

Growth, Structure and Physical Properties of Tetraaqua Bismaleatocobalt (II) Crystals

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Abstract: *Tetraaqua bismaleatocobalt(II) crystals are grown by the controlled ionic diffusion in hydrosilica gel. The functional groups present in the crystal are identified using FTIR spectrum. The compound crystallizes in the triclinic system with space group P-1. The thermogravimetric studies revealed a three stage decomposition scheme. The polarization mechanism of the compound is explored using the dielectric measurements. The optical band gap of the material is found to be 2.4 eV from diffuse reflectance spectroscopy (DRS). The narrow magnetic hysteresis loop and structural considerations indicate the weak ferromagnetic behaviour of the material.*

Keywords - *Crystal structure, Diffuse reflectance spectroscopy (DRS), Infrared spectroscopy, Thermogravimetric analysis (TGA), X-ray diffraction*

I. INTRODUCTION

Many crystals of metal coordination complexes like oxalates [1], tartrates [2], malates [3-4], and malonates [5-8] exhibit properties like ferroelectricity, piezoelectricity, photoconductivity and photoluminescence and have become technologically important. The coordination complexes of maleic acid with various transition and rare earth metals [9-10] have displayed interesting optical, magnetic and electrical properties, mainly due to their structural versatility. Details on the structure of certain precipitated metal maleates are found in literature [11 -13]. Although a report on the isomorphous series of compounds bearing the general formula $M(\text{HC}_4\text{H}_2\text{O}_4)_2 \cdot 4\text{H}_2\text{O}$, where $M = \text{Zn, Ni and Co}$ [14] is available, the detailed structure and properties of cobalt maleate is not explored till date. Conventional solution growth techniques seem unsuitable in yielding device grade crystals of metal maleates. Recently, we have resorted to the method of controlled diffusion of ionic species in hydrosilica gel medium and obtained strain free, optical quality crystals of barium maleate [15]. Here, we report the growth of prismatic crystals of cobalt maleate by the above method. Its structure as well as thermal, optical, electrical and magnetic behavior is elucidated.

II. EXPERIMENTAL

Gel matrices were prepared in straight glass tubes by titrating sodium meta silicate solution against aqueous maleic acid till a desired pH was obtained [16]. Ensuring proper gelation, aqueous cobaltous chloride solution was gently poured over, and the tubes were hermetically sealed and kept undisturbed at room temperature. Many batches of experiments corresponding to different densities of the gel (1.02gm/cc - 1.07gm/cc) and pH values of the medium (4 - 7, in steps of 0.1) were conducted. The strength of the inner and supernatant reactants was altered from 0.25 M to 2 M in different trials.

The FTIR spectrum was recorded using a Thermo Nicolet Avtar 370 model spectrophotometer, in the wave number range 400 cm^{-1} - 4000 cm^{-1} with a resolution of 4 cm^{-1} , by KBr pellet method. A fine crystal of size $0.30 \times 0.20 \times 0.20 \text{ mm}^3$, formed at gel solution interface, was chosen for single crystal X-ray diffraction (XRD) analysis. The Bruker AXS Kappa Apex2 CCD Diffractometer with graphite monochromated Mo-K α radiation was employed for the diffraction studies. The data collection, cell refinement and data reduction were done using the software APEX2/SAINT [17]. The crystal structure was solved using SIR92 [18] and was refined using SHELXL-97 [19 -20]. The Full-matrix least squares refinement based on 1105 reflections and 113 parameters, converged the residuals to $R_1 = 0.0258$, $wR_2 = 0.0728$. The thermal response of the material was traced using Perkin Elmer made Pyris Diamond TG - DTA analyzer by heating the sample in nitrogen atmosphere from room temperature to $820 \text{ }^\circ\text{C}$ at a rate of $20 \text{ }^\circ\text{C} / \text{minute}$. Dielectric measurements on silver electroded pellets were carried out using Hioki 3532 -50 Hi tester. The pellets used were of diameter 1.3 cm and thickness 1 mm. Measurements were carried out from 303 K to 373 K in the frequency range 50 Hz - 2 MHz. The Diffused Reflectance from the sample was collected using Cary 5E UV-Vis-NIR spectrophotometer in the range 200 nm - 2100 nm. The isothermal magnetization measurements were carried on powdered samples using EC&G PARC VSM 155 Vibrating Sample Magnetometer.

III. RESULTS AND DISCUSSION

3.1. Crystal formation

Prismatic and well faceted crystals of the title compound that began to grow in the gel-solution interface in about 4 to 5 months attained their maximum size in another couple of months. They were transparent and deep purple in colour. Better crystals were formed in a gel of density 1.06 gm/cc at pH 6 corresponding to 0.75M and 2M concentrations respectively of inner and outer reactants. Crystals of dimensions upto $10 \times 7 \times 6 \text{ mm}^3$ were yielded (Fig.1).

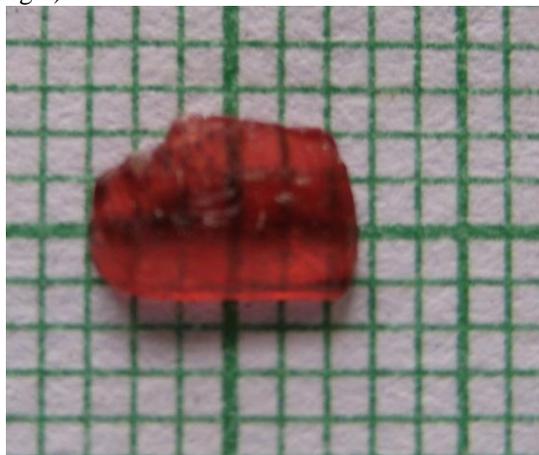


Figure 1. Photograph of the grown crystal.

3.2. FTIR spectral analysis

The recorded FTIR spectrum (Fig. 2) bears the signatures of all the functional groups present in the compound. It is interpreted in the light of the established data for similar compounds [21 - 22]. The bands assigned to various vibrations are shown in Table1.

The broad envelope in the high energy region at 3386.51 cm^{-1} is due to symmetric stretching mode of water molecule, while the weak band at 3056.13 cm^{-1} represents its stretching mode. Asymmetric and symmetric stretching of the carboxylate group occurs at wavenumbers 1556.41 cm^{-1} and 1396.53 cm^{-1} respectively and the strong band observed at 1681.93 cm^{-1} is due to the asymmetric stretching of C=O. The bands at 1484.21 cm^{-1} and 1364.20 cm^{-1} corresponds to C=C stretching. The absorption peaks at 1225.29 cm^{-1} and 942.93 cm^{-1} are respectively due to the bending of the C-O-H group, in and out of plane. The asymmetric and symmetric stretching modes of C-C bond occurs at wavenumbers 1120.73 cm^{-1} and 898.48 cm^{-1} in order. The C-H group bends out of plane at 865.98 cm^{-1} . The bands at 804.33 cm^{-1} and 512.21 cm^{-1} are ascribed to the deformation of the O-H group. The absorption at 748 cm^{-1} is due to the vibrations of the -CH group. The metal oxygen stretching occurs at 670.54 cm^{-1} .

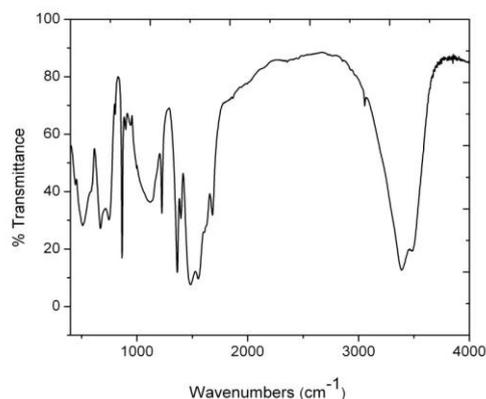


Figure 2. FTIR spectrum of the crystal.

Table 1. Spectral assignments of IR peaks.

Wave Number (cm ⁻¹)	Assignment
3386.51	ν_{as} H-O-H
3056.13	ν_s H-O-H
1681.93	ν_{as} C=O
1556.41	ν_{as} O-C=O
1484.21	ν_{as} C=C
1396.53	ν_s O-C=O
1364.20	ν_s C=C
1225.29	δ C-O-H in plane
1120.73	ν_{as} C-C
942.93	δ C-O-H out of plane
898.48	ν_s C-C
865.98	δ C-H out of plane
804.33	ρ_w H ₂ O
748.00	π C-H
670.54	ν M-O
512.21	ρ_t H ₂ O

3.3. Crystal structure analysis

Single crystal X-ray diffraction studies reveals that the crystallized complex is tetraaqua bismaleatocobalt (II) (Co (C₄H₃O₄)₂. 4H₂O). It crystallizes in the triclinic system with space group *P*-1. The unit cell dimensions are $a = 5.213(5) \text{ \AA}$, $b = 7.320(5) \text{ \AA}$, $c = 9.216(5) \text{ \AA}$, $\alpha = 109.170(5)^\circ$, $\beta = 104.372(5)^\circ$, $\gamma = 93.203(5)^\circ$. The crystal structure and refinement data are shown in Table 2. The ORTEP [23 - 25] of the molecule, drawn with thermal ellipsoids at 50% probability (Fig. 3), illustrates the structure of the molecule. It is seen that four water molecules are coordinated to the central cobalt ion forming a square base in a plane. Two maleate ligands are monodendately coordinated to the same cobaltous ion resulting in square bipyramidal geometry. The polymeric structure (Fig. 4) clearly shows the packing of the molecule in the triclinic lattice. Tables 3 and 4 list the selected bond lengths and bond angles in order.

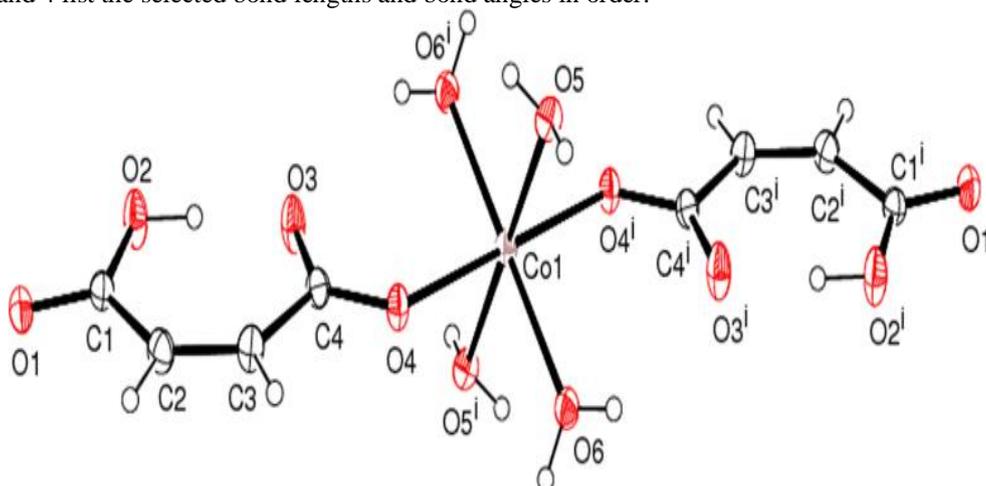


Figure 3. ORTEP of the molecule with 50 % probability.

Table 2. Crystal data and structure refinement.

Empirical formula	C ₈ H ₁₄ Co O ₁₂
Formula weight	361.12
Temperature	293(2) K
Wavelength	0.71073 \AA
Crystal system, space group	Triclinic, <i>P</i> -1
Unit cell dimensions	$a = 5.213(5) \text{ \AA}$, $\alpha = 109.170(5)^\circ$ $b = 7.320(5) \text{ \AA}$, $\beta = 104.372(5)^\circ$ $c = 9.216(5) \text{ \AA}$, $\gamma = 93.203(5)^\circ$
Volume	
Z, Calculated density	
Absorption coefficient	93.203(5) cm ² mol ⁻¹
F(000)	318.1(4) \AA^3
Crystal size	1, 1.885 Mg/m ³
θ range for data collection	1.415 mm ⁻¹

Limiting indices	185
Reflections collected / unique	0.30 mm x 0.20 mm x 0.20
Completeness to $\theta = 24.99^\circ$	mm
Absorption correction	2.44° to 24.99°
Max. and min. transmission	$-6 \leq h \leq 6, -8 \leq k \leq 8, -10 \leq l \leq 10$
Refinement method	$l \leq 10$
Data / restraints / parameters	5456 / 1105 [$R(\text{int}) =$
Goodness-of-fit on F^2	0.0323]
Final R indices [$I > 2\sigma(I)$]	98.7 %
R indices (all data)	Semi-empirical from
Largest diff. peak and hole	equivalents
	0.7781 and 0.6652
	Full-matrix least-squares on
	F^2
	1105 / 4 / 113
	1.171
	$R_1 = 0.0258, wR_2 = 0.0728$
	$R_1 = 0.0261, wR_2 = 0.0732$
	0.633 and $-0.356 \text{ e} \text{ \AA}^{-3}$

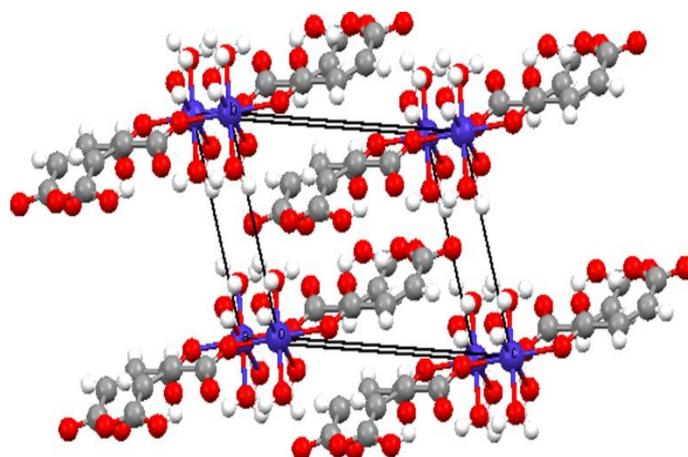


Figure 4. Polymeric structure of cobalt maleate tetrahydrate.

Table 3. Bond lengths in tetraaqua bismaleatocobalt(II).

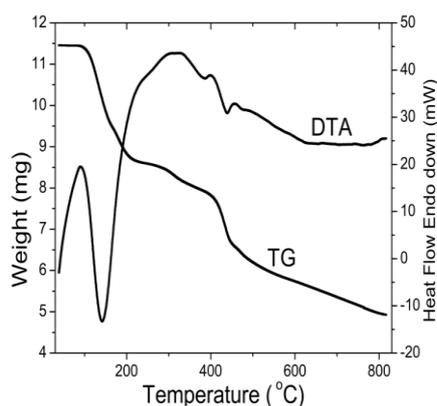
Bond	Length (Å)
C(1)-O(1)	1.224(2)
C(1)-O(2)	1.287(3)
C(1)-C(2)	1.485(3)
C(2)-C(3)	1.334(3)
C(2)-H(2)	0.9300
C(3)-C(4)	1.488(3)
C(3)-H(3)	0.9300
C(4)-O(4)	1.249(2)
C(4)-O(3)	1.262(3)
O(2)-H(2A)	0.8200
O(4)-Co(1)	2.1191(16)
O(5)-Co(1)	2.1258(17)
O(5)-H(5A)	0.836(10)
O(5)-H(5B)	0.830(10)
O(6)-Co(1)	2.0410(17)
O(6)-H(6B)	0.842(10)
O(6)-H(6A)	0.839(10)
Co(1)-O(6)#1	2.0410(17)
Co(1)-O(4)#1	2.1191(16)
Co(1)-O(5)#1	2.1258(18)

Table 4. Bond angles of tetraaqua bismaleatocobalt(II).

Bond	Angle (°)	Bond	Angle (°)
O(1)-C(1)-O(2)	121.36(18)	Co(1)-O(6)-H(6A)	121(2)
O(1)-C(1)-C(2)	118.47(18)	H(6B)-O(6)-H(6A)	115(3)
O(2)-C(1)-C(2)	120.15(17)	O(6)-Co(1)-O(6)#1	180.0
C(3)-C(2)-C(1)	130.55(18)	O(6)-Co(1)-O(4)#1	96.35(6)
C(3)-C(2)-H(2)	114.7	O(6)#1-Co(1)-O(4)#1	83.65(6)
C(1)-C(2)-H(2)	114.7	O(6)-Co(1)-O(4)	83.65(6)
C(2)-C(3)-C(4)	130.18(18)	O(6)#1-Co(1)-O(4)	96.35(6)
C(2)-C(3)-H(3)	114.9	O(4)#1-Co(1)-O(4)	180.00(8)
C(4)-C(3)-H(3)	114.9	O(6)-Co(1)-O(5)#1	88.66(8)
O(4)-C(4)-O(3)	122.96(17)	O(6)#1-Co(1)-O(5)#1	91.34(8)
O(4)-C(4)-C(3)	116.50(17)	O(4)#1-Co(1)-O(5)#1	88.28(7)
O(3)-C(4)-C(3)	120.54(17)	O(4)-Co(1)-O(5)#1	91.72(7)
C(1)-O(2)-H(2A)	109.5	O(6)-Co(1)-O(5)	91.34(8)
C(4)-O(4)-Co(1)	127.65(12)	O(6)#1-Co(1)-O(5)	88.66(8)
Co(1)-O(5)-H(5A)	110.3(18)	O(4)#1-Co(1)-O(5)	91.72(7)
Co(1)-O(5)-H(5B)	116.8(16)	O(4)-Co(1)-O(5)	88.28(7)
H(5A)-O(5)-H(5B)	102(2)	O(5)#1-Co(1)-O(5)	180.0

Symmetry transformations used to generate equivalent atoms: #1 -x+2,-y,-z+2

3.4. Thermal Studies

**Figure 5.** TG - DTA curves of cobalt maleate tetrahydrate.

The thermal stability and decomposition pattern of the grown crystals were evaluated from TG-DTA curves (Fig. 5). The crystal is found to be thermally stable up to 98 °C. It becomes anhydrous in the temperature range 98 °C - 184 °C. The sharp endothermic peak in the DTA curve at 143 °C corresponds to this dehydration. Upon heating the sample to 424 °C, the anhydrous cobalt maleate gets transformed to cobalt oxalate, eliminating acetylene and hydrogen molecules. The broad exotherm in DTA at 320 °C confirms the decomposition. During the next stage of decomposition (424 °C - 635 °C), two molecules of carbon monoxide are liberated leaving behind cobalt carbonate. The small exothermic peak around 460 °C in the DTA corresponds to this transformation. The mass loss observed in each stage concurs with the calculated values (Table 5). The TG curve shows gradual weight loss upon further heating indicative of the formation of an ultimate stable product at a temperature above 820 °C.

The stoichiometry of the title compound is evident from the thermal studies also and hence the chemical reaction leading to the formation of the title compound is:

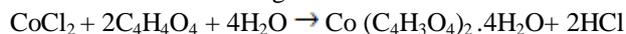


Table 5. The thermal decomposition process of $\text{Co}(\text{C}_4\text{H}_3\text{O}_4)_2 \cdot 4\text{H}_2\text{O}$.

Stage	Decomposition temperature ($^{\circ}\text{C}$)	Product after decomposition	Molecules evolved	Observed mass loss (%)	Calculated mass loss (%)
1	98 – 184	$\text{Co}(\text{C}_4\text{H}_3\text{O}_4)_2$	$4\text{H}_2\text{O}$	19.975	19.955
2	184 – 424	$\text{Co}(\text{C}_2\text{O}_4)_2$	$2\text{C}_2\text{H}_2 + \text{H}_2$	14.979	14.977
3	424 – 635	$\text{Co}(\text{CO}_3)_2$	2CO	15.513	15.512

3.5. Dielectric Studies

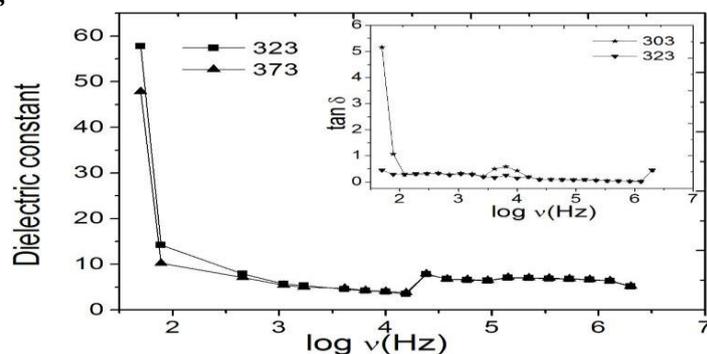


Figure 6. Frequency response of dielectric constant and dielectric loss.

The values of dielectric constant and loss tangent are found to be decreasing with increasing frequency (Fig. 6), indicating that beyond a certain frequency, the polarization could not follow the alternating applied electric field. The relatively higher value of dielectric constant at lower frequencies is due to the interfacial polarization [26-27]. The space charge polarization mechanism gives rise to higher dielectric loss at low frequencies. The characteristic low dielectric loss at higher frequencies is indicative of the optical quality of the crystals. The small peak in loss tangent (inset of Fig. 6) immediately before $\log v = 4$ ($v = 6430\text{ Hz}$) is attributed to the position exchange of the metallic ion between its two equally probable potential energy sites. When the frequency of the applied field matches the natural frequency of position change, maximum electrical energy is transferred to the jumping ions resulting in a small resonance peak in the loss tangent [28].

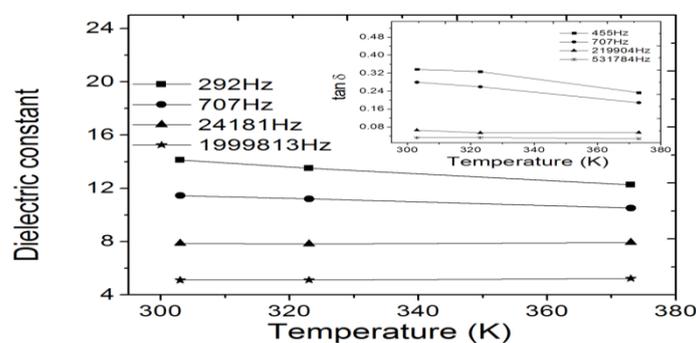


Figure 7. Thermal response of dielectric constant and dielectric loss.

The dielectric constant and dielectric loss are found to be almost temperature independent (Fig. 7), indicative of the good chemical homogeneity [29] and structural stability of the grown crystals.

3.6. Diffused Reflectance Spectroscopy

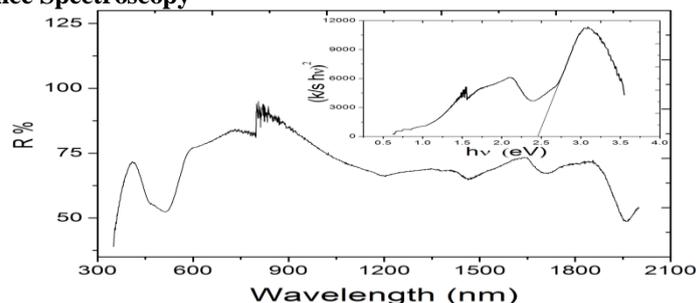


Figure 8. Diffused reflectance spectrum of the compound.

Fig. 8 presents the diffused reflectance from the sample in the UV-Vis-NIR region. Following the Kubelka-Munk method, the optical band gap of the material is determined by plotting $((k/s)hv)^2$ versus hv (inset of Fig. 8) where R , k and s are the reflectance, absorption and scattering coefficients respectively [30 -31]. The band gap evaluated from the linear fit of the curve on the energy axis is 2.4 eV. The low value of the band gap indicates relatively densely packed crystalline nature of the complex [32].

3.7. Magnetic studies

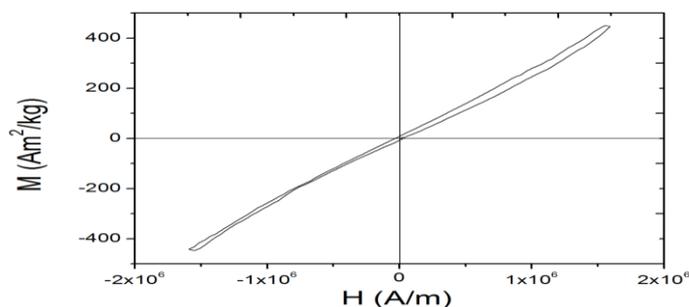


Figure 9. Hysteresis loop of cobalt maleate tetrahydrate.

The VSM measurements yielded a narrow hysteresis loop (Fig. 9) at room temperature. The structure sensitive parameters such as saturation magnetization, remanent magnetization and coercivity are found to be 449.5 Am²/kg, 7.762 Am²/kg and 32006 A/m respectively. The structure of the title compound being octahedral, the degeneracy of the d orbitals of Co^{2+} ions splits into high energy two fold degenerate e_g and low energy three fold degenerate t_{2g} . Since the number of unpaired $3d$ electrons in Co^{2+} ion is 3, the complex is in high state. Also, in this material the antiferromagnetic interaction arising due to the overlapping magnetic orbitals does not occur due to the monodentate coordination of the maleate ligands with the metal ion. In brief, the material would exhibit weak ferromagnetism.

IV. CONCLUSION

Well faceted, purple crystals of cobalt maleate have been grown by the limited diffusion of cobalt ions into hydrosilica gel impregnated with maleate ions. The FTIR and single crystal XRD studies confirm that the grown crystal is tetraaqua bismaleatocobalt(II). Also, the single XRD studies proved that the symmetry of the crystal system is triclinic with space group $P-1$. The material is stable up to 98 °C. It exhibits the usual dielectric behavior of metal coordinated carboxylates. The peaking of loss tangent at 6430 Hz indicates that the metal ion has two equally probable potential energy sites. The optical band gap obtained using the DRS studies is 2.4 eV. Magnetic studies in conjunction with structural information show that the material is weakly ferromagnetic.

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