Evaluation of the mass attenuation coefficient and Effective Atomic Number of the Eremurus spp. Root in Mammography Energy Range

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\textbf{Abstract:} The potential of the Eremurus spp. root as a binder in Rhizophora-Eremurus spp. particleboard mammography phantom had been approved. In this study, the potential of Eremurus spp. as a phantom material has been investigated. The effective atomic number of the Eremurus spp. was calculated as an important parameter in the low energy range. Also, the mass attenuation coefficient of the Eremurus spp. root was measured in the 16.63 keV – 25.30 keV photon energy as a mammography range. Although, the effective atomic number of the Eremurus spp. was near to that of tissue, the mass attenuation of the Eremurus spp. root was not found close to those of breast tissue and water phantom. The results show that the Eremurus spp. root can be used just as a binder in phantom and it cannot be as a main phantom material.

\textbf{Keywords:} Effective Atomic Number, Eremurus spp., Mammography, Mass Attenuation Coefficient, XRF

I. Introduction

The phantom has been widely used as a simulated system in medical physics [1]. The phantom can be made from various material in different shapes [2, 3]. Water is the most used as a phantom material based on similar composition with body tissue [2, 4]. But, the physical properties of water causes that water phantom cannot be used in all medical and research centers [5]. The natural material such as wood has been considered as a phantom material [6-11]. The Rhizophora-Eremurus spp. particleboard has been investigated as a mammography phantom by some researchers [2, 10, 12, 13], which confirmed the potential of the Rhizophora-Eremurus spp. particleboard as a mammography phantom. The Eremurus spp. root was used as a binder in the Rhizophora-Eremurus spp. particleboard, which just had 5 % to 15% of the Eremurus spp. weight percentage. In this study, the potential of the Eremurus spp. root has been investigated as a main phantom material [14].

The breast is a soft organ, which is not including the dense mass such as the bone. Therefore, the lower energies of X-ray are used in the mammography to illustrate the breast diseases. A composite material contains multiple elements. During photons interaction with matter, the atomic number is one of the most important parameters [15, 16]. The breast is a composite material that contains multiple elements. The mixture matter can be assumed as a simple matter to calculate its atomic number, which is called effective atomic number ($Z_{\text{eff}}$). Therefore, $Z_{\text{eff}}$ of a phantom material should be firstly compared with that of tissue [13]. One of the most important parameters for a phantom is the mass attenuation coefficient in the lower energy range [12]. The mass attenuation coefficient is defined as a ratio of the linear attenuation coefficient ($\mu$) per density of absorber material ($\rho$). The unit of mass attenuation coefficient is m$^2$.kg$^{-1}$ in the SI system. The mass attenuation coefficient is a more significant quantity in the attenuation properties of a material, because it offers the reduction of X-ray intensity as a function of the mass of traveled material instead of the path length as the linear attenuation [17-19]. In this study, the effective atomic number of the Eremurus spp. root was calculated and compared with those of tissue and water phantom. Then, the mass attenuation coefficient of Eremurus spp. root was measured by X-rays in 16.63 keV – 25.30 keV energy range, and was compared with the theoretical values for water and young-age breast with 75 % muscle and 25 % fat that is called Breast 1 [7, 13] calculated by the XCOM computer program [20].

II. Materials And Methods

1.1. Effective Atomic Number ($Z_{\text{eff}}$)

The photoelectric effect is one of the most significant interaction of photons with matter in the low-energy photon range, which is used in mammography technique [15, 21, 22]. The photoelectric effect is actively affected by the atomic number ($Z$) or effective atomic number ($Z_{\text{eff}}$) of the composite materials [15, 21, 22].
Therefore, the response of two materials with the same effective atomic number could be significantly closer together under the radiation in the low-energy range. The effective atomic number of a compound material is determined by Eq. 1 [15, 23, 24]:

\[
Z_{\text{eff}} = \left( \sum_{i=1}^{N} \left( \alpha_i Z_i^n \right) \right) \left( \frac{1}{m} \right)
\]

(1)

where \( \alpha_i \) and \( Z_i \) are the electronic fraction and atomic number of the \( i \)th element in the composite, respectively. The experimental coefficient is called \( m \) that has been evaluated to be equal 3.4 for biological materials such as water, wood, or human organs [23, 24]. Also, the electronic fraction of the \( i \)th element is given by Eq. 2 [15, 24, 23, 24]:

\[
\alpha_i = \frac{w_i \left( \frac{Z_i}{A_i} \right)}{\sum_{i} w_i \left( \frac{Z_i}{A_i} \right)}
\]

(2)

where, \( w_i \) and \( A_i \) are fractional weight and atomic mass of the \( i \)th element, respectively.

1.2. Attenuation coefficient properties

In the present study, an X-ray fluorescent (XRF) beam was used to determine the mass attenuation coefficient of the root of Eremurus spp. XRF photons were emitted from high-purity metal target that was exposed by an annular 241Am \( \gamma \) source. The XRF energies from the metal targets were niobium (\( K_{\alpha} = 16.63 \) keV), molybdenum (\( K_{\alpha} = 17.47 \) keV), palladium (\( K_{\alpha} = 21.26 \) keV), silver (\( K_{\alpha} = 22.17 \) keV), and tin (\( K_{\alpha} = 25.30 \) keV). The experimental schematic diagram of XRF set-up is shown in Fig. 1.

Figure 1. The experimental schematic diagram of XRF set-up to measure the attenuation coefficients of the root of Eremurus spp.

According to the Beer-Lambert law, the attenuation of a photon beam passing through a material is determined by Eq. 3 [17]:

\[
I = I_0 e^{-\mu x}
\]

(3)

where \( I \) is the transmitted photon intensity, \( I_0 \) is the primary photon intensity, \( x \) is the thickness (cm) of the sample and \( \mu \left( \text{cm}^{-1} \right) \) is the linear attenuation coefficient of the material. The mass attenuation coefficient is defined by Eq. 4 [12]:

\[
\mu = \frac{1}{x} \ln \left( \frac{I_0}{I} \right) = \frac{\mu}{\rho} \ln \left( \frac{I_0}{I} \right)
\]

(4)

where \( \mu/\rho \) is the mass attenuation coefficient \( \left( \text{cm}^2 \text{g}^{-1} \right) \) and \( \rho x \) is called the mass density or mass thickness. The error of the mass attenuation coefficient can be determined by Eq. 5 [25]:

\[
\sigma_{\mu/\rho} = \left( \sigma_{\mu} \right)^2 + \left( \frac{\sigma_{\rho}}{\rho} \right)^2 \left( \frac{\mu}{\rho} \right)
\]

(5)

where \( \sigma_{\mu} \left( \text{cm}^{-1} \right) \) and \( \sigma_{\rho} \left( \text{g cm}^{-3} \right) \) are the errors in the linear mass attenuation coefficient and in the density, respectively that are given by Eqs. 6 and 7 [25]:

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\[ \sigma_{(\mu)} = \pm \left( \frac{\mu_{\text{max}} - \mu_{\text{min}}}{2} \right) \]  
\[ \sigma_{(\rho)} = \pm \left( \frac{\rho_{\text{max}} - \rho_{\text{min}}}{2} \right) \]  

Also the percentage difference of the mass attenuation coefficient is calculated by Eq. 8 [26]:

\[ \text{error}\% = \frac{(\mu / \rho)_{\text{theo}} - (\mu / \rho)_{\text{exp}}}{(\mu / \rho)_{\text{theo}}} \times 100\% \]  

where \((\mu / \rho)_{\text{exp}}\) and \((\mu / \rho)_{\text{theo}}\) are the experimental and theoretical mass attenuation coefficients, respectively.

The cylindrical samples of the *Eremurus* spp. root were made for XRF by Carver 4350L manual hydraulic press machine with 1 g/cm\(^3\) as the target density. The diameter of samples was 15 mm and the thicknesses were 3 mm, 6 mm, 8 mm, and 15 mm, approximately. Fig. 2 shows the samples used for the measurement of the mass attenuation coefficients.

![Figure 2](image.png)

**Figure 2.** Experimental samples used for the measurement of the mass attenuation coefficients of the *Eremurus* spp. root, in four different thicknesses a (3 mm), b (6 mm), c (8 mm), and d (15 mm).

### III. Results And Discussion

1.3. Calculated effective atomic number of the *Eremurus* spp. root (\(Z_{\text{eff}}\))

The powdered *Eremurus* spp. root was used as the samples for FE–SEM coupled EDX. The FE–SEM micrographs and EDX results of the *Eremurus* spp. root is shown in Fig. 3.

![Figure 3](image.png)

**Figure 3:** The FE-SEM and EDX results of the *Eremurus* spp. root.

The elemental composition of water [27], young-age breast :breasts 1 with 75% muscle and 25% fat [7], and *Eremurus* spp. are shown in Table 1 that consists calculated \(Z_{\text{eff}}\) values of them based in Eqs. 1 and 2.

<table>
<thead>
<tr>
<th>Composite</th>
<th>Component Elements</th>
<th>(Z_{\text{eff}})</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water</td>
<td>H 0.11 C 0.00 N 0.00 O 0.89 Na 0.06 Mg 0.00 P 0.00 S 0.00 Cl 0.13 K 0.02 Ca 0.18</td>
<td>7.50</td>
</tr>
<tr>
<td>Breast 1(^{3})</td>
<td>10.70 28.30 2.63 57.60 0.06 0.02 0.15 0.38 0.06 0.23 0.01</td>
<td>7.29</td>
</tr>
<tr>
<td><em>Eremurus</em> spp. root</td>
<td>52.44 6.91 40.01 0.00 0.00 0.00 0.00 0.13 0.52 0.00</td>
<td>7.36</td>
</tr>
</tbody>
</table>

\(^{3}\) [7]; \(^{2}\) [27]; \(^{2}\) [7]

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The $Z_{eff}$ values of *Eremurus* spp. was found among those of water and breast 1. The percentage difference between $Z_{eff}$ value of breast 1 with that of *Eremurus* spp. root was 0.96%, which proved the potential of the *Eremurus* spp. root to be as a tissue–equivalent phantom material.

1.4. Mass attenuation coefficient measurement

The linear and mass attenuation coefficient of the root of *Eremurus* spp. in the photon energy range of 16.63 keV – 25.3 keV is shown in Table 2, which simultaneously illustrates the XCOM calculated mass attenuation coefficients of water and young-age breast, and the difference and percentage difference of the mass attenuation coefficients of the root of *Eremurus* spp.

**Table 2.** Mass attenuation coefficients of water and Breast 1 from the XCOM computer program [20], and linear attenuation coefficient, mass attenuation coefficient, error, and percentage difference of the mass attenuation coefficients of the root of *Eremurus* spp.

<table>
<thead>
<tr>
<th>Energy (keV)</th>
<th>Water (XCOM)</th>
<th>Breast 1 (XCOM)</th>
<th><em>Eremurus</em> spp. root</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\mu/\rho$ (cm²g⁻¹)</td>
<td>$\mu$ (cm⁻¹)</td>
<td>$\mu/\rho$ (cm²g⁻¹)</td>
</tr>
<tr>
<td>16.63</td>
<td>1.270</td>
<td>1.160</td>
<td>2.225</td>
</tr>
<tr>
<td>17.47</td>
<td>1.120</td>
<td>1.020</td>
<td>1.922</td>
</tr>
<tr>
<td>21.26</td>
<td>0.706</td>
<td>0.652</td>
<td>1.196</td>
</tr>
<tr>
<td>22.17</td>
<td>0.645</td>
<td>0.598</td>
<td>1.062</td>
</tr>
<tr>
<td>25.30</td>
<td>0.497</td>
<td>0.466</td>
<td>0.805</td>
</tr>
</tbody>
</table>

The mass attenuation of the root of *Eremurus* spp. is compared with the XCOM calculated that of water and young-age breast in Fig. 4.

**Figure 4.** The comparison between the mass attenuation coefficients of the root of *Eremurus* with XCOM calculated that of water phantom and Breast 1 (Young-age breast).

According to Table 2 and Fig. 4, the mass attenuation coefficient of the root of *Eremurus* spp. was not close to that of water and Breast 1. Therefore, the *Eremurus* spp. root is not suitable to be a main and major phantom material in wooden mammography phantom. But, the weight percentage of the resin is around 5% - 15% in the particleboard [28]. So, the congruence and similarity of the mass attenuation coefficients of the root of *Eremurus* spp. with that of water and breast 1, caused that the root of *Eremurus* spp. had potential to be a binder material for the fabrication of particleboards.

**IV. Conclusion**

The effective atomic number of the *Eremurus* spp. root was found much closer to those of breast tissue and water phantom. But, the mass attenuation coefficient of the root of *Eremurus* spp. was not the same as that of water and young-age breast. So the using of the root of *Eremurus* spp. was not found suitable as particles to fabricate particleboard phantom. But the results from XRF were found to be congruent, and compatible with that of water and breast tissue, which showed a suitability of the root of *Eremurus* spp. as a resin to fabricate particleboard phantom.
References


