) is current variance and \( \sigma^2_{t-1} \) is the conditional variance.

In such cases volatility is conditional and will change conditionally throughout the period in different magnitude. This heteroscedasticity of equity returns is governed by mainly three factors viz., 1) Long-run variance, 2) Previous day’s returns, and 3) Previous day’s variance.

Hence conditional variance is the measure of stock volatility which can be put in GARCH terms as equation (8). GARCH model is relevant when there is excessive volatility clustering and volatility dependence.

![Volatility clustering in residuals](image)

It can be noticed from Fig.2 that the volatility in residuals is dissimilar. There is slight volatility clustering in the distribution of the residuals. From day 1 to 141 the volatility is low. During this period low volatility is followed by low volatility for a prolonged period up to 141 days. From 141 to 142 days the volatility is very high. But this high volatility is not followed for a prolonged period. It is only for two days. From 142 to 1950th day low volatility is followed by low volatility for a prolonged period. From 1951 to 2401th day high volatility is followed by high volatility. From 2401 to 3739th day low volatility is followed by low volatility. Thus volatility has 5 segments. They are day 1 to 141, day 141 to 142, day 142 to 1950, day 1951 to 2401, and day 2401 to 3739. The first spell is characterized by low volatility followed by low volatility for a long period, the second by high volatility for a short period, the third by low volatility followed by low volatility for prolonged period, the fourth by relatively high volatility followed by high volatility and fifth by low volatility followed by low volatility for a prolonged period.
Volatility in Indian Stock Market: A study to assess volatility, persistence and GARCH effects.

The low/ high volatility followed by low / high volatility for a prolonged period indicates volatility clustering and volatility interdependency and persistence. This is an evidence of the prevalence of conditional volatility or GARCH effect in Indian stock market.

When mean and variance equations of the GARCH (1,1) model are solved and maximized the log likelihood, the parameters are estimated as under:

TABLE 7: GARCH(1,1) Parameters

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Coefficients</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\omega$</td>
<td>0.00028565</td>
</tr>
<tr>
<td>$\alpha_1$</td>
<td>0.28657148</td>
</tr>
<tr>
<td>$\beta_1$</td>
<td>0.24478029</td>
</tr>
<tr>
<td>$(\alpha_1, \beta_1) = \lambda$</td>
<td>0.53135177</td>
</tr>
</tbody>
</table>

Unconditional variance

0.00071906

TABLE 7 provides the estimated GARCH (1,1) parameters. The constraints of GARCH (1,1) parameters are

$\alpha_1 > 0$

$\beta_1 > 0$

$(\alpha_1, \beta_1) = \lambda < 1$

Here, $\alpha_1$ is the coefficient of 1 lag squared residuals $\varepsilon_t^2$, $\beta_1$ is the coefficient of 1 lag variance $\sigma^2_{t-1}$, $\lambda$ is the sum of $\alpha_1$ and $\beta_1$ representing volatility persistence.

Unconditional volatility ($\sigma^2_t$) = $\frac{\omega}{1-\alpha-\beta}$

(11)

Conditional volatility = $\sigma^2_t = \sigma^2 \cdot \lambda^t$

(12)

TABLE 7 shows that the parameters are above 0 and the sum of $\alpha_1$ and $\beta_1$ is less than 1. The parameters tell the quantum of conditional volatility in the variance of returns. If alpha increases beta will reduce and vice versa. If $\lambda$, the sum of $\alpha_1$ and $\beta_1$ nears 1 it signals extreme conditional volatility persistence on current unconditional variance. If $\lambda$ is lower persistence can be said lower. If $\lambda$ is higher persistence is higher. If $\lambda$ is 1 as per equation (11) unconditional volatility becomes zero. In that case the whole volatility will be conditional.

TABLE 7 shows that $\lambda$ is 0.53135177. It implies that the past shocks only moderately influence the current variance. The current variance has both the components of unconditional and conditional variances in an equal way. The conditional part of current variance as per TABLE 7 is 53% of unconditional variance.

VII. Conclusion

This paper attempted to study the volatility in Indian stock market with the daily data of S&P BSE Sensex for a period of 15 years from 2000 to 2014 with a total of 3740 observations. BSE Sensex was chosen to represent Indian stock market. The study has found that there is considerable difference between the quantitative change and percentage change in the Sensex. Keeping aside a few days of exceptional behavior due to excess skewness and excess kurtosis the percentage change in the index is below 8%. The standard deviation for the entire period is considerably lower, less than 3%. The time-adjusted standard deviation for 180 intervals of 21 days is almost similar to the percentage change in the index. The time-adjusted standard deviation showed a trend of steady decline from the initial periods’ 10% to below 4% ending with 1.73%. Volatility estimate based on the summed daily returns show volatility similar to time-adjusted standard deviation. But the relationship between the summed returns and the volatility estimate is found very strong when they are regressed. Hence it becomes possible to predict the volatility if daily returns are available. There are enough evidences for the presence of heteroscedasticity in the equity returns of Indian stock market. When residuals are examined it is found that there is volatility clustering. Low volatility is followed by low volatility and high volatility is followed by high volatility for a prolonged period. Indian stock market has GARCH effect. The GARCH parameters show evidences for moderate volatility persistence in the equity returns.

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